# EFFECTIVE THEORIES OF HIGGS SECTOR VACUUM STATES 

Daniel Egana-Ugrinovic<br>Rutgers University

In collaboration with Scott Thomas

UC Davis
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## A new era of discovery: the Higgs sector

- Possible deviations from the SM Higgs couplings could be found (e.g. Craig, Galloway, Thomas I 305.2424).
* New scalars extending the Higgs sector could be found (e.g. Craig, D'Eramo, Draper, Thomas, Zhang, I 504.04630).
- Flavor physics could provide hints to new scalars, that could be charged (e.g. Crivellin 1412.25 2).
- Which one(s) would be the possible extension(s) of the Higgs sector corresponding to a particular signature?


## EW Precision

- First experimental constraint: EW precision

$$
\rho=\frac{m_{W}^{2}}{m_{Z}^{2} \cos ^{2} \theta_{W}}=1.0008_{-0.0007}^{+0.0017}
$$

Easily achieved only with a vacuum parametrized by $\operatorname{SU}(2)$ singlets and doublets (*)

(* Exceptions: see Gunion,<br>Haber, Kane, Dawson, The<br>Higgs Hunter's Guide, or Georgi,<br>Machacek, Nucl. Phys. B 262,<br>463)

## Alignment

- Second experimental constraint, alignment:

The Higgs seems to couple to SM particles with similar strength than the Higgs condensate (experimental fact) (*)


> (* at least to gauge bosons and 3 rd gen. fermions)

Naturally achieved in the decoupling limit

## The EFT's of the Higgs sector

- These experimental facts are very constraining.
- The aligned $\underline{x S M}$ and $\underline{2 H D M}$ are the simplest UV completions fulfilling these principles.

The objective
Be as general as possible and derive the $\times$ SM and 2HDM EFT (at tree level).

Leave no effect behind.

## Outline

I. The effective theory of the xSM. Democratic dilution of couplings?
2. The 2HDM: an unconventional review. Challenges of the mixing language.
3. The low energy theory of the 2 HDM.
4. Comments. The complex alignment parameter. Examples of applications of the EFT.

## The xSM

## The xSM

- The most general renormalizable potential contains 7 parameters

$$
V=\frac{\mu^{2}}{2} S^{2}+\frac{\zeta}{3} S^{3}+\frac{\lambda_{S}}{8} S^{4}+m^{2} H^{\dagger} H+\frac{\lambda}{2}\left(H^{\dagger} H\right)^{2}+\xi S H^{\dagger} H+\frac{\lambda^{\prime}}{2} S^{2} H^{\dagger} H
$$

without loss of generality, we write no tadpole term

- There are 4 mass scales $\zeta, \xi, \mu, m$. Define the decoupling limit as

$$
\lambda_{i} v^{2} \ll \mu^{2}
$$

* We allow for the remaining mass scales to be as large as $\mu$

$$
\xi, \zeta \leq \mu \quad \text { That is it: this is very general }
$$

## The vacuum states. Fermionic interactions.

B Define the vacuum states

$$
H_{0}=\frac{1}{\sqrt{2}}(v+h) \quad S=v_{s}+s
$$

B And standard fermionic interactions

$$
\begin{gathered}
-\mathcal{L}_{Y}=\lambda_{i j}^{u} Q_{i} H \bar{u}_{j}-\lambda_{i j}^{d} Q_{i} H^{c} \bar{d}_{j}-\lambda_{i j}^{\ell} L_{i} H^{c} \bar{\ell}_{j}+\text { h.c. } \\
\lambda_{i j}^{f}=\frac{\sqrt{2} m_{i j}^{f}}{v}=\frac{\sqrt{2} m_{i}^{f}}{v} \delta_{i j}^{f}
\end{gathered}
$$

## Very short review: the mixing language

- The interaction term $\xi S H^{\dagger} H$ induces mixing. The Higgs mass eigenstate is

$$
\varphi_{1}=h \cos \gamma+s \sin \gamma \quad \cos \gamma=1-\frac{\xi^{2}}{2 \mu^{2}}\left(\frac{v}{\mu}\right)^{2}+\mathcal{O}\left(\frac{v^{4}}{\mu^{4}}\right)
$$

- Couplings of the higgs mass eigenstate are democratically diluted with respect to SM value *

$$
\begin{aligned}
g_{\varphi_{1} V V} & =\frac{2 m_{V}^{2}}{v} \cos \gamma \\
g_{\varphi_{1}^{2} V V} & =\frac{2 m_{V}^{2}}{v^{2}} \cos ^{2} \gamma \\
\lambda_{\varphi_{1} i j}^{f} & =\frac{m_{i}^{f}}{v} \cos \gamma \delta_{i j}
\end{aligned}
$$

* Self couplings are more complicated


## Deriving the $x$ SM EFT

- An example diagram is

- EFT organizes the effects in an expansion in a small parameter.
- To get this expansion right, need to identify the operator's effective dimension.

