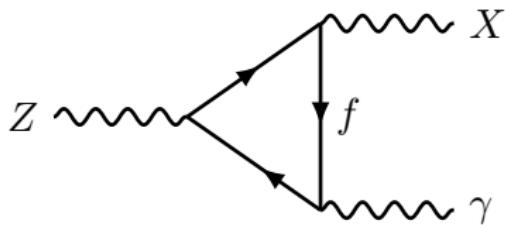


# Constraints on non-conserved gauge currents

*why UV consistency matters*

1705.06726, 1707.01503, 180X.XXXXX

**Jeff Dror**, Robert Lasenby, Maxim Pospelov



# Introduction



- Why **light vectors?**
  - Hidden sectors
  - Experimental hints
- **Generalizing the vector portal**
- Gauging **anomalous symmetries**
  - Non-decoupling heavy fermions
  - Example: baryon number vector
  - Constraints
- Gauging symmetries **broken at tree-level**
  - Axial couplings
  - Weak-isospin violating
  - Mass-mixed with the  $Z$
- “Real life” applications
  - Beryllium anomaly

- The energy frontier has driven the field for the several decades
- Standard Model (SM) able to explain all current data
- Looking in the wrong place?
- New particles below the electroweak scale?
  - ① Light particle could be **mediator** to dark sector



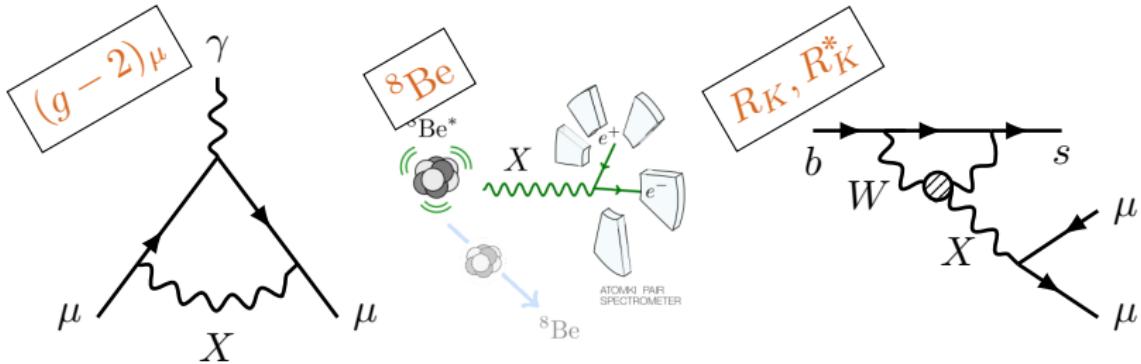
- ② Useful to **explain experimental-anomalies**
- ③ Be open minded: “**Who ordered that?**”





- Scalar portal,  $\phi$ ,  
 $\phi |H|^2, \phi^2 |H|^2, \dots$
- Fermionic portal,  $N$ ,  
 $HLN, \dots$
- **Vector portal**,  $X^\mu$ ,  
 $F_{\mu\nu}X^{\mu\nu}, X_\mu J_{B-L}^\mu, X_\mu J_{L_\mu - L_\tau}^\mu, \dots$
- SM: **EM,  $B - L$ ,  $L_\mu - L_\tau$ , etc. are conserved**
- Coupling to **conserved** currents → straightforward but restrictive
- Relax this requirement?

- Many experimental hints for **new light states**



- Others: proton radius puzzle, 3.5 keV line, ...
- ${}^8\text{Be}$  anomaly models - **fun application of new constraints**

# How to introduce these particles?



- Fundamental spin-1 particles are tricky
- Cause amplitudes to grow with energy ( $\Rightarrow$  **unitarity violation**)
- e.g.,

$$f \rightarrow f \text{ (with a } X \text{ loop)} \quad \Rightarrow \mathcal{M}^\mu \propto \frac{q^\mu}{m_X} \sim \frac{E}{m_X}$$

- $1/m_X$  behavoir consequence of non-conserved current:

$$\partial_\mu j^{\mu 5} = 2im_\psi \bar{\psi} \gamma^5 \psi$$

- Avoid growth by choosing charges of a symmetry
- Safe choices  $\rightarrow$  good symmetries of SM

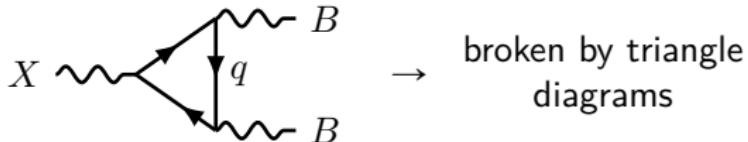
# Gauging “bad” symmetries



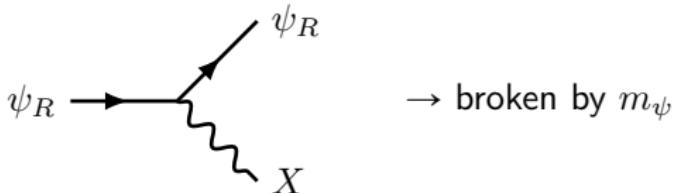
- We can gauge symmetries **broken in the SM!**

- Breaking can be

- at **quantum-level** (e.g., baryon number vector)



- at **tree level** (e.g., axial couplings)



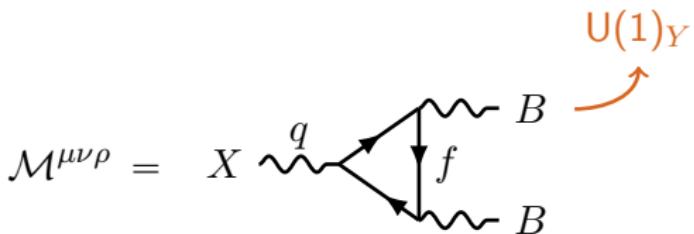
- $\partial_\mu J_X^\mu \neq 0$  leads to rates enhanced by  $(E/m_X)^2$ 
  - $\Rightarrow$  unitarity violation



