Exercise 1

1. Consider from the superpotential

$$W = \frac{1}{2}M\phi_H^2 + \frac{\lambda}{2}\phi_H\phi^2 + \frac{\delta}{3}\phi_H\phi^3 + \frac{y}{6}\phi_H^3 ,$$

find the exact effective superpotential after integrating out ϕ_H . Can you argue from holomorphy what the general form of the effective superpotential has to be?

2. Using holomorphy and symmetries show that the superpotential

$$W = \mu_1 \phi + \mu_2 \phi^2 + \ldots + \mu_n \phi^n + \ldots$$

is not renormalized.