
Naturalness and Higgs decays in the MSSM with a singlet– *searching for a stealthy Higgs*

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LBNL

Layout

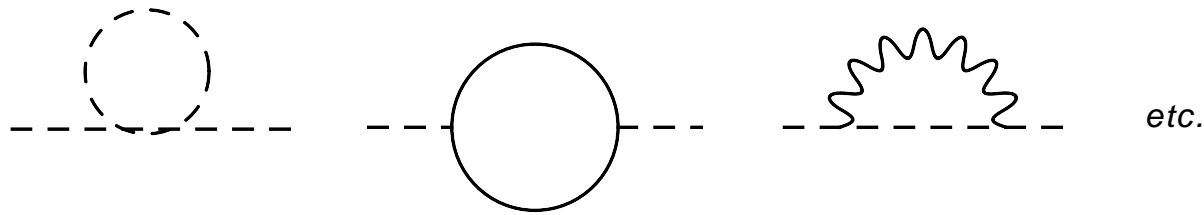
- SUSY little hierarchy problem and a possible solution
- Higgs limits from LEP
- MSSM+S \neq NMSSM and its new operators
- New phenomenology
- Conclusions and the future

Hierarchy problem

- EWSB in SM driven by fundamental scalar, the Higgs

$$V_{classical} = \lambda(|\phi|^2 - v^2)^2$$

- Higgs potential receives large radiative corrections

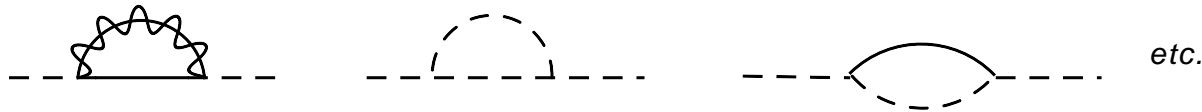


$$\Delta m_{\phi}^2 \sim \frac{\lambda^2}{16\pi^2} \Lambda^2$$

Hierarchy problem

- Naturalness arguments tell us $\Lambda \sim \text{TeV}$
- New physics at a TeV
- Technicolour, Little Higgs, Extra Dimensions, **Supersymmetry**

Low scale SUSY introduces superpartners below the TeV scale to cut off quadratic divergences



Hierarchy problem

- **The good:** Superpartners soften divergence

$$\frac{\lambda^2}{16\pi^2}\Lambda^2 \rightarrow \frac{y^2}{16\pi^2}m_{\tilde{t}}^2 \log \frac{\Lambda}{m_{\tilde{t}}}$$

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$$m_h^2 \leq m_z^2 \cos^2 2\beta$$

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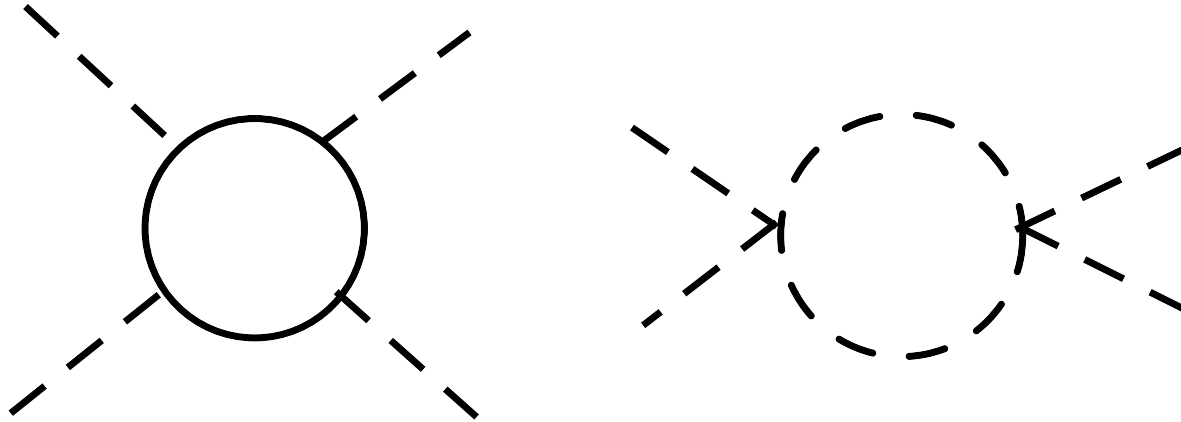
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- **The ugly(?):** Need to raise Higgs mass, e.g. increase quartics. Loop corrections, NMSSM, Fat higgs, non-decoupling D-terms, little supersymmetry etc.

SUSY little hierarchy problem

One loop corrections to Higgs quartic increase Higgs mass



$$\delta\lambda \rightarrow \Delta m_h^2 = \frac{3y_t^2}{4\pi^2} m_t^2 \log \left(\frac{m_{\tilde{t}}^2}{m_t^2} \right)$$

Compare

$$\Delta m_H^2 = -\frac{3y_t^2}{4\pi^2} m_{\tilde{t}}^2 \log \frac{\Lambda}{m_{\tilde{t}}}$$

SUSY little hierarchy problem

- LEP bound on SM-like Higgs (much of MSSM parameter space) $m_h > 114\text{GeV}$
- Requires heavy stops ($\mathcal{O}(400\text{GeV})$), large quartic corrections
- Fine-tuning ($\mathcal{O}(5\%)$) of soft Higgs mass against μ -term to get $v = 174\text{GeV}$
- Alternative ways of raising quartic? e.g. NMSSM, little SUSY, fat Higgs, non-decoupling D-terms.....