- Focus on symmetries violated by the chiral anomaly
- Can see breaking at amplitude level using Ward Identity:

$$q_\rho \mathcal{M}^\rho(q) = 0$$

- **Chiral anomaly:**



- UV divergent: chose regulator which preserves SM

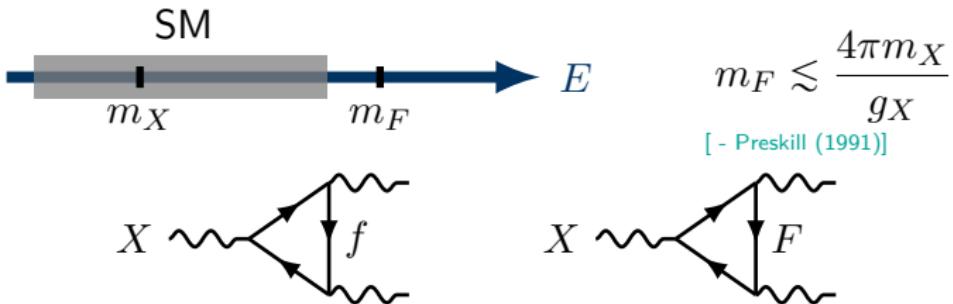
$$q_\rho \mathcal{M}^{\mu\nu\rho} = \frac{g_X g'^2}{12\pi^2} \sum_{f \in \text{quarks}} X_f Y_f^2 \epsilon^{\mu\nu\rho\sigma} k_\rho p_\sigma$$

- Now study assumption further

# Theory needs “fixing”



- Introduce heavy  $U(1)_X$  chiral fermions (SM-chiral ruled out)

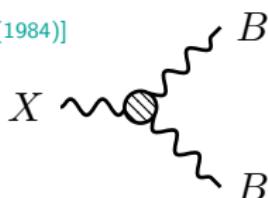


**Cancel anomaly:**  $\sum_f X_f Y_f^2 = - \sum_F X_F Y_F^2$

[ - D'Hoker, Farhi (1984)]

- But these fermions don't decouple!

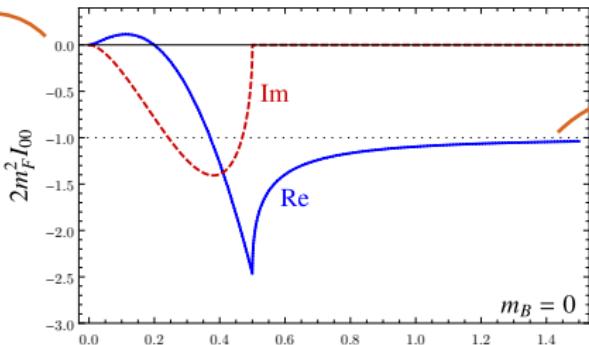
- For  $E \ll m_F$  have effective interactions:



- Massless SM + new fermions,  $F$ :

$$-q_\rho \mathcal{M}^{\mu\nu\rho} = \left( 0 + \frac{g'^2 g_X}{12\pi^2} \sum_F 2m_F^2 I_{00}(m_F) X_F Y_F^2 \right) \epsilon^{\nu\rho\lambda\sigma} p_\lambda k_\sigma$$

anomaly  
cancelled



constant value  
for  $m_F \gg m_X$ !

$$\lim_{m_F \gg m_X} q_\rho \mathcal{M}^{\mu\nu\rho} = -\frac{g'^2 g_X}{12\pi^2} \sum_F \overbrace{X_F Y_F^2}^{= - \sum_f X_f Y_f^2} \epsilon^{\nu\rho\lambda\sigma} p_\lambda k_\sigma$$

# 3-pt vertex



- How to derive 3-pt interaction in SM+ $X$  EFT?
- Regulator uniquely determines assumption about UV
- In full theory chose regulator **valid for energy**  $\rightarrow \infty$
- Impossible in the SM+ $X$  EFT
- Can choose:
  - ① **EFT breaks  $SU(2)_L \times U(1)_Y$**  (heavy fermions are SM-chiral)
  - ② **EFT breaks  $U(1)_X$**  (heavy fermions are  $U(1)_X$ -chiral)
- If EFT breaks EW symmetry
  - Heavy fermions get mass from Higgs
  - **ruled out**
- Alternatively, EFT breaks  $U(1)_X$ 
  - leads to amplitudes growing with **energy/ $m_X$** !

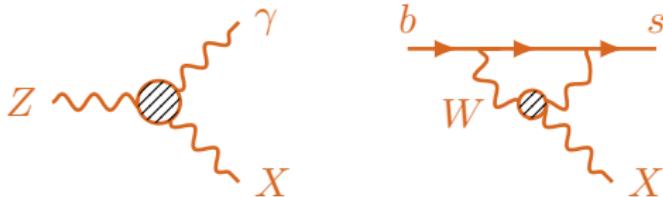
# Effective interactions



- Longitudinal model dominates,  $X_\mu \rightarrow \partial_\mu \varphi / m_X$
- Triangle diagrams arise from (assuming EFT breaks  $U(1)_X$ ),

$$\mathcal{L}_{\text{eff}} = \frac{g_X}{16\pi^2 m_X} \left[ \sum_f X_f Y_f^2 \right] \varphi (g^2 W^a \tilde{W}^a - g'^2 B \tilde{B})$$

- Need to add to  $\mathcal{L}_X$ !
- New processes: [JD, Pospelov, Lasenby - 1705.06726]



- These grow with energy,  $\mathcal{M} \propto E/m_X$ !

# Frequently Asked Questions (FAQ)



① What happens with  $B - L$  below  $m_t$ ?



- Theory appears anomalous
- $B - L$  is good symmetry  $\rightarrow$  can't exist "anomalous" interactions
- Integrating out top breaks EW ( **top is EW chiral**)
- Below  $m_t$ ,  $\partial_\mu J_{EW}^\mu \neq 0$  but  $\partial_\mu J_X^\mu = 0$
- Rates "enhanced" by  $E^2/m_W^2$  (not  $E^2/m_X^2$ !)

② What if  $m_F \ll m_Z$ ?

- No 3-pt diagram but collider constraints  $\Rightarrow m_F \gtrsim 100$  GeV

③ What about  $\varphi \tilde{F}F$  and  $\varphi \tilde{G}G$  ?