> In the $x S M$
> Effective dimension $=$ Operator dimension

## The xSM EFT

- Up to operator dimension six:

$$
D_{\mu} H^{\dagger} D^{\mu} H+\frac{1}{2} \zeta_{H} \partial_{\mu}\left(H^{\dagger} H\right) \partial^{\mu}\left(H^{\dagger} H\right)-V^{\prime}(H)
$$

- By any means not the most general EFT you could write.
- Most coefficients (but not all) controlled exclusively by one parameter: $\square$


## The analogue of mixing in EFT terms

- Let us expand the kinetic operator

$$
\partial_{\mu}\left(H^{\dagger} H\right) \partial^{\mu}\left(H^{\dagger} H\right)=v^{2} \partial_{\mu} h \partial^{\mu} h+2 v h \partial_{\mu} h \partial^{\mu} h+h^{2} \partial_{\mu} h \partial^{\mu} h
$$

„ "Mixing" is encoded in WF renormalization.

## Mixing <br>  <br> WF renormalization

- The remaining two operators can be replaced in favor of operators with no derivatives using e.o.m., and they lead to additional modifications of the Higgs couplings.


## Fermionic and Gauge Couplings

- All couplings are modified at the same operator dimension.

$$
\begin{aligned}
& \lambda_{\varphi i j}^{f}=\frac{m_{i}^{f}}{v}\left[1-\sqrt{\frac{\xi^{2}}{2 \mu^{2}} \frac{v^{2}}{\mu^{2}}}+\mathcal{O}\left(\frac{v^{4}}{\mu^{4}}\right)\right] \delta_{i j} \\
& \frac{g_{\varphi^{3}}}{v}=-\frac{3 m_{\varphi}^{2}}{v^{2}}+\left(\frac{9 \lambda \xi^{2}}{2 \mu^{2}}-\frac{3 \lambda^{\prime} \xi^{2}}{\mu^{2}}-\frac{9 \xi^{4}}{2 \mu^{4}}+\frac{2 \zeta \xi^{3}}{\mu^{4}}\right) \frac{v^{2}}{\mu^{2}} \\
& g_{\varphi V V}=\frac{2 m_{V}^{2}}{v}\left[1-\mathcal{O}\left(\frac{v^{4}}{\mu^{4}}\right)\right. \\
& g_{\varphi^{2} V V}=\frac{2 m_{V}^{2}}{v^{2}}\left[1-2 \frac{v^{2}}{\mu^{2}}\right. \\
& \frac{\xi^{2}}{\mu^{2}} \frac{v^{2}}{\mu^{2}} \\
&\left.\mathcal{O}\left(\frac{v^{4}}{\mu^{4}}\right)\right] \\
&
\end{aligned}
$$

The last coupling is not just dilution!

## Four linear couplings do not match

- Amplitudes match, couplings do not necessarily match. Consider the short distance piece of the amplitude.
(Short distance only)
$g_{\varphi \varphi V V}^{E F T}=g_{\varphi_{1} \varphi_{1} V V}^{\text {Mixing }} \quad+$

- This diagram cannot be neglected: it leads to effects of order $v^{2} / \mu^{2}$


## Trilinear couplings must match

* This ensures the equality of the long distance pieces of the amplitudes.
(Long distance only)

- Long distance pieces of amplitudes are controlled by trilinear couplings.

> Trilinear couplings in the mixing and EFT languages always match.

## The 2HDM: an unconventional review

## The Most General 2HDM

- It is a theory of two identical doublets with a condensate specified by

$$
\begin{gathered}
\frac{v_{1}^{2}}{2}=\left\langle\Phi_{1}^{\dagger} \Phi_{1}\right\rangle \quad \frac{v_{2}^{2}}{2}=\left\langle\Phi_{2}^{\dagger} \Phi_{2}\right\rangle \\
\xi=\operatorname{Arg}\left\langle\Phi_{1}^{\dagger} \Phi_{2}\right\rangle
\end{gathered}
$$

- As such

$$
\tan \beta=\frac{v_{1}}{v_{2}} \quad \begin{gathered}
\text { does not have physical } \\
\begin{array}{c}
\text { meaning at this point } \\
\text { (see for instance Haber, } \\
\text { O'Neil, 0602242) }
\end{array}
\end{gathered}
$$