Or, keep Higgs (and stops) light and instead evade LEP constraints

Non-standard Higgs decays \rightarrow new states coupled to Higgs, **not** invisible decays.

MSSM + singlet

- Extend the Higgs sector in the simplest possible way:
MSSM + $S \neq$ NMSSM [Gunion et al.]
- NMSSM assumes $\langle S \rangle = \mu$. Make assumptions about UV theory
- We are interested in phenomenological questions about Higgs decays
- New, previously ignored operators, new decays
 - Supersoft [Nelson, Weiner and PF]
 - New vector-like matter coupled to S [Dobrescu, Landsberg, Matchev]
 - $S = s + ia + \theta\psi_s + \dots$

Rough calculation

Can non-standard decays dominate?

$$\Gamma_{h \rightarrow 2a} \gtrsim 4 \times \Gamma_{h \rightarrow bb}$$

$$\mathcal{L} \supset \frac{c}{\sqrt{2}} v h a^2$$

$$\Gamma_{h \rightarrow 2a} = \frac{c^2 v^2}{16\pi m_h} \left(1 - 4 \frac{m_a^2}{m_h^2}\right)^{1/2}$$

$$\Gamma_{h \rightarrow 2b} = \frac{3m_b^2}{16\pi v^2} m_h \left(1 - 4 \frac{m_a^2}{m_h^2}\right)^{3/2}$$

$$\Gamma_{h \rightarrow 2a} \gtrsim 4 \times \Gamma_{h \rightarrow bb} \Rightarrow \frac{cv}{\sqrt{2}} \gtrsim 5 \text{ GeV}$$

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Yes!

Effects of mixing

Mass eigenstates related to interaction eigenstates by,

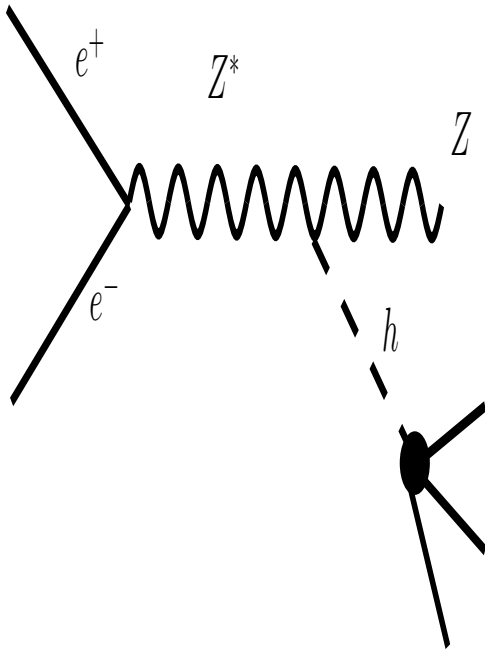
$$\begin{pmatrix} \tilde{s} \\ \tilde{h} \end{pmatrix} = \begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} s \\ h \end{pmatrix}$$

$$m_{\tilde{h}}^2 = \frac{m_{mssm}^2 - m_{\tilde{s}}^2 \sin^2 \theta}{\cos^2 \theta}$$

An increase in mass through mixing without radiative corrections, alleviates tuning.

LEP limits

LEP limits usually quoted as limits on ξ^2
(or c^2 or k or ...)



$$\xi_X^2 \equiv \frac{\sigma(e^+e^- \rightarrow hZ)}{\sigma(e^+e^- \rightarrow hZ)_{SM}} \times BR(h \rightarrow X)$$

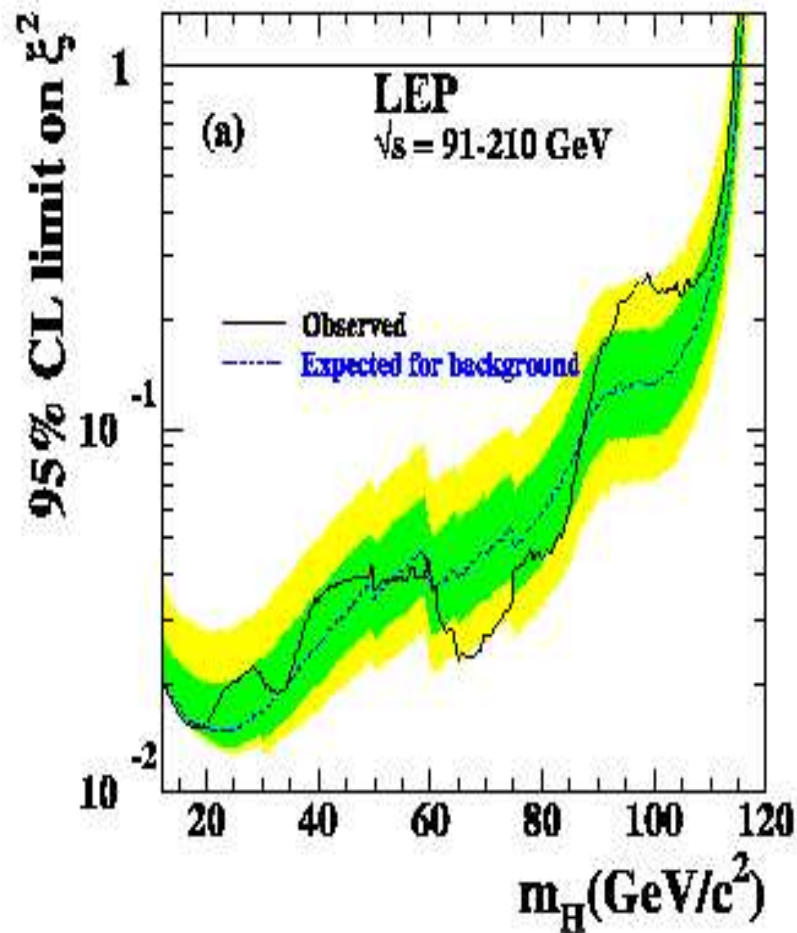
$$\left(\begin{array}{l} \text{SM higgs : } m_h \geq 114.4\text{GeV} \\ \text{Invis. higgs : } m_h \geq 114\text{GeV} \\ \text{Model indep. : } m_h \geq 81\text{GeV} \end{array} \right)$$