- All interactions are vector-like  $\rightarrow$  no chiral anomaly

# Baryon number vector

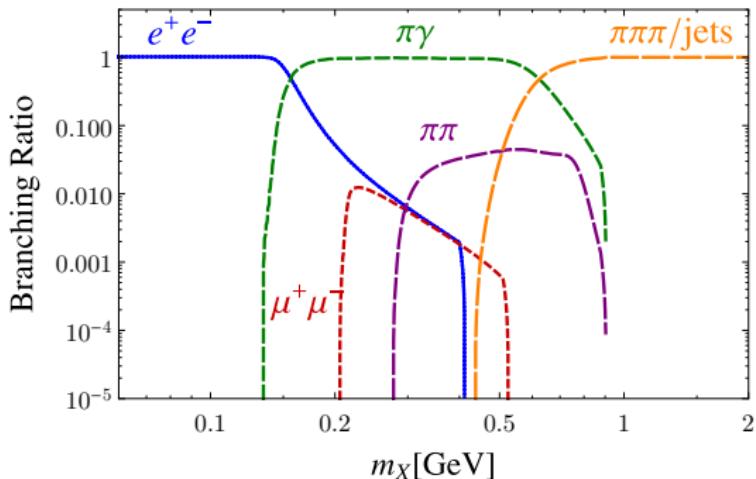


- The  $X$  Lagrangian looks like,

$$\frac{m_X^2}{2} X^2 + \frac{g_X}{3} X^\mu \sum_i \bar{q}_i \gamma_\mu q_i + \frac{3g_X}{32\pi^2} \frac{\varphi}{m_X} (g^2 W^a \tilde{W}^a - g'^2 B \tilde{B})$$

- $X$  can decay:

[1404.4370 - Tulin]

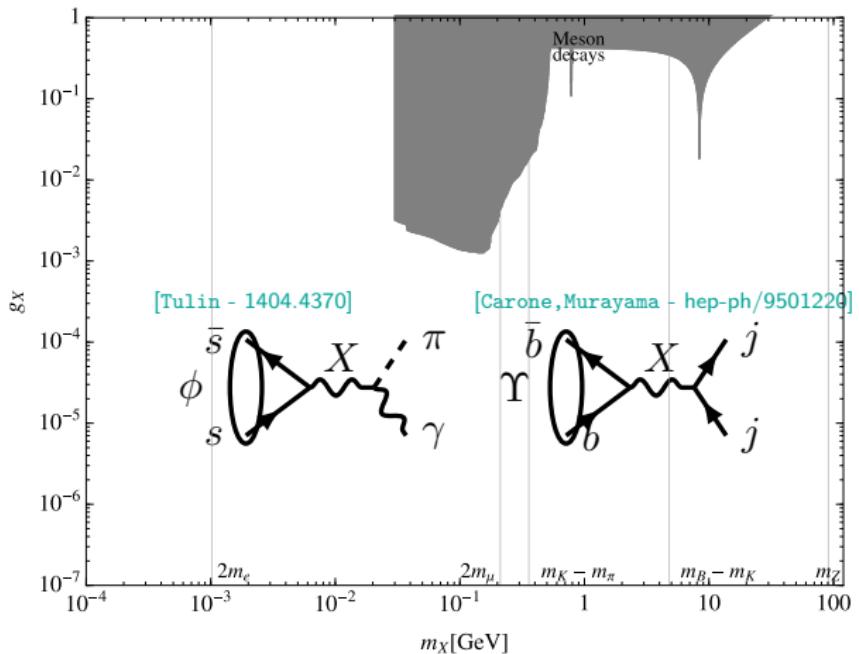


# Constraints

# $B$ vector constraints



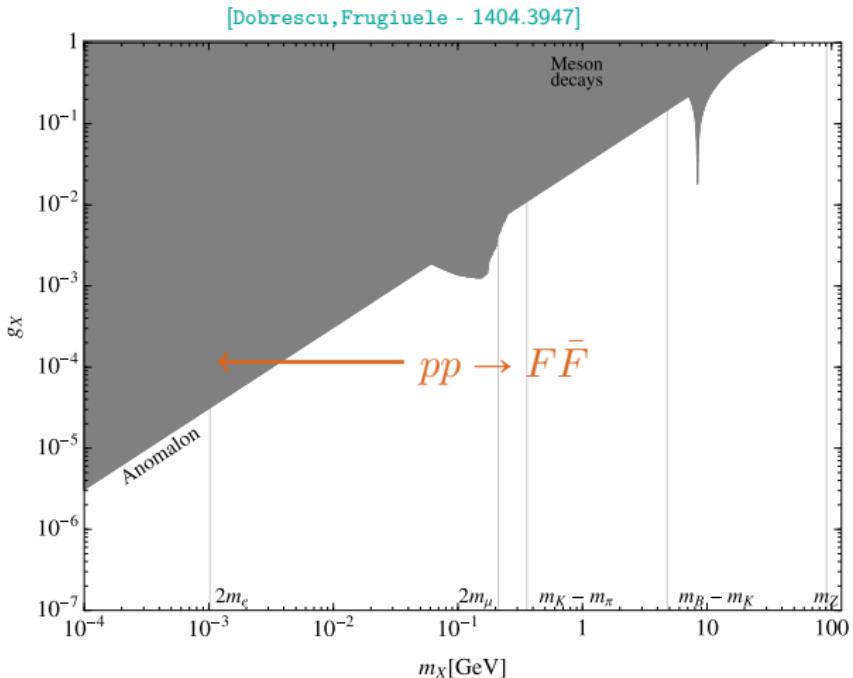
- Non-enhanced limits:



# $B$ vector constraints



- Direct searches for heavy fermions:

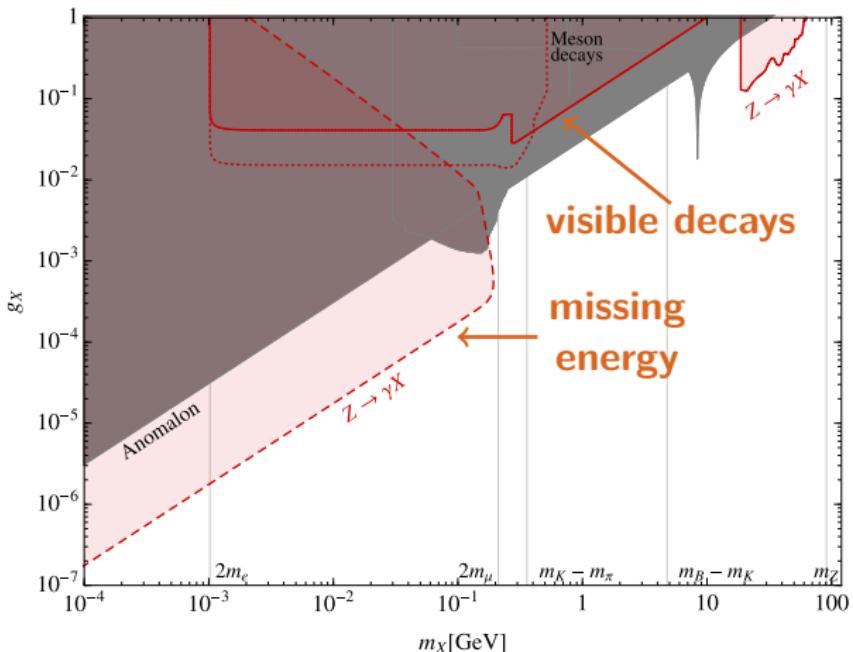


# $B$ vector constraints



- $Z \rightarrow X\gamma$ :

