Higgs boson implications for natural and unnatural theories

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The observed Higgs looks Standard Model



The observed Higgs looks Standard Model



What can we learn about higher energy scales?

Where is New Physics?

Hierarchy problem: $m_h \approx \Lambda$ $[\Lambda = highest scale h couples to]$

How to deal with it?

- $\rightarrow~$ The Fermi scale is natural ~~ [$\Rightarrow~$ NP at scale $\Lambda \lesssim ~\text{TeV}]$
- \rightarrow Multiverse: Fermi scale anthropic, near-critical, ...
- \rightarrow Third way(s)

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Outline

I Higgs boson and the SM up to higher energies Buttazzo, Degrassi, Giardino, Giudice, Salvio, S, Strumia arXiv:1307.3536

II Higgs boson and the NMSSM Barbieri, Buttazzo, Kannike, S, Tesi arXiv:1304.3670,1307.4937 Extrapolating the SM to higher energies

$$V(h) = -m^2 h^2 + rac{\lambda}{4} h^4$$
 $M_h^2 = 2\lambda v^2, \quad v^2 = rac{1}{\sqrt{2} G_\mu}$

Before LHC: $ightarrow M_h \lesssim 175 \; {
m GeV} \; {
m or} \; \lambda \; {
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 $\rightarrow M_h \gtrsim 110$ GeV or our vacuum is unstable Cabibbo et al. 1979,...

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m GeV}$ or our vacuum is unstable Cabibbo et al. 1979,...



Exponential sensitivity to $\lambda \& \lambda \lesssim 0 \Rightarrow$ precise computation needed!

Most accurate computation to date (full 2-loop)

 $\overline{\mathrm{MS}}$ parameters in terms of physical ones: G_{μ} , $\alpha_s(M_Z)$, M_t , M_h , M_Z , M_W

$$\lambda(\mu) = rac{G_{\mu}}{\sqrt{2}}M_{h}^{2} - \delta^{(1)}\lambda - \delta^{(2)}\lambda + \Delta_{\lambda}$$
 $G_{\mu} = rac{1}{\sqrt{2}v_{0}^{2}}(1 + \Delta r_{0})$
 $v_{
m OS}^{2} = rac{1}{\sqrt{2}G_{\mu}} \equiv ext{minimum of } V_{
m eff}(h)$

$$\delta^{(2)}\lambda = -\frac{G_{\mu}}{\sqrt{2}}M_{h}^{2}\left\{\Delta r_{0}^{(2)} + \frac{1}{M_{h}^{2}}\left[\frac{T^{(2)}}{v_{\rm OS}} + \delta^{(2)}M_{h}^{2}\right] - \Delta r_{0}^{(1)}\left(\Delta r_{0}^{(1)} + \frac{1}{M_{h}^{2}}\left[\frac{3\,T^{(1)}}{2\,v_{\rm OS}} + \delta^{(1)}M_{h}^{2}\right]\right)\right\}$$



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 $\overline{\mathrm{MS}}$ parameters in terms of physical ones: G_{μ} , $\alpha_s(M_Z)$, M_t , M_h , M_Z , M_W





Red dotted: Instability scale Λ_I in GeV.

Error on boundaries: α_s and theory



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Error on boundaries: α_s and theory

$$M_h > 129.6$$
GeV + 2.0($M_t - 173.35$ GeV) - 0.5GeV $\frac{\alpha_3(M_Z) - 0.1184}{0.0007} \pm 0.3$ GeV



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Error on boundaries: α_s and theory

$$M_h > 129.9 ext{GeV} + 2.0 (M_t - 173.35 ext{GeV}) - 0.5 ext{GeV} rac{lpha_3 (M_Z) - 0.1184}{0.0007} \pm 1 ext{ GeV}$$



Red dotted: Instability scale Λ_I in GeV.

Error on boundaries: α_s and theory

 $M_t < (171.36 \pm 0.15 \pm 0.25_{lpha_3} \pm 0.17_{M_h}) \text{GeV}$ vs

$$\Delta M_t = \pm 0.7_{exp} \pm 0.3_{th} \text{GeV}$$

In terms of Planck scale parameters



Legenda: No EW vacuum: $\lambda|_{\text{EW scale}} < 0$, Planck-scale dominated: $\Lambda_I > M_{\text{Planck}}$ Anthropic band Agrawal et al. 9707389

 λ and y_t are near-critical: accident or deeper meaning?