@ 95% CL ($\xi^2 = 1$)

We will be most interested in the constraints on cascade decays

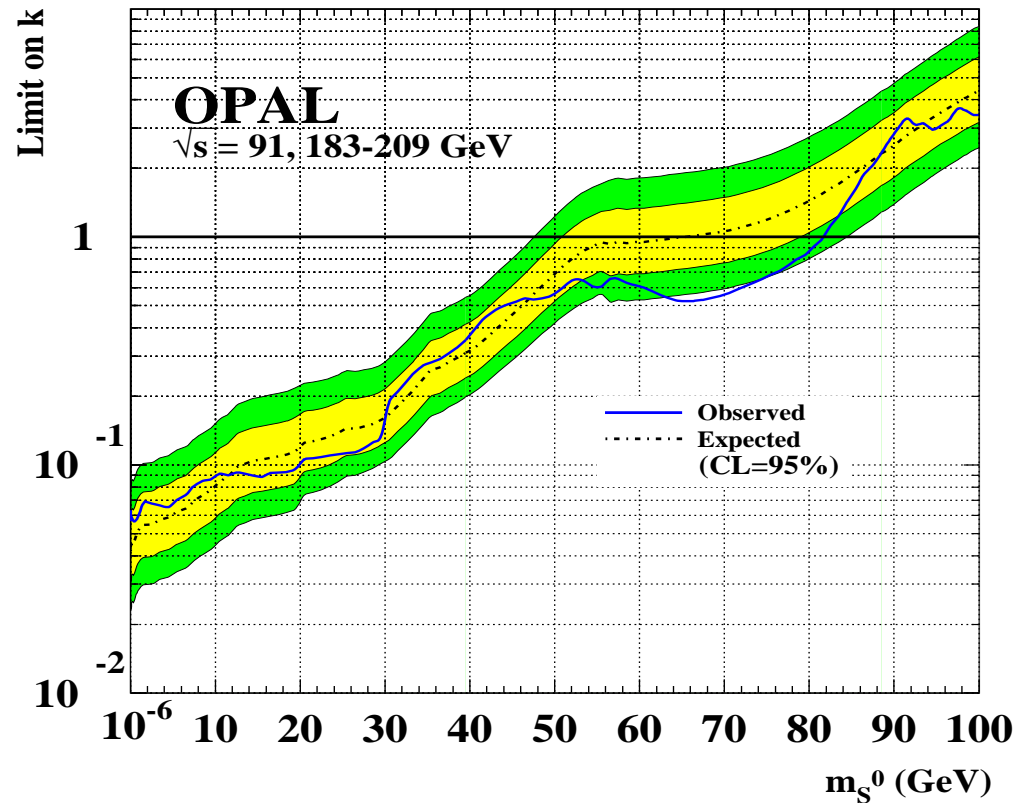
LEP constraints–SM like

$m_h \geq 114.4\text{GeV}$ [André Sopczak, SUSY05]