## The Higgs Basis

- We can always perform a rotation

$$
\begin{array}{r}
e^{-i \xi / 2} H_{1}=\cos \beta \Phi_{1}+\sin \beta e^{-i \xi} \Phi_{2} \\
H_{2}=-\sin \beta e^{i \xi} \Phi_{1}+\cos \beta \Phi_{2} \\
\frac{v^{2}}{2}=\left\langle H_{1}^{\dagger} H_{1}\right\rangle \quad 0=\left\langle H_{2}^{\dagger} H_{2}\right\rangle
\end{array}
$$

- This is the Higgs basis (e.g. Davidson, Haber 0504050). Useful in the alignment limit, so we work in this basis.



## The potential in the Higgs basis

- The most general renormalizable potential in the Higgs basis is

$$
\begin{array}{r}
V\left(H_{1}, H_{2}\right)=\tilde{m}_{1}^{2} H_{1}^{\dagger} H_{1}+\tilde{m}_{2}^{2} H_{2}^{\dagger} H_{2}+\left(\tilde{m}_{12}^{2} H_{1}^{\dagger} H_{2}+\text { h.c. }\right) \\
+\frac{1}{2} \tilde{\lambda}_{1}\left(H_{1}^{\dagger} H_{1}\right)^{2}+\frac{1}{2} \tilde{\lambda}_{2}\left(H_{2}^{\dagger} H_{2}\right)^{2}+\tilde{\lambda}_{3}\left(H_{2}^{\dagger} H_{2}\right)\left(H_{1}^{\dagger} H_{1}\right)+\tilde{\lambda}_{4}\left(H_{2}^{\dagger} H_{1}\right)\left(H_{1}^{\dagger} H_{2}\right) \\
+\left[\frac{1}{2} \tilde{\lambda}_{5}\left(H_{1}^{\dagger} H_{2}\right)^{2}+\tilde{\lambda}_{6} H_{1}^{\dagger} H_{1} H_{1}^{\dagger} H_{2}+\tilde{\lambda}_{7}\left(H_{2}^{\dagger} H_{2}\right)\left(H_{1}^{\dagger} H_{2}\right)+\text { h.c. }\right]
\end{array}
$$

- The EWSB conditions are

$$
\begin{gathered}
v^{2}=-2 \frac{\tilde{m}_{1}^{2}}{\tilde{\lambda}_{1}} \\
\tilde{m}_{12}^{2}=-\frac{1}{2} \tilde{\lambda}_{6} v^{2} \\
\hline
\end{gathered}
$$

No-tadpole condition

- The only limitation we will impose, is that we work in the decouplings limit $\tilde{\lambda}_{i} v^{2} \ll \tilde{m}_{2}^{2}$


## The observables in the Higgs potential

- The potential contains a $U(I)$ background symmetry


B There are II invariants under the background symmetry in the potential: I | physical observables (examples: $\tilde{\lambda}_{2}, \tilde{\lambda}_{6}^{*} \tilde{\lambda}_{6}, v$ )

* The background symmetry is unbroken by the Higgs vev.


## The Yukawas. CP violation.

- The most general Yukawas are

$$
\left[\begin{array}{c}
\left.\tilde{\lambda}_{a i j}^{u} Q_{i} H_{a} \bar{u}_{j}-\tilde{\lambda}_{a i j}^{d \dagger} Q_{i} H_{a}^{c} \bar{d}_{j}-\tilde{\lambda}_{a i j}^{\ell \dagger} L_{i} H_{a}^{c} \bar{\ell}_{j}+\text { h.c. }\right] \\
\tilde{\lambda}_{1 i j}^{f}=\frac{\sqrt{2} m_{i j}^{f}}{v}
\end{array}\right.
$$

* The physical CP violating phases are

$$
\begin{gathered}
\theta_{1}=\operatorname{Arg}\left(\tilde{\lambda}_{6}^{2} \tilde{\lambda}_{5}^{*}\right) \\
\theta_{2}=\operatorname{Arg}\left(\tilde{\lambda}_{7}^{2} \tilde{\lambda}_{5}^{*}\right) \\
\operatorname{Arg}\left(\tilde{\lambda}_{6}^{*} \tilde{\lambda}_{2 i j}^{f}\right)
\end{gathered}
$$

CP violation
in the potential
CP violation in the potential or Yukawas

## Review of the mixing language

- Normally you would write the mass matrix and diagonalize it.