[JD, Pospelov, Lasenby - 1705.06726]

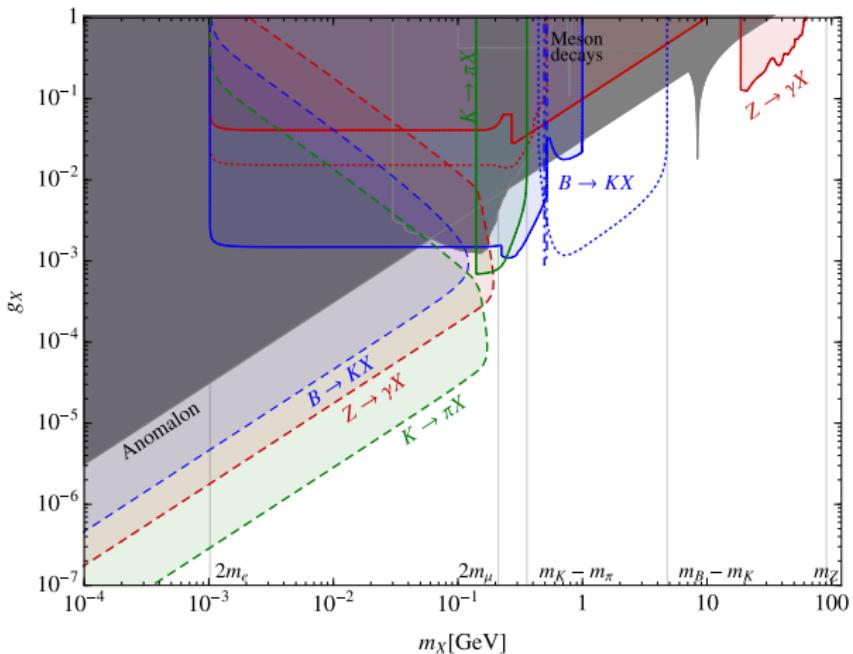


# $B$ vector constraints



- $B \rightarrow KX$  (not just  $K^*$ !),  $K \rightarrow \pi X$  :

[JD,Pospelov,Lasenby - 1705.06726]  
[Recast of - Babar,Belle,LHCb]

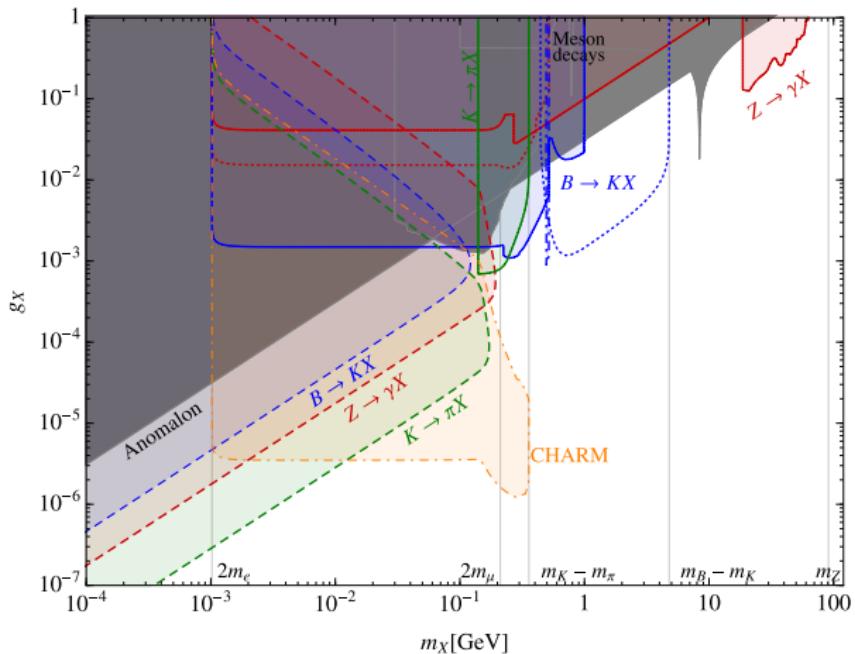


# $B$ vector constraints



- Beam dump:

[JD, Pospelov, Lasenby - 1705.06726]

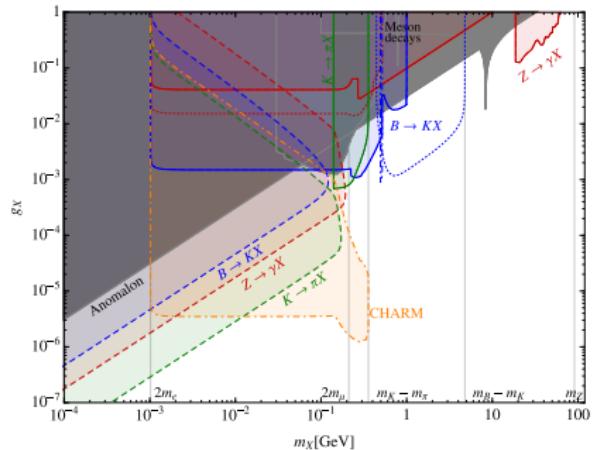


# Limit summary ( $U(1)_B$ )

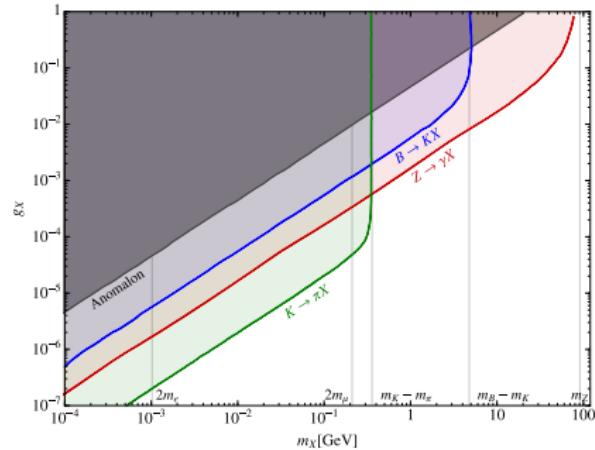


- Summary of all limits
- Significant improvement over old limits (gray)