Model Independent

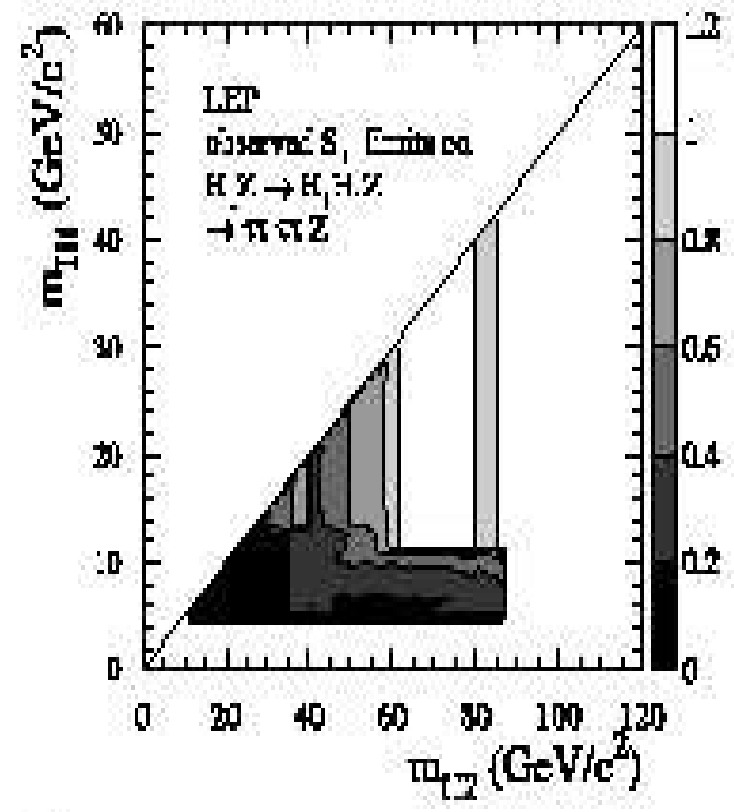
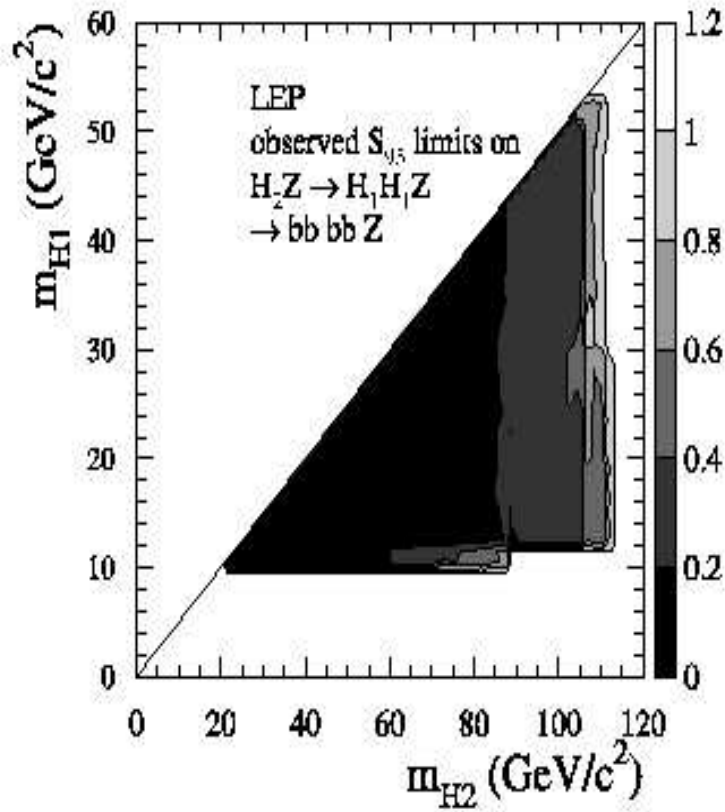
$$m_h \geq 81 \text{ GeV}$$



[*Eur. Phys. J. C* **27** (2003) 311-329; hep-ex/0206022]

Cascade decays

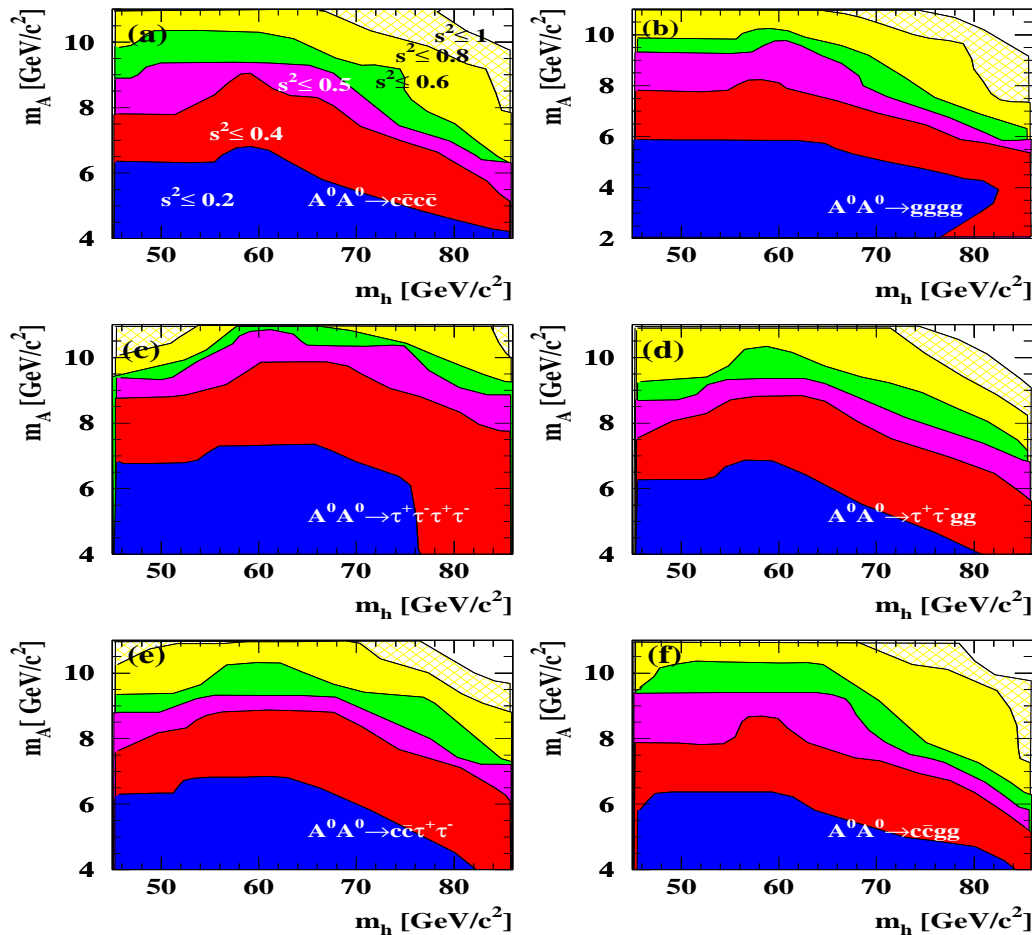
$m_h \geq 110\text{GeV}$ for 4b final state [André Sopczak, SUSY05]