$$
\mathcal{M}^{2}=\left(\begin{array}{ccc}
\tilde{\lambda}_{1} v^{2} & \left|\tilde{\lambda}_{6}\right| \cos \left(\theta_{1} / 2\right) v^{2} & -\left|\tilde{\lambda}_{6}\right| \sin \left(\theta_{1} / 2\right) v^{2} \\
\left|\tilde{\lambda}_{6}\right| \cos \left(\theta_{1} / 2\right) v^{2} & \tilde{m}_{2}^{2}+\frac{1}{2} v^{2}\left(\tilde{\lambda}_{3}+\tilde{\lambda}_{4}+\left|\tilde{\lambda}_{5}\right|\right) & 0 \\
-\left|\tilde{\lambda}_{6}\right| \sin \left(\theta_{1} / 2\right) v^{2} & 0 & \tilde{m}_{2}^{2}+\frac{1}{2} v^{2}\left(\tilde{\lambda}_{3}+\tilde{\lambda}_{4}-\left|\tilde{\lambda}_{5}\right|\right)
\end{array}\right)
$$

- In the CP violating case this leads to cumbersome expressions for the couplings (e.g. Haber, O'Neil 0602242 v ). Can this be improved?
- Moreover, in the singlet case couplings in the mixing and EFT language did not match.


## The 2HDM and the power of EFT

## Deriving the EFT: effective dimension

- Examples:

$\lambda_{6}^{*} \lambda_{6}\left(H^{\dagger} H\right)^{3}$

$\left(\tilde{m}_{12}^{2}\right)^{*} \lambda_{6}\left(H^{\dagger} H\right)^{2}$
$\sim v^{2}$ No tadpole condition


## In the 2HDM <br> Effective dimension $\neq$ Operator dimension

$$
E D=4-n_{\tilde{m}_{2}^{2}}
$$

## The low energy theory of the 2HDM

- This is just to show you how does the EFT look.

$$
\begin{aligned}
& Z_{H} D_{\mu} H^{\dagger} D^{\mu} H+\zeta_{H}\left[\frac{1}{2} \partial_{\mu}\left(H^{\dagger} H\right) \partial^{\mu}\left(H^{\dagger} H\right)+H^{\dagger} H D_{\mu} H^{\dagger} D^{\mu} H\right] \\
+ & \zeta_{H}^{\prime}\left[2 H^{\dagger} H \partial_{\mu}\left(H^{\dagger} H\right) \partial^{\mu}\left(H^{\dagger} H\right)+\left(H^{\dagger} H\right)^{2} D_{\mu} H^{\dagger} D^{\mu} H\right]-V(H) \\
- & {\left[Q_{i} H\left(\lambda_{i j}^{u}+\eta_{i j}^{u} H^{\dagger} H\right) \bar{u}_{j}-Q_{i} H^{c}\left(\lambda_{i j}^{d \dagger}+\eta_{i j}^{d \dagger} H^{\dagger} H\right) \bar{d}_{j}\right.} \\
- & \left.L_{i} H^{c}\left(\lambda_{i j}^{\ell \dagger}+\eta_{i j}^{\ell \dagger} H^{\dagger} H\right) \bar{\ell}_{j}+\text { h.c. }\right]
\end{aligned}
$$

... plus many four fermion operators

$$
\begin{aligned}
& \Omega_{i j m n}^{u u(0)}\left(Q_{i} \bar{u}_{j}\right)\left(\bar{u}_{m}^{\dagger} Q_{n}^{\dagger}\right)+\Omega_{i j m n}^{d d(0)}\left(Q_{i} \bar{d}_{j}\right)\left(\bar{d}_{m}^{\dagger} Q_{n}^{\dagger}\right)+\Omega_{i j m n}^{\ell \ell(0)}\left(L_{i} \bar{\ell}_{j}\right)\left(\bar{\ell}_{m}^{\dagger} L_{n}^{\dagger}\right) \\
+ & {\left[\Omega_{i j m n}^{d \ell(0)}\left(Q_{i} \bar{d}_{j}\right)\left(\bar{\ell}_{m}^{\dagger} L_{n}^{\dagger}\right)+\Omega_{i j m n}^{u(2(2)}\left(Q_{i} \bar{u}_{j}\right)\left(Q_{m} \bar{d}_{n}\right)+\Omega_{i j m n}^{u \ell(2)}\left(Q_{i} \bar{u}_{j}\right)\left(L_{m} \bar{\ell}_{n}\right)+\text { h.c. }\right] }
\end{aligned}
$$