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Natural Supersymmetry [Dimopoulos Giudice '95, Cohen Kaplan Nelson '96]



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m_f [GeV]

Naturalness and m_h in the MSSM



Naturalness and m_h in the NMSSM

NMSSM Add singlet S $\Delta W = \lambda SH_uH_d + f(S)$ $\rightarrow m_h^2 \le m_Z^2 c_{2\beta}^2 + \Delta_t^2 + \lambda^2 v^2 s_{2\beta}^2 \Rightarrow$ Lighter stops allowed! \rightarrow Better fine tuning for $\lambda \ge 1!$...,Hall Pinner Ruderman 1112.2703

Naturalness and m_h in the NMSSM

Add singlet $S \qquad \Delta W = \lambda S H_{\mu} H_d + f(S)$ NMSSM

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 \rightarrow Better fine tuning for $\lambda \gtrsim 1!$...,Hall Pinner Ruderman 1112.2703



The Higgs sector

(CP-even scalars)

 $\rightarrow\,$ How Higgs measurements affect parameter space

 $\rightarrow\,$ Where to look for the other Higgses

ightarrow Sketch of a model for $\lambda\gtrsim 1$

Physical parameters

$$\mathcal{H}_{\rm ph} \equiv \begin{pmatrix} h_3 \\ h_1 \\ h_2 \end{pmatrix} = R^T \begin{pmatrix} H \\ h \\ S \end{pmatrix}, \quad R = R_{\delta}^{12} R_{\gamma}^{23} R_{\sigma}^{13} \qquad \qquad m_{h_1} = 125.7 \text{ GeV}$$
$$\mathcal{M}^2 = \begin{pmatrix} \widetilde{\mathcal{M}}^2(m_{H^{\pm}}^2, \lambda, t_{\beta}, \Delta_t) \\ v \mathcal{M}_1 & v \mathcal{M}_2 & \mathcal{M}_3^2 \end{pmatrix} = R^T \operatorname{diag}(m_{h_3}^2, m_{h_1}^2, m_{h_2}^2) R$$

Analytical relations!

$$\delta, \gamma, \sigma \left(\textit{m}_{\textit{h}_2}, \textit{m}_{\textit{h}_3}, \textit{m}_{\textit{H}^{\pm}}, \lambda, t_{\beta}, \Delta_t \right)$$

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$$\begin{split} & \begin{array}{l} \text{Analytical relations!} \quad \delta, \ \gamma, \ \sigma \left(m_{h_2}, \ m_{h_3}, \ m_{H^{\pm}}, \ \lambda, \ t_{\beta}, \ \Delta_t \right) \\ & s_{\gamma}^2 = \frac{\det \widetilde{\mathcal{M}}^2 + m_{h_1}^2 (m_{h_1}^2 - \operatorname{tr} \widetilde{\mathcal{M}}^2)}{(m_{h_1}^2 - m_{h_2}^2) (m_{h_1}^2 - m_{h_3}^2)} \quad s_{\sigma}^2 = \frac{m_{h_2}^2 - m_{h_1}^2}{m_{h_2}^2 - m_{h_3}^2} \ \frac{\det \widetilde{\mathcal{M}}^2 - m_{h_2}^2 (m_{h_3}^2 - \operatorname{tr} \widetilde{\mathcal{M}}^2)}{\det \widetilde{\mathcal{M}}^2 - m_{h_2}^2 m_{h_3}^2 + m_{h_1}^2 (m_{h_2}^2 - \operatorname{tr} \widetilde{\mathcal{M}}^2)} \\ & s_{2\delta} = \left[2s_{\sigma} c_{\sigma} s_{\gamma} \left(m_{h_3}^2 - m_{h_2}^2 \right) \left(2\widetilde{\mathcal{M}}_{11}^2 - m_{h_1}^2 c_{\gamma}^2 - m_{h_2}^2 (s_{\gamma}^2 + s_{\sigma}^2 c_{\gamma}^2) - m_{h_3}^2 (c_{\sigma}^2 + s_{\gamma}^2 s_{\sigma}^2) \right) \\ & + 2\widetilde{\mathcal{M}}_{12}^2 \left(m_{h_3}^2 \left(c_{\sigma}^2 - s_{\gamma}^2 s_{\sigma}^2 \right) + m_{h_2}^2 \left(s_{\sigma}^2 - s_{\gamma}^2 c_{\sigma}^2 \right) - m_{h_1}^2 c_{\gamma}^2 \right) \right] \\ & \times \left[\left(m_{h_3}^2 - m_{h_2}^2 s_{\gamma}^2 - m_{h_1}^2 c_{\gamma}^2 \right)^2 + \left(m_{h_2}^2 - m_{h_3}^2 \right)^2 c_{\gamma}^2 s_{\sigma}^4 \\ & + 2 \left(m_{h_2}^2 - m_{h_3}^2 \right) \left(m_{h_3}^2 + m_{h_2}^2 s_{\gamma}^2 - m_{h_1}^2 \left(1 + s_{\gamma}^2 \right) \right) c_{\gamma}^2 s_{\sigma}^2 \right]^{-1} \end{split}$$

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Two limiting cases

H decoupled:
$$m_{h_3} \gg m_{h_{1,2}}$$
 and $\sigma, \delta \to 0$ free par.s: $m_{h_2}, t_\beta, \Delta_t, \lambda$

S decoupled: $m_{h_2} \gg m_{h_{1,3}}$ and $\sigma, \gamma \to 0$ free par.s: $m_{h_3}, t_\beta, \Delta_t$

Higgs couplings and fit



Higgs couplings and fit



H decoupled case

 $[\delta, \sigma = 0, \text{ free parameters: } m_{h_2}, \lambda, t_{\beta}, \Delta_t]$



solines of
$$\sin^2 \gamma = \frac{m_{hh}^2 - m_{h_1}^2}{m_{h_2}^2 - m_{h_1}^2}$$

 $\lambda = 0.8$



 $\lambda = 1.4$



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H dec - phenomenology of h_2



CMS and ATLAS: work in progress...