Cascade decays

$$m_h \geq 86 \text{ GeV}, \text{ if } m_a \lesssim 12 \text{ GeV}$$

OPAL



New Operators with singlets

NMSSM

$W = \lambda_S S H_u H_d + \kappa_S S^3 \leftarrow$ Supersymmetric

$V = \lambda_S A_\lambda S H_u H_d + \kappa_S A_\kappa S^3 + m_S^2 |S|^2 + c.c. \leftarrow$ soft SUSY breaking

Additional possible terms

- $\delta_s^2 s^2, \delta_a^2 a^2$ —Scalar/pseudo-scalar masses
- Mixing term: $m_{CP}^2 s a$
- $\lambda_Q S Q \bar{Q} + M_Q Q \bar{Q}$ —Fermiophobic decays
- Supersoft operator: $W'_\alpha W^\alpha S$

NMSSM-like operators

Superpotential: $\lambda_s S H_u H_d$

Leads to **mixing**

$$\begin{pmatrix} \lambda_h^2 v^2 + \delta_s^2 & -2\lambda_h v \tilde{\mu} s_{\alpha-\beta} & 2\lambda_h v \tilde{\mu} c_{\alpha-\beta} \\ -2\lambda_h v \tilde{\mu} s_{\alpha-\beta} & m_h^2 & 0 \\ 2\lambda_h v \tilde{\mu} c_{\alpha-\beta} & 0 & m_H^2 \end{pmatrix}$$

Decays $h \rightarrow 2s, 2a$ and $s \rightarrow 2a$

NMSSM-like operators

A-term: $A_h S H_u H_d$

- Generated at the loop level if $\lambda_h S H_u H_d$ is present
- Mixes A^0 and a , allows $a \rightarrow 2b/2\tau$
- Have $h \rightarrow 2s, 2a$ and $s \rightarrow 2a$

$$\begin{pmatrix} \delta_s^2 & A_h v \cos(\alpha + \beta) & A_h v \sin(\alpha + \beta) \\ A_h v \cos(\alpha + \beta) & m_h^2 & 0 \\ A_h v \sin(\alpha + \beta) & 0 & m_H^2 \end{pmatrix}$$

$$\begin{pmatrix} m_a^2 & -A_h v \\ -A_h v & m_A^2 \end{pmatrix}$$

NMSSM-like operators

Superpotential and A-term have similar affect on Higgs physics

$$A_S S^3$$

- Alone this does little, (opposite) contribution to scalar masses.
- With another source of mixing gives $h \rightarrow 2s, 2a$

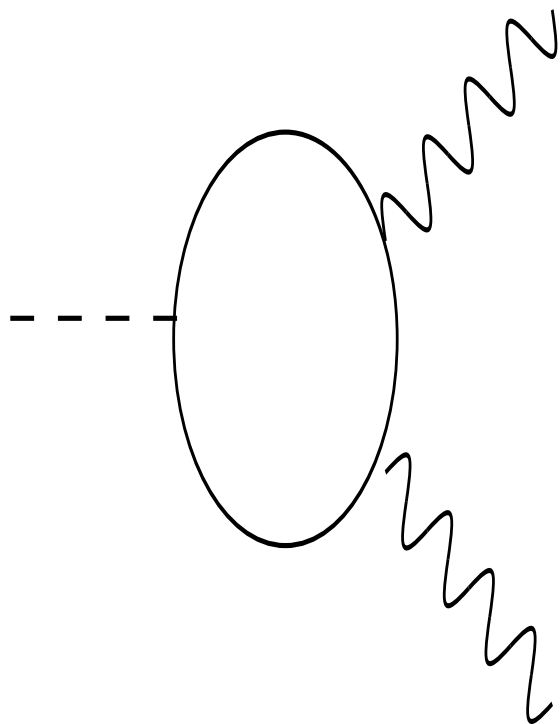
Other Operators

Mixing term: $m_{CP}^2 sa$

- Does *not* violate CP by itself, only if a couples to fermions or gauge bosons, or mixes with A^0 —no EDM problems.
- Can induce $h \rightarrow sa$ if $h \rightarrow 2s$ forbidden. e.g. with supersoft

Other Operators

$$\lambda_Q S Q \bar{Q} + M_Q Q Q \bar{Q}$$



Fermiophobic
decays

- Integrate out heavy coloured matter, loop induced $s, a \rightarrow 2g/2\gamma$ decays
- Dominant for a , if small mixing between a and A^0 through loop-induced A_h
- Branching ratios for $h \rightarrow 2a \rightarrow (4g, 2g2\gamma, 4\gamma) = (0.99, 7.6 \times 10^{-3}, 1.5 \times 10^{-5})$
- Viable search channel at TeVatron/LHC?—possibly [Dobrescu, Landsberg Matchev]