## The 2HDM EFT: Higgs and fermions

- The Higgs-fermion sector contains

$$
\left[\lambda_{i j}^{u} Q_{i} H \bar{u}_{j}+\eta_{i j}^{u} Q_{i} H H^{\dagger} H \bar{u}_{j}+\cdots+\text { h.c. }\right]
$$

Effective dimension six

$$
\lambda_{\varphi \varphi i j}^{f}=\frac{m_{i}^{f}}{v} \delta_{i j}-2\left(\frac{\tilde{\lambda}_{i 2 i}^{f} \tilde{j}_{6}^{\tilde{*}}}{2 \sqrt{2}}\right)\left(\frac{v^{2}}{\tilde{m}_{2}^{2}}\right)+\mathcal{O}\left(\frac{v^{4}}{\tilde{m}_{2}^{4}}\right)
$$

- Controlled by the heavy doublet Yukawa and $\tilde{\lambda}_{6}^{*}$
- Source of flavor violating processes ( $\Delta F=1$ only)
- CP violation directly measurable in EDM's


## The 2HDM EFT: fermions

- The fermionic sector contains
$\frac{\tilde{\lambda}_{2 i j}^{u} \tilde{\lambda}_{2 m n}^{u \dagger}}{\tilde{m}_{2}^{2}}\left(Q_{i} \bar{u}_{j}\right)\left(\bar{u}_{m}^{\dagger} Q_{n}^{\dagger}\right)+\cdots \quad$ Effective dimension six
$\uparrow$
- Controlled by the heavy doublet Yukawa.
- Source of CP and flavor violation ( $\Delta F=1 \& \Delta F=2$ )


## The 2HDM EFT: Higgs and gauge bosons

* The gauge-kinetic sector contains

$$
\frac{\tilde{\lambda}_{6}^{*} \tilde{\lambda}_{6}}{\tilde{m}_{2}^{4}}\left(H^{\dagger} H\right)^{2} D_{\mu} H^{\dagger} D^{\mu} H+\ldots \text { All operators show up first } \text { at effective dimension eight }
$$

$\uparrow$
Controlled again by $\tilde{\lambda}_{6} \ldots$ !

$$
g_{\varphi^{2} V V}=\frac{2 m_{V}^{2}}{v^{2}}\left[1-3 \tilde{\lambda}_{6}^{*} \tilde{\lambda}_{6} \overline{\frac{v^{4}}{\tilde{m}_{2}^{4}}}+\mathcal{O}\left(\frac{v^{6}}{\tilde{m}_{2}^{6}}\right)\right]
$$

## The 2HDM EFT: self couplings

* The Higgs potential contains

$$
\begin{gathered}
m_{H}^{2} H^{\dagger} H+\frac{1}{2} \lambda_{H}\left(H^{\dagger} H\right)^{2}-\frac{\tilde{\lambda}_{6}^{*} \tilde{\lambda}_{6}}{\tilde{m}_{2}^{2}}\left(H^{\dagger} H\right)^{3}+\ldots \text { Effective dimension six } \\
\text { Controlled by } \tilde{\lambda}_{6}
\end{gathered}
$$

$$
g_{\varphi_{1}^{4}}=-\frac{3 m_{\varphi_{1}}^{2}}{v^{2}}+36 \tilde{\lambda}_{6}^{*} \tilde{\lambda}_{6} \sqrt[\frac{v^{2}}{\tilde{m}_{2}^{2}}]{\square}+\mathcal{O}\left(\frac{v^{4}}{\tilde{m}_{2}^{4}}\right)
$$

## Comparing the different couplings

- Fermionic and gauge couplings are modified at different effective dimension.

$$
\begin{aligned}
\lambda_{\varphi i j}^{f} & \frac{m_{i}^{f}}{v} \delta_{i j}-2\left(\frac{\tilde{\lambda}_{2 i j}^{f} \tilde{\lambda}_{6}^{*}}{2 \sqrt{2}}\right)\left(\frac{v^{2}}{\tilde{m}_{2}^{2}}\right)+\mathcal{O}\left(\frac{v^{4}}{\tilde{m}_{2}^{4}}\right) \\
g_{\varphi_{1} V V} & =\frac{2 m_{V}^{2}}{v}\left[1-\frac{1}{2} \tilde{\lambda}_{6}^{*} \tilde{\lambda}_{6} \frac{v^{4}}{\tilde{m}_{2}^{4}}+\mathcal{O}\left(\frac{v^{6}}{\tilde{m}_{2}^{6}}\right)\right] \\
g_{\varphi^{2} V V} & =\frac{2 m_{V}^{2}}{v^{2}}\left[1-3 \tilde{\lambda}_{6}^{*} \tilde{\lambda}_{6} \frac{v^{4}}{\tilde{m}_{2}^{4}}+\mathcal{O}\left(\frac{v^{6}}{\tilde{m}_{2}^{6}}\right)\right] \\
g_{\varphi_{1}^{4}} & =-\frac{3 m_{\varphi_{1}}^{2}}{v^{2}}+36 \tilde{\lambda}_{6}^{*} \tilde{\lambda}_{6} \frac{v^{2}}{\tilde{m}_{2}^{2}}+\mathcal{O}\left(\frac{v^{4}}{\tilde{m}_{2}^{4}}\right)
\end{aligned}
$$