**$X$  decays to SM**

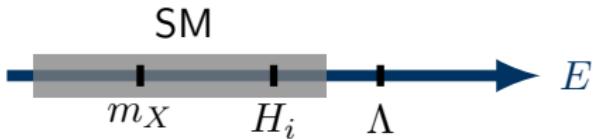


**$X$  decays to dark sector**



# Tree-level breaking

- Amplitudes grow with energy... **even at tree-level**
- Need modification of EW sector



$$\Lambda \lesssim m_X/g_X$$

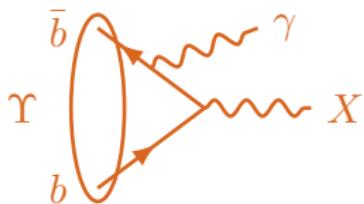
- Below this scale,  $\partial_\mu J_X^\mu \neq 0!$
- For  $E \ll \Lambda$ :

$$\mathcal{M} \propto E/m_X$$

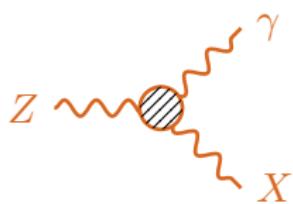
# Axially-coupled vector



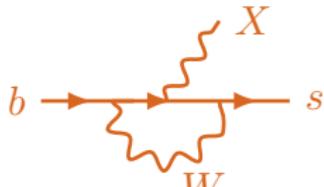
- $X$  can have axial couplings to SM fermions
- $m_f$  are  $\cancel{U(1)_X}$
- Still have  $\cancel{U(1)_X}$ -chiral anomaly (now with  $F\tilde{F}$  and  $G\tilde{G}$ )



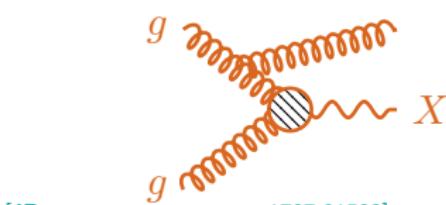
[Fayet - hep-ph/0607318]



[JD, Pospelov, Lasenby - 1705.06726]



[JD, Pospelov, Lasenby - 1707.01503]



[JD, Pospelov, Lasenby - 1707.01503]

# Axially-coupled UV completions



- SM+axial, e.g.,

$$\mathcal{L} \supset H \bar{L}_L e_R + X_\mu \bar{e}_R \gamma^\mu e_R$$

- Not UV complete
- Need to charge Higgs under  $U(1)_X$
- **Benchmark model:  $U(1)_R$**
- Still need heavy fermions to cure anomaly

[1609.02188 - Ismail,Keung,Tsao,Unwin]  
[1609.09072 - Kahn,Krnjaic,Mishra-Sharma,Tait]

# Example: $U(1)_R$ -coupled vector

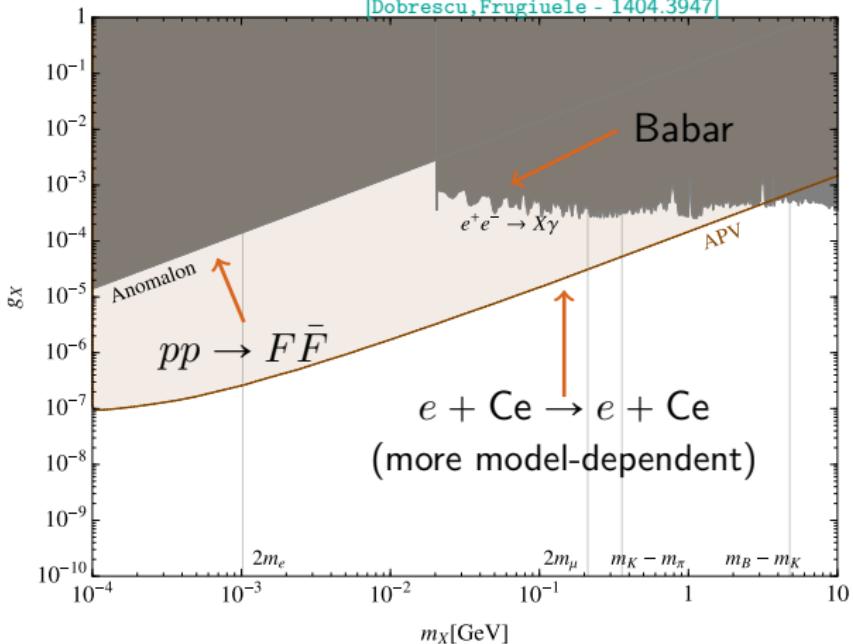


- Non-enhanced limits:

[Fayet - hep-ph/0702176]

[Babar - 1406.2980]

[Dobrescu,Frugueule - 1404.3947]

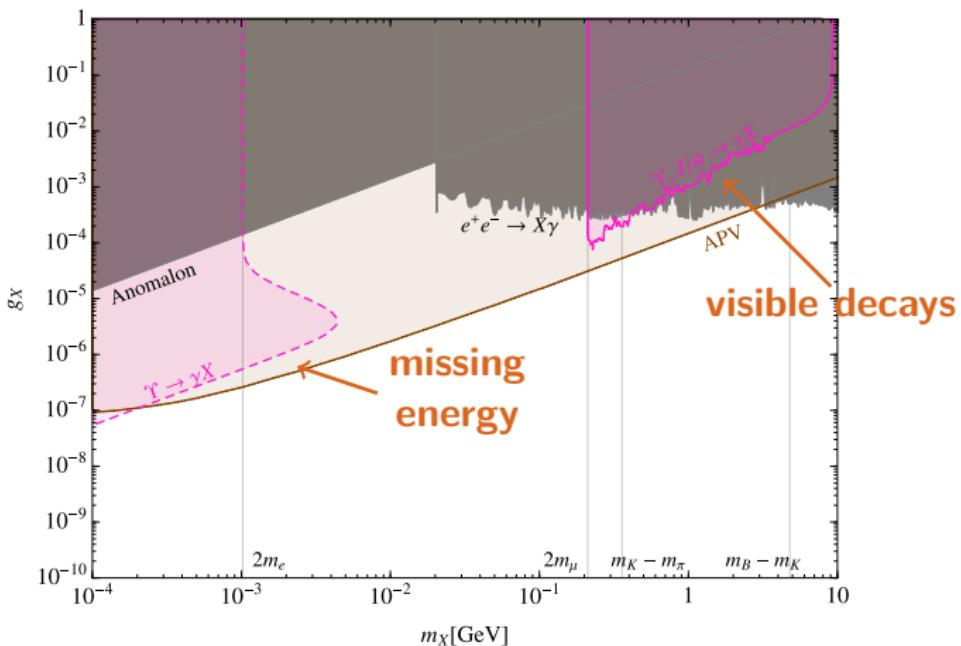


# Example: $U(1)_R$ -coupled vector



○  $\Upsilon \rightarrow X\gamma$ :