Other operators—Supersoft

Source of SUSY breaking is a D-term in a hidden sector $U(1)$. [Nelson, Weiner and PF]

In presence of SM adjoints, (e.g. S),

$$\int d^2\theta \sqrt{2} \frac{W'_\alpha W_j^\alpha A_j}{M} + \text{h.c.} \rightarrow$$

$$\mathcal{L} \supset -m_D \lambda_j \tilde{a}_j - \sqrt{2} m_D (a_j + a_j^*) D_j - D_j \left(\sum_i g_k q_i^* t_j q_i \right) - \frac{1}{2} D_j^2$$

offshell, and onshell ($m_D = D'/M$)

$$\mathcal{L} \supset -m_D \lambda_j \tilde{a}_j - m_D^2 (a_j + a_j^*)^2 - m_D (a_j + a_j^*) \left(\sum_i g_k q_i^* t_j q_i \right)$$

Supersoft

- ESPs marry gauginos → **Dirac gaugino masses**
- Real scalar piece of ESP gets a tree level mass
- New scalar trilinear interaction, no analogue in MSSM
- Scalar masses not even log sensitive to high scale, running stops at gaugino mass.

Supersoft

In MSSM+S we have an adjoint.

$$\mathcal{L} = \int d^2\theta \frac{W'_\alpha}{M} W_Y^\alpha S + h.c. \rightarrow -\frac{1}{2}(m_D s + D_Y)^2 + \frac{m_D}{2} \psi_S \lambda$$

$D_Y = \sum_i g_Y q_i \phi_i^* \phi_i$ Mixing from this operator leads to,

$$\begin{pmatrix} m_D^2 + \Delta_s^2 & \frac{gm_D v s_{\alpha+\beta}}{\sqrt{2}} & -\frac{gm_D v c_{\alpha+\beta}}{\sqrt{2}} \\ \frac{gm_D v s_{\alpha+\beta}}{\sqrt{2}} & m_h^2 & 0 \\ -\frac{gm_D v c_{\alpha+\beta}}{\sqrt{2}} & 0 & m_H^2 \end{pmatrix}$$

Also leads to $h \rightarrow ss$ decays

Necessary operators

- a should decay: A_h, m_{CP}^2, M_Q^{-1}
- h should have cascade decays: m_D, λ_h, A_s (with source of mixing from another operator), A_h
- If s is light it also needs cascade decays (unless below 12 GeV): λ_h (with source of mixing from another operator), A_s, A_h (with source of mixing from another operator), m_{CP}^2

Some operators better than others

Scenarios

- Mixing with s pushes higgs heavy, $m_h \geq 114\text{GeV}$, or 110GeV for $4b$ final state
- Single stage higgs decays $h \rightarrow 2a \rightarrow 2X$. If $X = b\bar{b}$, $m_h \geq 110\text{GeV}$, if $X = 2\tau$ (tuned?), $m_h \gtrsim 86\text{GeV}$ or $X = 2g$ $m_h \gtrsim 82\text{GeV}$
- Double stage decay $h \rightarrow 2s \rightarrow 4a \rightarrow 4X$ or $h \rightarrow as \rightarrow 3a \rightarrow 3X$, $m_h \geq 82\text{GeV}$

Two types of tuning

- $\frac{\partial \log m_Z}{\partial \log \text{"parameter"}} \sim \text{stop mass}$
- Spectral tuning to avoid experimental constraints

Single stage cascades

$$h \rightarrow 2a \rightarrow 4b$$

Least tuning with supersoft: $m_D, A_s, m_{\tilde{t}} = 325\text{GeV} \Rightarrow$

$\sin^2 \theta$	$m_{\tilde{h}}$	$m_{\tilde{s}}$	$m_{\tilde{a}}$	$B(\tilde{h} \rightarrow 2\tilde{a})$	$B(\tilde{s} \rightarrow 2\tilde{a})$	tuning
0.1	109	73.8	32.6	0.86	.99	3%

Light stops, but still “tuned”—Just so region

Single stage cascades

$$h \rightarrow 2a \rightarrow 4g, 4\tau$$

- Possible with λ_h and M_Q^{-1} but need A_h small.
- Less tuned with m_D , A_s and M_Q^{-1} (A_h for 4τ),
 $m_{\tilde{t}} = 175\text{GeV} \Rightarrow$

$\sin^2 \theta$	$m_{\tilde{h}}$	$m_{\tilde{s}}$	$m_{\tilde{a}}$	$B_{\tilde{h} \rightarrow 2\tilde{a}}$	$B_{\tilde{s} \rightarrow 2\tilde{a}}$	tuning
.22	94.9	76.2	28.3	.92	.99	100%
			(8.37)	(.93)		(10%)

Tuning comes about from making $m_a < 12\text{GeV}$

Fermiophobic Higgs

$$h \rightarrow 2a \rightarrow 4g, 2g2\gamma, 4\gamma$$

- Very hard to see at TeVatron/LHC
- To reconstruct Higgs at LHC need 4γ channel
- Dominant backgrounds (small) are $n \text{ jets} + (4 - n)\gamma$, pileup events
- Consistent pairs trick
- $\text{Br} \gtrsim \text{few} \times 10^{-4}$ discoverable with 300 fb^{-1}