H dec - phenomenology of h_2

 m_{h_2} < 250 GeV: signal strengths = $s_{\gamma}^2 \times$ Standard Model



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LHC? work in progress...

Baglio Djouadi Spira 1212.5581

H dec - h_2 lighter than h_1

FIT: again LHC14 impact is mild $(\lambda = 1.4 \text{ wants } t_{\beta} > 10)$ h_2 pheno: again signal $= s_{\gamma}^2 \times SM$, direct searches not (yet) competitive



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S decoupled case

 $[\gamma, \sigma = 0, \text{ free parameters: } m_{h_3}, t_{eta}, \Delta_t]$

$$\frac{g_{h_3tt}}{g_{htt}^{SM}} = s_{\delta} - \frac{c_{\delta}}{t_{\beta}} \qquad \frac{g_{h_3bb}}{g_{hbb}^{SM}} = s_{\delta} + t_{\beta}c_{\delta} \qquad \frac{g_{h_3VV}}{g_{hVV}^{SM}} = s_{\delta} \qquad \left[\Delta_t = 75 \text{ GeV}\right]$$

LHC8 fit status:

dashed: $m_{H^{\pm}}$ cont: λ



 h_3 pheno: more similar to MSSM, CMS and ATLAS are looking for it

S decoupled case



LHC14 fit projections (300 fb^{-1}):

dashed: $m_{H^{\pm}}$ cont: λ



 h_3 pheno: more similar to MSSM, CMS and ATLAS are looking for it

Fully mixed case and $h_2 \rightarrow \gamma \gamma$

Signal strengths relative to the SM

$$[m_{h_3} = 500 \text{ GeV}, s_{\sigma}^2 = 0.001, v_s = v]$$

 $\lambda = 0.1$ $\Delta_t = 85 \text{ GeV}$





 $h_2 > h_{
m LHC}$: harder to have an enhancement

[free parameters: m_{h_3}, t_{β}]



LHC14 fit projections: above regions completely filled, up to $m_{h_3}\simeq 1~{
m TeV}$

$$\left[\text{if } \frac{\mu A_t}{m_t^2} \text{ very large this conclusion could change } \right]$$

 $\gtrsim 1~\text{TeV}$ from LHC14!

 $m_{h_{2,3}}(\text{NMSSM})$ can be much lighter!

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• Where to look for another Higgs?

H-dec: $h_2 \rightarrow hh$, or SM-like S-dec: $h_3 \rightarrow \bar{t}t, \bar{b}b, ...$

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• Where to look for another Higgs? H-dec: $h_2 \rightarrow hh$, or SM-like S-dec: $h_3 \rightarrow \overline{t}t, \overline{b}b, ...$

• Other effects? Large deviations in λ_{hhh} allowed in H-dec case

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Living with a $\lambda \gtrsim 0.7$

 $m_h \simeq 126 \text{ GeV} + \text{Naturalness} \Rightarrow \lambda (\text{weak scale}) \gtrsim 0.8$ Hall Pinner Ruderman 1112.2703, ... λ perturbative up to GUT scale $\Rightarrow \lambda (\text{weak scale}) \lesssim 0.7$ Espinosa Quiros PLB 279 (1992), ...

Ways out

Add max number of families in $\overline{5} + 5$ of SU(5) that do not spoil GUT

 $\Rightarrow\lambda\lesssim$ 0.8 Masip Munoz-Tapia Pomarol hep-ph/9801437,...

Promote (some of) S, H_u, H_d to composite objects

Harnik et al. hep-ph/0311349, ...

 $\Rightarrow\lambda\lesssim2$, not bigger otherwise strong sector at \sim 10 TeV (EWPT)

• Field content: NMSSM + vector-like $F_u \sim 5$ and $F_d \sim \overline{5}$ of SU(5)

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- Superpotential W: PQ symmetric, SU(5) broken only by $H_{u,d}$

 $W = \lambda_S SF_u F_d + M_u F_u \overline{F}_u + M_d F_d \overline{F}_d + m_u H_u \overline{h}_u + m_d H_d \overline{h}_d + \lambda_t H_u Qt$

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$$\begin{array}{l} \rightarrow \ S, \ \hat{H}_u = c_u H_u + s_u h_u, \ \hat{H}_d = c_d H_d + s_d h_d \ \text{are massless} \\ \\ \rightarrow \ \hat{W} = \lambda S \hat{H}_u \hat{H}_d + y_t \hat{H}_u Qt, \quad \lambda = \lambda_S s_u s_d, \ y_t = \lambda_t c_u \end{array}$$

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Add PQ-breaking soft terms at Fermi scale

Growth of λ cured above $M_{u,d}, m_{u,d} \lesssim 1000$ TeV $(\lambda \lesssim 1.5)$

Learning from the Higgs boson: unnatural (I) and natural (II) new physics

I SM vacuum metastable, λ and y_t near-critical [deep message?]

II NMSSM Higgs sector, insisting on physical parameters

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