[Fayet - hep-ph/0702176]  
[JD, Pospelov, Lasenby - 1707.01503]

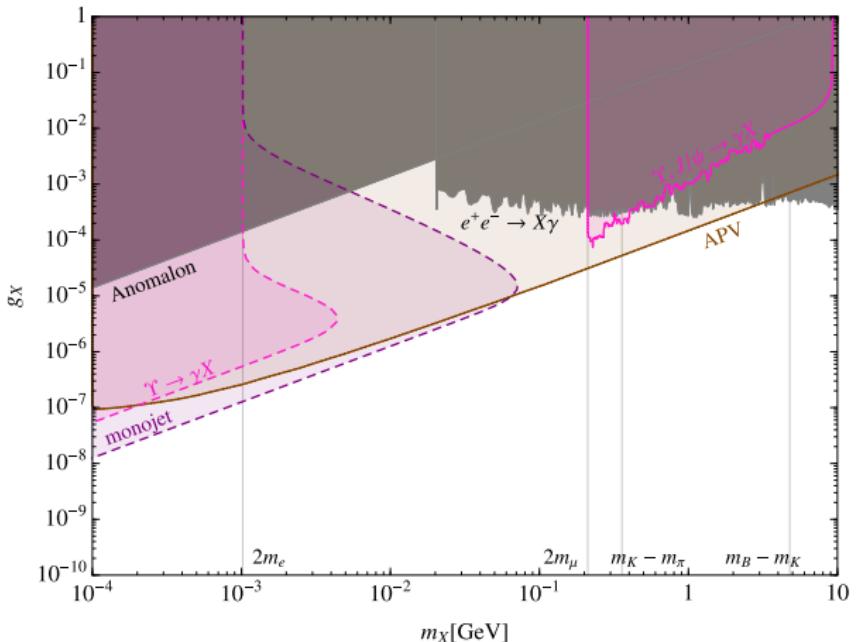


# Example: $U(1)_R$ -coupled vector



- Monojet (using  $\varphi \tilde{G}G$ ):

[JD,Pospelov,Lasenby - 1707.01503]

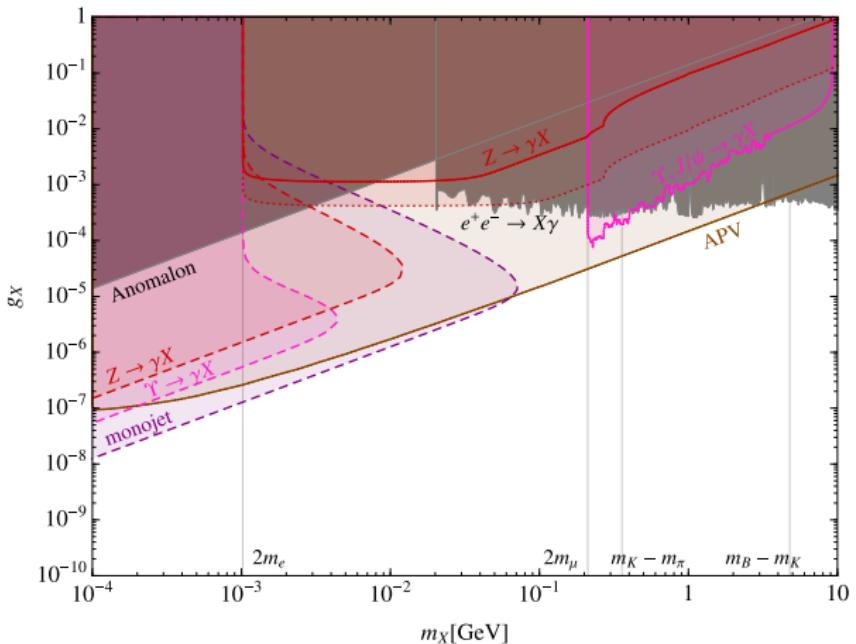


# Example: $U(1)_R$ -coupled vector



○  $Z \rightarrow X\gamma$ :

[JD,Pospelov,Lasenby - 1705.06726]

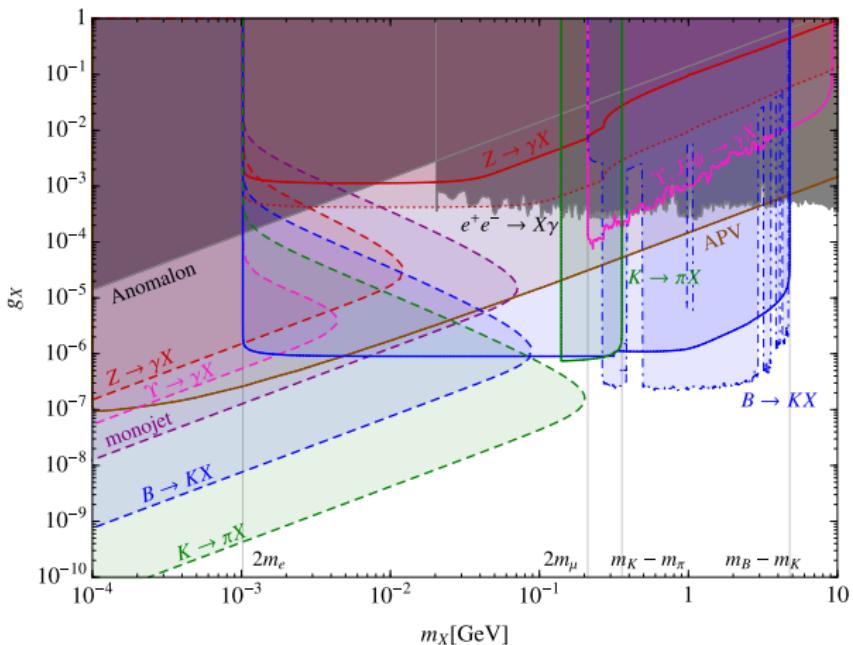


# Example: $U(1)_R$ -coupled vector



- FCNC:

[JD,Pospelov,Lasenby - 1705.06726]