Double stage cascades

$$h \rightarrow 2s \rightarrow 4a \rightarrow 8g, 8b, 8\tau$$

- Tough to get with λ_h since s lighter than a .
- Final states never searched for, complicated
- m_D, A_s and M_Q^{-1} or $A_h, m_{\tilde{t}} = 360\text{GeV} \Rightarrow$

$\sin^2 \theta$	$m_{\tilde{h}}$	$m_{\tilde{s}}$	$m_{\tilde{a}}$	$B_{\tilde{h} \rightarrow 2\tilde{a}}$	$B_{\tilde{h} \rightarrow 2\tilde{s}}$	$B_{\tilde{s} \rightarrow 2\tilde{a}}$	tuning
.06	111	39.3	16.2	.35	.50	.99	4%
			(7.13)	(0.36)	(0.49)		(2%)

$$\tilde{h} \rightarrow \tilde{a}\tilde{s} \rightarrow 3\tilde{a} \rightarrow 6b, 6\tau$$

$\sin^2_{\theta_{sh}}$	$\sin^2_{\theta_{ah}}$	$m_{\tilde{h}}$	$m_{\tilde{s}}$	$m_{\tilde{a}}$	$B_{\tilde{h} \rightarrow \tilde{a}\tilde{s}}$	$B_{\tilde{s} \rightarrow 2\tilde{a}}$	tuning
0.10	.01	103	67.0	18.4	.70	.91	100%
			(66.6)	(9.87)	(0.69)	(0.96)	18%

Benchmark summary

Simple(st?) extension of MSSM greatly enhances Higgs phenomenology, different from NMSSM.

- $h \rightarrow 2a \rightarrow 4b$ Just so, less tuned with supersoft
- $h \rightarrow 2s/2a \rightarrow 4\tau$ Requires spectral tuning. OPAL limits stop at 86GeV—**Why?—new analysis**
- $h \rightarrow 2a \rightarrow 4g$ Higgs as light as 82GeV, only OPAL did model independent. Possible $2g2\gamma$ or 4γ signals
- $\tilde{h} \rightarrow \tilde{a}\tilde{s} \rightarrow 3\tilde{a} \rightarrow 6b, 6\tau$ little tuning with supersoft, not present in NMSSM. Higgs as light as 82GeV
- $h \rightarrow 2s \rightarrow 4a \rightarrow 8g, 8b, 8\tau$ only with supersoft, not in NMSSM

Lesson: pheno first model later.

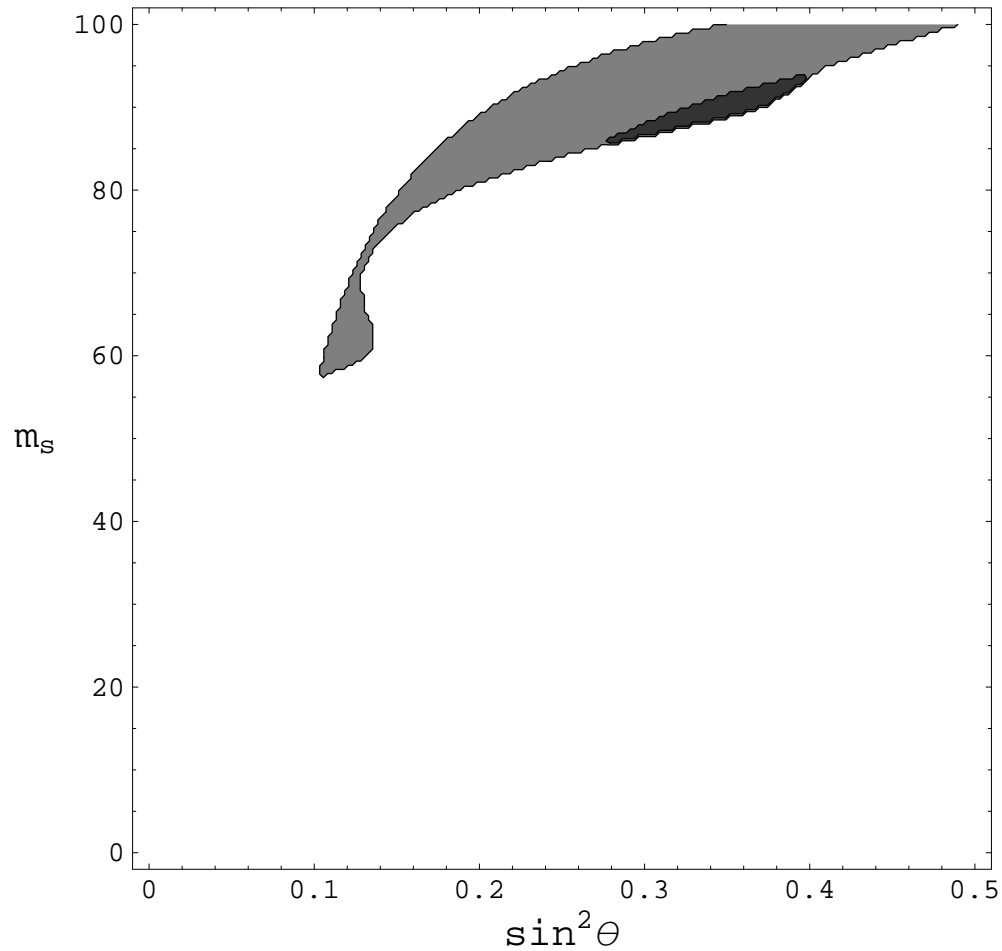
Conclusions and the future

- MSSM suffers from LHP
- *Lowering* Higgs mass and giving it novel decays also solves problem, allows for light stops
- MSSM+S \neq NMSSM
- Consider all operators, in particular supersoft and new coloured matter
- Tunings come in two forms