Very different
from the mixing result

# Interesting facts, an example application and a scorecard for LHC and flavor 

## CP violation

b We found CP violation at ED 6 in higgs-fermion interactions.

- What about the bosonic CP violating phases $\theta_{1} \& \theta_{2}$ ??

$$
\begin{aligned}
& \theta_{1}=\operatorname{Arg}\left(\tilde{\lambda}_{6}^{2} \tilde{\lambda}_{5}^{*}\right) \\
& \theta_{2}=\operatorname{Arg}\left(\tilde{\lambda}_{7}^{2} \tilde{\lambda}_{5}^{*}\right)
\end{aligned}
$$

The CP violation associated with this phases does not appear at ED 6.
All CP violation in Higgs-fermion interactions!

## The complex alignment parameter

- What is this $\tilde{\lambda}_{6}^{*}$ controlling the deviations from the SM couplings?

It is related to a complex alignment parameter $\overline{\text {. }}$


- It is a physical quantity (it is measurable)
- No need to diagonalize the mass matrix!
$\Xi=-\left|\tilde{\lambda}_{6}\right| e^{-i \theta_{1} / 2} \frac{v^{2}}{\tilde{m}_{2}^{2}}+\mathcal{O}\left(\frac{v^{4}}{\tilde{m}_{2}^{4}}\right)$
Example of use: $\quad g_{\varphi_{1} H^{ \pm} W}=-\frac{i m_{W}}{v} \Xi$


## How to detect a perfectly aligned 2HDM

* If all couplings are measured to be SM like, can we get hints of the 2HDM in low energy data?

$$
\frac{\tilde{\lambda}_{2 i j}^{u} \tilde{\lambda}_{2 m n}^{u \dagger}}{\tilde{m}_{2}^{2}}\left(Q_{i} \bar{u}_{j}\right)\left(\bar{u}_{m}^{\dagger} Q_{n}^{\dagger}\right)+\cdots
$$

There will still be hope to find hints of a second doublet in flavor experiments. This is a large effect: ED 6, couplings can be order one.

## Where is $\tan \beta$ ?

- If you work with a general 2HDM you should not make any reference to $\tan \beta$. It artificially extends your parameter space.
- Where is $\tan \beta$ ? It is a direction singled out by particular models:
- In the MSSM: direction relative to the flat direction $\mathrm{Hu}=\mathrm{Hd}$.
- In type I, II, III, IV 2HDM: direction relative to the coupled doublet.


## What is so special about types I-IV?

b Just that the Yukawas of the heavy doublets are proportional to the mass matrix. Example: type I

$$
\tilde{\lambda}_{2 i j}^{u, d, \ell}=\sqrt{2} e^{-\frac{i \xi}{2}} \cot \beta \frac{m_{i j}^{u, d, \ell}}{v}
$$

Type I

$$
\lambda_{\varphi i j}^{u, d, \ell}=\frac{m_{i j}^{u, d, \ell}}{v}\left[1-\tilde{\lambda}_{6}^{*} e^{-i \xi / 2} \cot \beta \frac{v^{2}}{\tilde{m}_{2}^{2}}+\mathcal{O}\left(\frac{v^{4}}{\tilde{m}_{2}^{4}}\right)\right]
$$

Unique CP violating phase in the low energy theory at ED 6.