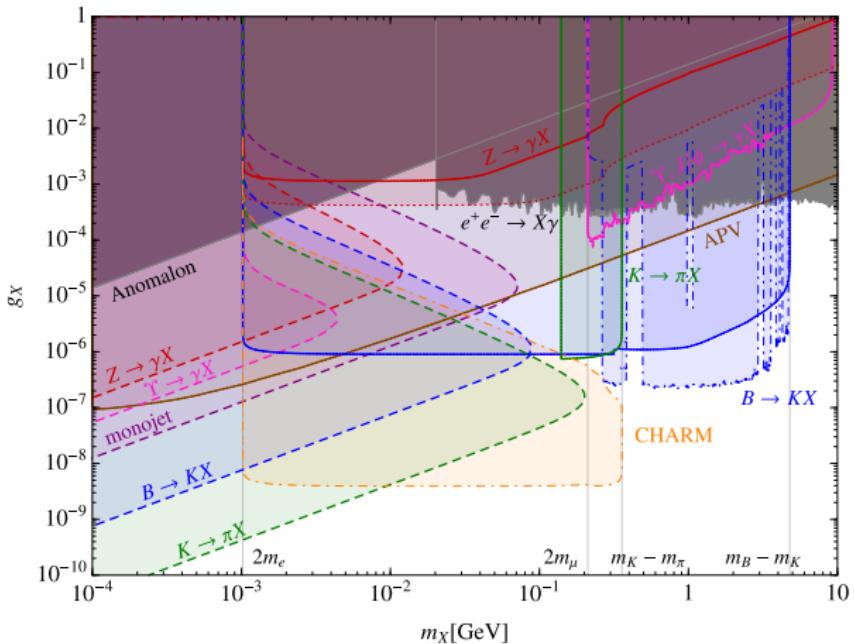


# Example: $U(1)_R$ -coupled vector



- Beam dump:

[JD,Pospelov,Lasenby - 1705.06726]

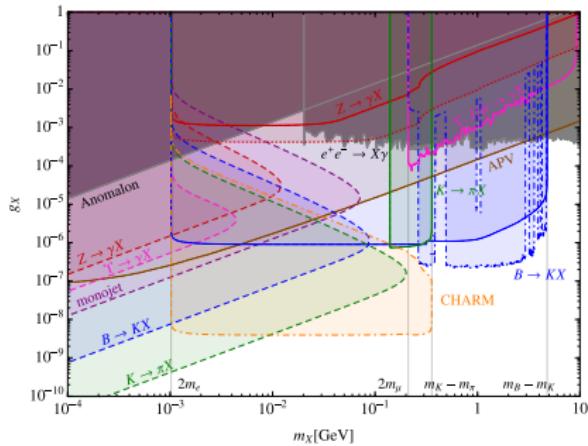


# Limit summary ( $U(1)_R$ )

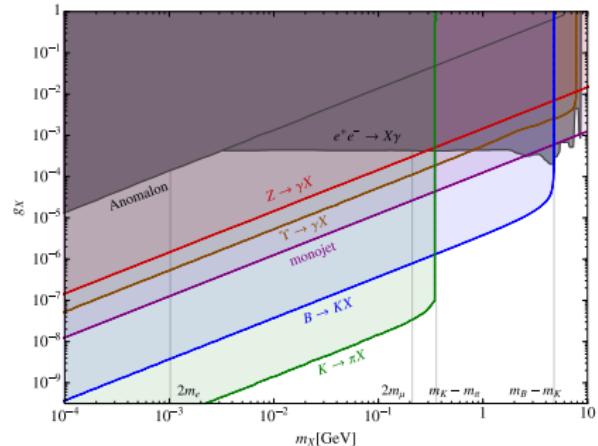


- Summary of all limits
- Significant improvement over old limits (gray)

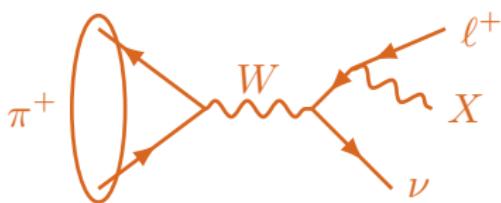
$X$  decays to SM



$X$  decays to dark sector



- Can build models that charged current violates  $U(1)_X$
- Occurs if couple only one particle of  $SU(2)$  doublet to  $X$
- Enhanced processes:



[Karshenboim, McKeen, Pospelov - 1401.6154]

[JD, Pospelov, Lasenby - 1707.01503]

- $\pi^+ \rightarrow e^+ \nu X$  is particularly stringent
- SM rate for  $\pi^+ \rightarrow e^+ \nu (\gamma^* \rightarrow e^+ e^-) \propto m_e^2$  (at tree-level)
- Not the case for  $X$  rate

# EW coupling



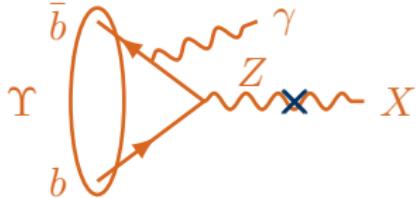
- $X$  could couple to EW sector (other than kinetic mixing)
- Such couplings are not  $U(1)_X$  invariant
- Prominent example: mass-mixing:

$$\mathcal{L} \supset \varepsilon_Z m_Z^2 X_\mu Z^\mu$$

- Typical for generic light vector model
- Enhanced rates,  $\propto \varepsilon_Z$



[JD, Pospelov, Lasenby - 180X,XXXXX]

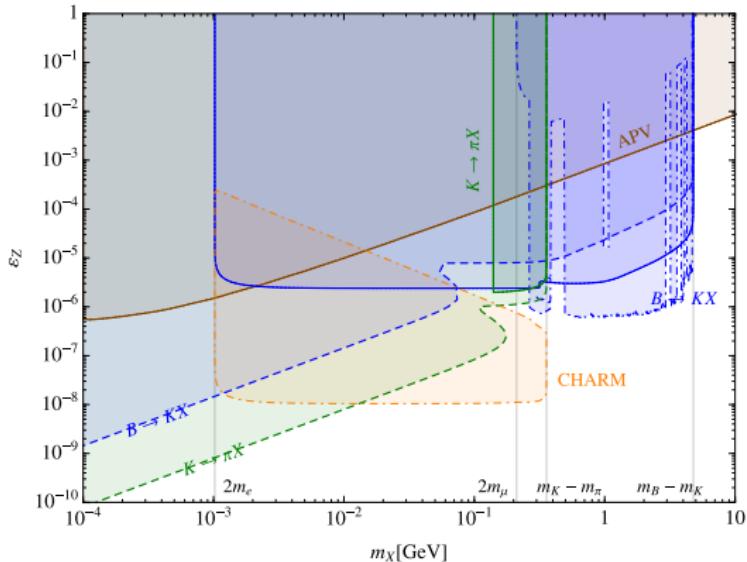


[JD, Pospelov, Lasenby - 1705.06726]