Conclusions and the future

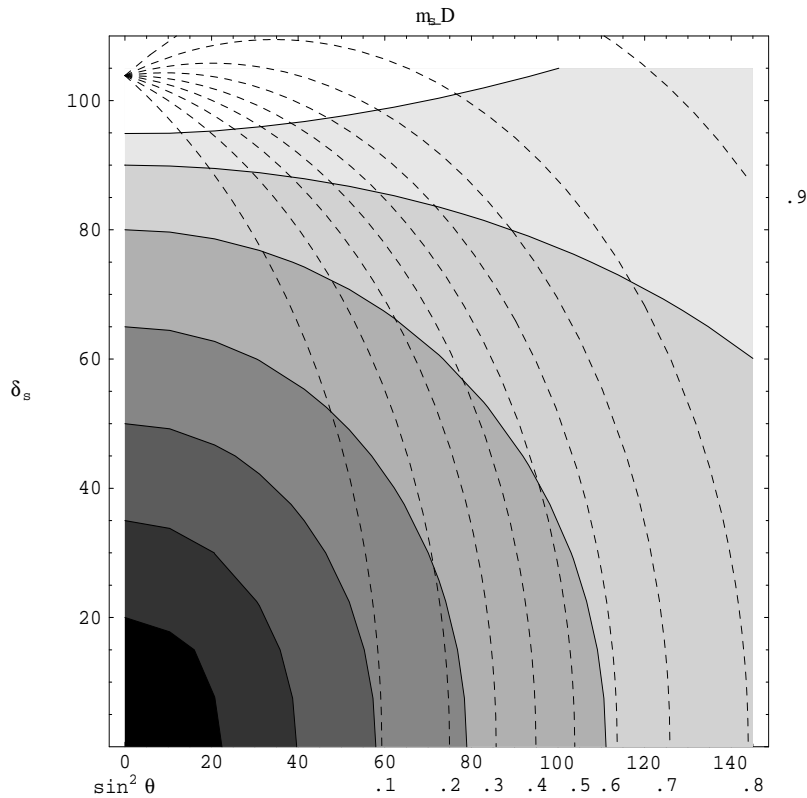
- New signals from general analysis
- New signals demand new analyses e.g. model independent, low a mass
- New scenarios with light (stealthy) higgs **and** light superpartners
- New analyses for LHC and beyond e.g. 4γ final state

Allowed regions



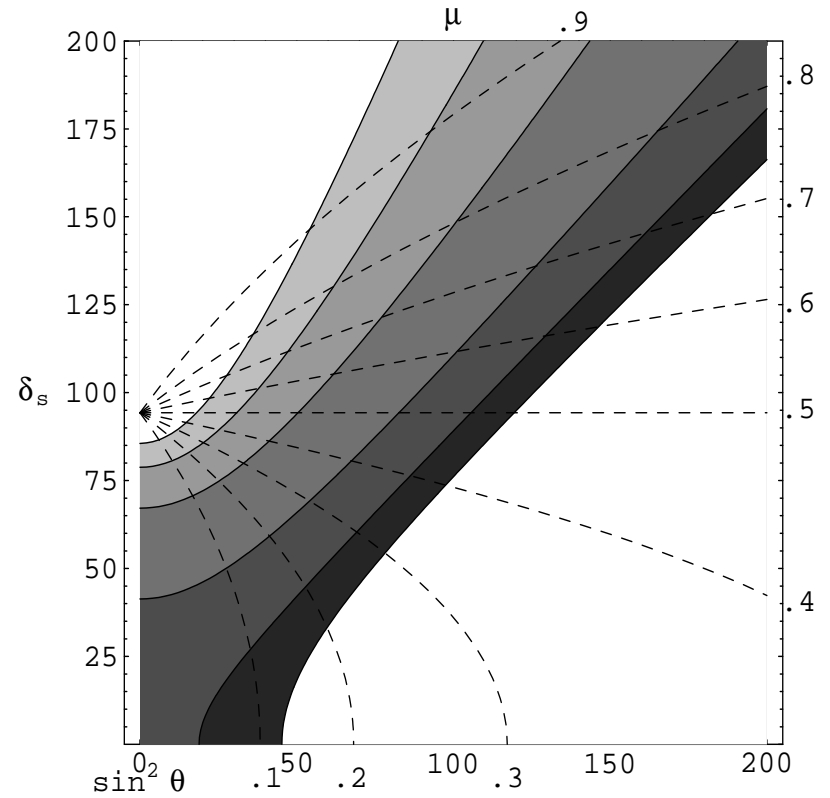
Allowed regions if $h \rightarrow 2a \rightarrow 4b, s \rightarrow 4b, m_{\tilde{t}} = 300\text{GeV}$

Possible realisations



Using supersoft operator

darkest to lightest—20,25,50,65,80,90,95 GeV



Using superpotential ($\lambda_h = 0.25$)

darkest to lightest—20,40,60,80,90,96 GeV