## Four fermion operators in types I-IV

The CP violating phase does not show up on four fermion operators. Consider as an example

$$
\begin{gathered}
\tilde{\Omega}_{i j m n}^{u u(0)}\left(u_{i} \bar{u}_{j}\right)\left(\bar{u}_{m}^{\dagger} u_{n}^{\dagger}\right) \quad, \quad \tilde{\Omega}_{i j m n}^{u u \pm(0)}\left(d_{i} \bar{u}_{j}\right)\left(\bar{u}_{m}^{\dagger} d_{n}^{\dagger}\right) \\
\tilde{\Omega}_{i j m n}^{u u(0)}=2 \frac{1}{\tilde{m}_{2}^{2}} \delta_{i j} \delta_{m n} \frac{m_{i}^{u} m_{m}^{u *}}{v^{2}} \cot ^{2} \beta \\
\tilde{\Omega}_{i j m n}^{u u \pm(0)}=2 \frac{1}{\tilde{m}_{2}^{2}} \frac{V_{i j}^{T} m_{j}^{u} m_{m}^{u *} V_{m n}^{*}}{v^{2}} \cot ^{2} \beta
\end{gathered}
$$

## An example application: EDM's and the 2HDM

- The electron dipole moment is strongly constrained from experiment

$$
d_{e} \lesssim 10^{-29} \mathrm{e} \mathrm{~cm} \quad \text { ACME, } 13 \mid 0.7534 \text { atom-ph }
$$

B All the contributions at effective dimension six come from Barrzee diagrams



## EDM's in types I-IV

- Places bound on the unique CP violating phase at ED six.

$$
\sin \theta=\frac{v^{2}}{\tilde{m}_{2}^{2}}\left|\tilde{\lambda}_{6}\right| \sin \left[\operatorname{Arg}\left(\tilde{\lambda}_{6}^{*} e^{-i \xi / 2}\right)\right]\left[1+\mathcal{O}\left(\frac{v^{2}}{\tilde{m}_{2}^{2}}\right)\right]
$$

- Examples (numbers are estimates, work in progress):

$$
\begin{array}{ll}
d_{e} \approx 10^{-28} \sin \theta \cot \beta & \text { e cm }
\end{array} \begin{aligned}
& \text { Types I, IV } \\
& d_{e} \approx 10^{-26} \sin \theta \tan \beta \text { e cm }
\end{aligned} \begin{array}{r}
\text { Types II, III } \\
\text { at large } \tan \beta
\end{array}
$$

## A scorecard for LHC and flavor experiments

## The effective theories of the vacuum

|  | The $\times S M$ | The 2HDM |
| :---: | :---: | :---: |
| Change in fermionic couplings | ED 6 and always smaller than SM | ED 6 |
| Change in couplings to gauge bosons | ED 6 and always smaller than SM | ED 8 and always smaller than SM |
| Change in self couplings | ED 6 | ED 6 and always smaller than SM |
| $\qquad$ <br> Changes parametrized mostly by (*) (correlations!) | A single real number | The complex alignment parameter and a complex matrix $\tilde{\lambda}_{2 i j}^{f}$ |
| Flavor violation | $X$ | $\Delta F=1, \Delta F=2$ <br> chirality violating \& chirality preserving |
| CP violation | $X$ | ED 6 and only in fermionic interactions |

(* Higgs self couplings are controlled by a larger set of the UV completion parameters)

## Effective dimensions at LHC

- The plot below is an exclusion plot for the alignment parameter in type I 2HDM. Large exclusion: ED 6 effect. Poor exclusion: only ED 8 in action.

Craig, Galloway, Thomas I305.2424


## A scorecard for LHC and flavor experiments

## The effective theories of the vacuum

|  | The $\times S M$ | The 2HDM |
| :---: | :---: | :---: |
| Change in fermionic couplings | ED 6 and always smaller than SM | ED 6 |
| Change in couplings to gauge bosons | ED 6 and always smaller than SM | ED 8 and always smaller than SM |
| Change in self couplings | ED 6 | ED 6 and always smaller than SM |
| Changes parametrized mostly by ( ${ }^{*}$ ) (correlations!) | A single real number | The complex alignment parameter and a complex matrix $\tilde{\lambda}_{2 i j}^{f}$ |
| Flavor violation | $X$ | $\Delta F=1, \Delta F=2$ <br> chirality violating \& chirality preserving |
| CP violation | $X$ | ED 6 and only in fermionic interactions |

(* Higgs self couplings are controlled by a larger set of the UV completion parameters)