# Mass-mixing

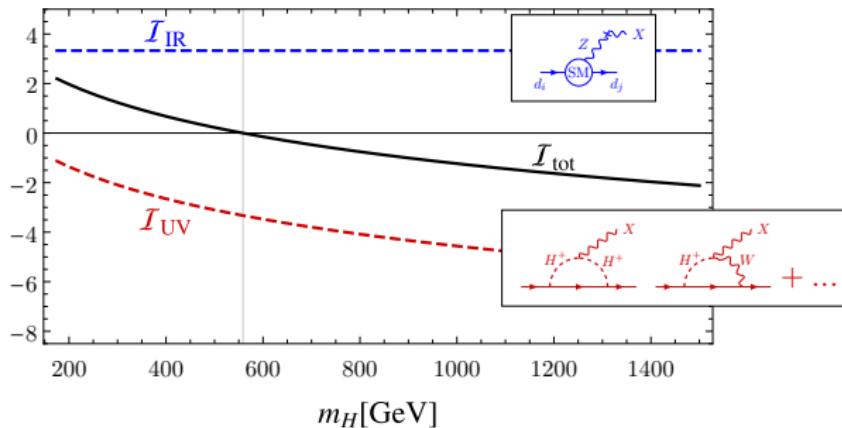


- Constraints on a mass-mixing are tricky
- Mixing is not EW-gauge invariant!
- Leads to log-enhanced FCNCs



- 2HDM for mass-mixing  
[\[1203.2947 - Davoudiasl et al\]](#)
- $m_H \gg m_W \gg m_X$
- standard motivation for APV
- FCNC from IR and UV
- $g_{d_i d_j X} \propto \mathcal{I}_{\text{IR}} + \mathcal{I}_{\text{UV}}$

Particle	SM	$U(1)_X$
$H_1$	✓	✗
$H_2$	✓	✓
$H_d$	✗	✓



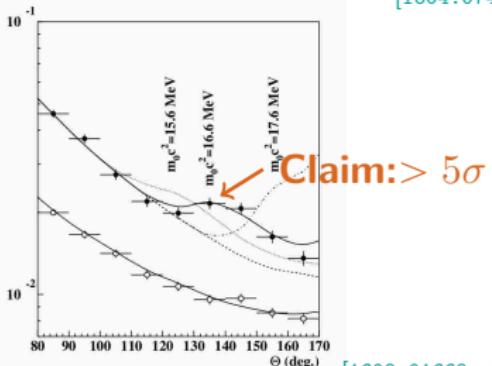
# Applications

# Beryllium anomaly



- Excess in  ${}^8\text{Be}^* \rightarrow \text{Be } e^+ e^-$  in  $m_{ee}$  (or  $\theta_{ee}$ )

[1504.01527 - Krasznahorkay et al]  
[1604.0741 - Feng et al]

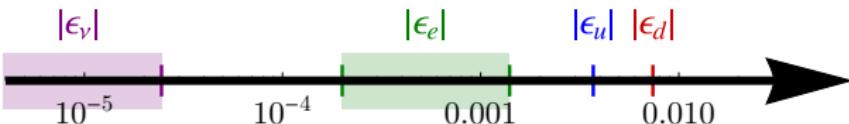


[1609.01669 - Ellwanger, Moretti]

- New physics explanation: vector/pseudoscalar

- Unusual vector:  
[1608.03591 - Feng et al]

$$\mathcal{L} \supset \sum e \epsilon_f \bar{f} \gamma^\mu f X_\mu \quad \text{"anomalies to fix anomalies"}$$



# $^8\text{Be}$ - baryon number model



- Explaining the Beryllium anomaly requires some vector gymnastics
- Requires  $|\epsilon_e| \sim \epsilon_u \simeq -2\epsilon_d$ ,  $\epsilon_\nu \simeq 0$
- Idea: gauge baryon number with introduce kinetic mixing.
  - Sets  $\epsilon_\nu \rightarrow 0!$  [1608.03591 - Feng et al]
  - Can tune  $\epsilon_u$  to cancel  $\epsilon_d$
- But predicts...

$$\text{Br}(K \rightarrow \pi(X \rightarrow \text{inv})) \simeq 10^{-5} \left( \frac{g_X}{10^{-3}} \right)^2 \left( \frac{17 \text{ MeV}}{m_X} \right)^2$$

$$\left[ \text{Limit : Br}(K \rightarrow \pi + \text{inv}) \simeq (2 \pm 1) \times 10^{-10} \right]$$

[E949 - 2008]

- Idea:  $B - L$  without neutrino coupling can explain anomaly  
[1608.03591 - Feng et al]
- Use mass-mixing to eliminate neutrino coupling
- Require  $g_X \sim 10^{-3}$
- Model has weak-isospin violation ( $W\ell\nu$  does not preserve  $\text{U}(1)_X$ )

$$\text{Br}(\pi^+ \rightarrow e^+ \nu(X \rightarrow e^+ e^-)) \simeq 10^{-7} \left( \frac{17 \text{ MeV}}{m_X} \right)^2 \left( \frac{g_X}{10^{-3}} \right)^2$$

$$\left[ \text{Limit : Br}(\pi^+ \rightarrow e^+ \nu e^+ e^-) \simeq \lesssim 3 \times 10^{-9} \right]$$

[SINDRUM Collaboration - 1989]

# ${}^8\text{Be}$ - axially coupled vector



- Idea: axially-coupled vector [1612.01525 - Kozaczuk, Morrissey, Stroberg]
- Changes all the constraints
- Allows for somewhat smaller couplings  $g_X^u \sim g_X^d \sim 10^{-4-5}$
- But...

$$\text{Br}(B \rightarrow K(X \rightarrow e^+ e^-)) \simeq 0.1 \left( \frac{17 \text{MeV}}{m_X} \right)^2 \left( \frac{g_X}{10^{-5}} \right)^2$$

$$\left[ \text{Limit : } \delta \text{Br}(B \rightarrow K e^+ e^-) \lesssim 10^{-7} \right]$$

[BaBar Collaboration - 0807.4119]

# Take home message



- Can gauge non-conserved currents
- Broken at loop level?
  - Dangerous!
- Broken at tree level?
  - More dangerous!
- **Constraints grow with energy!**
- **FCNC's dominate for  $m_X \lesssim m_B$**
- Rule out most  ${}^8\text{Be}$  anomaly models
- Moral:



**careful what you gauge!**