## Backup: four fermion operators

- From integrating out the heavy Higgs

$$
\begin{aligned}
& \quad \Omega_{i j m n}^{u u(0)}\left(Q_{i} \bar{u}_{j}\right)\left(\bar{u}_{m}^{\dagger} Q_{n}^{\dagger}\right)+\Omega_{i j m n}^{d d(0)}\left(Q_{i} \bar{d}_{j}\right)\left(\bar{d}_{m}^{\dagger} Q_{n}^{\dagger}\right)+\Omega_{i j m n}^{\ell \ell(0)}\left(L_{i} \bar{\ell}_{j}\right)\left(\bar{\ell}_{m}^{\dagger} L_{n}^{\dagger}\right) \\
& +\left[\Omega_{i j m n}^{d \ell(0)}\left(Q_{i} \bar{d}_{j}\right)\left(\bar{\ell}_{m}^{\dagger} L_{n}^{\dagger}\right)+\Omega_{i j m n}^{u d(2)}\left(Q_{i} \bar{u}_{j}\right)\left(Q_{m} \bar{d}_{n}\right)+\Omega_{i j m n}^{u \ell(2)}\left(Q_{i} \bar{u}_{j}\right)\left(L_{m} \bar{\ell}_{n}\right)+\text { h.c. }\right]
\end{aligned}
$$

- From the light Higgs

$$
\begin{aligned}
& \omega_{i j m n}^{u u(0)}\left(u_{i} \bar{u}_{j}\right)\left(\bar{u}_{m}^{\dagger} u_{n}^{\dagger}\right)+\omega_{i j m n}^{d d(0)}\left(d_{i} \bar{d}_{j}\right)\left(\bar{d}_{m}^{\dagger} d_{n}^{\dagger}\right)+\omega_{i j m n}^{\ell \ell(0)}\left(\ell_{i} \bar{\ell}_{j}\right)\left(\bar{\ell}_{m}^{\dagger} \ell_{n}^{\dagger}\right) \\
+ & {\left[\omega_{i j m n}^{d \ell(0)}\left(d_{i} \bar{d}_{j}\right)\left(\bar{\ell}_{m}^{\dagger} \ell_{n}^{\dagger}\right)+\omega_{i j m n}^{u d(2)}\left(u_{i} \bar{u}_{j}\right)\left(d_{m} \bar{d}_{n}\right)+\omega_{i j m n}^{u \ell(2)}\left(u_{i} \bar{u}_{j}\right)\left(\ell_{m} \bar{\ell}_{n}\right)\right.} \\
+ & \omega_{i j m n}^{u u(2)}\left(u_{i} \bar{u}_{j}\right)\left(u_{m} \bar{u}_{n}\right)+\omega_{i j m n}^{u d(0)}\left(u_{i} \bar{u}_{j}\right)\left(\bar{d}_{m}^{\dagger} d_{n}^{\dagger}\right)+\omega_{i j m n}^{u \ell(0)}\left(u_{i} \bar{u}_{j}\right)\left(\bar{\ell}_{m}^{\dagger} \ell_{n}^{\dagger}\right) \\
+ & \left.\omega_{i j m n}^{d d(2)}\left(d_{i} \bar{d}_{j}\right)\left(d_{m} \bar{d}_{n}\right)+\omega_{i j m n}^{d \ell(2)}\left(d_{i} \bar{d}_{j}\right)\left(\ell_{m} \bar{\ell}_{n}\right)+\omega_{i j m n}^{\ell \ell(2)}\left(\ell_{i} \bar{\ell}_{j}\right)\left(\ell_{m} \bar{\ell}_{n}\right)+\text { h.c. }\right]
\end{aligned}
$$

## Comparison of four fermion operators

- Take a particular example. For the Heavy Higgs mediated operators

$$
\left(d_{i} \bar{d}_{j}\right)\left(\bar{d}_{m}^{\dagger} d_{n}^{\dagger}\right) \frac{\tilde{\lambda}_{2 i j}^{d \dagger} \tilde{\lambda}_{2 m n}^{d}}{\tilde{m}_{2}^{2}}
$$

- The same operator coming from the light Higgs is

$$
\begin{aligned}
& \left(d_{i} \bar{d}_{j}\right)\left(\bar{d}_{m}^{\dagger} d_{n}^{\dagger}\right)\left[\delta_{i j} \delta_{m n} \frac{m_{i}^{d \dagger} m_{m}^{d}}{\lambda_{1} v^{4}}-\frac{1}{\sqrt{2}} \delta_{i j} \tilde{\lambda}_{2 m n}^{d} \frac{\tilde{\lambda}_{6}^{*}}{\lambda_{1}} \frac{m_{i}^{d \dagger}}{v} \frac{1}{\tilde{m}_{2}^{2}}\right. \\
& \left.-\frac{1}{\sqrt{2}} \delta_{m n} \tilde{\lambda}_{2 i j}^{d \dagger} \frac{\tilde{\lambda}_{6}}{\lambda_{1}} \frac{m_{m}^{d \dagger}}{v} \frac{1}{\tilde{m}_{2}^{2}}\right]
\end{aligned}
$$

- The parametric dependence is different, the ED is the same.

