

## small-scale structure


small-scale $P(k)$ is interesting!

- shape of primordial power spectrum related to shape of inflaton potential
- small-scale $P(k)$ sensitive to physics of DM particles

Current best probe is Ly $\alpha$ forest (e.g. Seljak et al. 2006), but already approaching gas Jeans scale!

## abundances

- another probe: abundance of objects (e.g. cluster dn/dM)


SZ maps

## abundances

- another probe:abundance of objects (e.g. cluster dn/dM)
- low mass halos \& sub-halos sensitive to smallscale $P(k)$




## halos and subhalos

## $\mathrm{z}=11.9$

$800 \times 600$ physical kpc
"Via Lactea" Diemand et al. 2006

Diemand, Kuhlen, Madau 2006

## subhalos



Figure 1: Left: Density projection in the Via Lactea-II simulation [18]. Middle: Similar, but excluding particles belonging to subhalos whose masses never exceeded $10^{8} M_{\odot}$ any time throughout the simulation. Right: Like the middle panel, but excluding subhalos with $M_{\max }<10^{10} M_{\odot}$. This sequence should qualitatively illustrate the effect of truncating the power spectrum on substructure content in DM halos.

## How to measure?

- count small galaxies / satellites
$\square$ missing satellite problem (see Kravtsov 2012 for recent review)



How to measure?

- count small galaxies / satellites
$\square$ missing satellite problem (see Kravtsov 2012 for recent review)
$\square$ but low-mass subhalos could be dark...
- need gravitational probe to see dark halos/subhalos
- heating of tidal streams (e.g. Carlberg 2012)
- gravitational lensing!


Figure 11. Estimated gap rate vs. stream width relation for M31 NW, Pal 5, the EBS, and the CDM halo prediction. All data are normalized to 100 kpc . The width of the theoretical relation is evaluated from the dispersion in the length-height relation of Figure 8 . Predictions for an arbitrary alternative mass
functions, $N(M) \propto M^{-1.6}$, normalized to have 33 halos above $10^{9} M_{\odot}$ are shown with a dotted line.

## Gravitational lensing

- the deflection of light rays caused by inhomogeneities
- also distorts the apparent shapes \& sizes of observed sources
- amount of lensing characterized by convergence $\kappa \sim \int \delta \rho d l$
- Two regimes:
- weak lensing $(|\kappa| \ll 1)$ : small distortion
- strong lensing ( $\kappa \gtrsim 1$ ) : large distortion \& multiple imaging



## subhalo lensing

small ( $M<10^{8} M_{\odot}$ ) halos and subhalos are wimpy lenses!

- small size ( $\leqslant \mathrm{kpc}$ ), so each one affects a small fraction of the sky
- lensing amplitude is weak (central $\kappa, \gamma \leqslant 0.1$ )
- need a way to boost their effect to detect them...


## strong lensing



- if a small halo/subhalo projects near a strong lens, then the big lens can magnify the lensing effect of the small halo


$$
\Delta \theta \approx \mathbf{M} \cdot \Delta \alpha
$$

if high magnification, then perturbation can have big effect! (Mao \& Schneider 1998)

## universality relations

- when 2 images are close together, they should have nearly equal brightness


$$
\frac{\Delta f}{f} \propto \frac{\Delta r}{r_{s}}
$$

## universality relations

- when 2 images are close together, they should have nearly equal brightness

[

$$
\frac{\Delta f}{f} \propto \frac{\Delta r}{r_{s}}
$$

- similar relation when 3 images occur close together:

$\frac{f_{A}-f_{B}+f_{C}}{f_{A}+f_{B}+f_{C}} \propto \frac{\Delta r}{r_{s}}$


## universality relations



$\frac{f_{A}-f_{B}+f_{C}}{f_{A}+f_{B}+f_{C}} \propto \frac{\Delta r}{r_{s}}$

## flux anomalies

- implication: local scale length $r_{s}$ is much smaller than size of the system $\Rightarrow$ substructure in the potential
- in radio quasars, flux ratio anomalies can only be caused by mass substructure (not true for optical lenses)
- flux anomalies occur in almost all of the observed quasar lenses $\Rightarrow$ lots of substructure!


# how do we know it's substructure? 

- radio flux ratios independent of $\lambda$, as expected for lensing but unlike propagation effects (like scintillation or dust extinction)
- observed parity dependence:
+ parity magnified, - parity demagnified
- radio quasars too big to be affected by stellar microlensing, unlike stellar QSO's.
- see Kochanek \& Dalal (2003) for more...


## analysis of radio lenses

- Dalal \& Kochanek (2002) analyzed sample of $\mathbf{7}$ radio lenses
- found that ~ I-2\% of projected mass at 5 kpc is in substructure



## how to improve?

- DK02 analyzed a tiny sample (7 lenses), but many more lenses are known, e.g. > 100 optical lenses
- unfortunately, optical QSO's are affected by extinction and stellar microlensing
- can circumvent with mid-IR fluxes, but most QSO's are faint in mid-IR
- galaxy lenses (e.g. SLACS) are really challenging (see, e.g.,Vegetti et al. 2012)


## how to improve?

- we need a new class of lensed sources!


## $4 \mathrm{ceg}^{2}$

All these "large-scale" fluctuations are primary CMB.


## so what?

- why should we care about SPT's SMGs?
- because they're (basically) all lensed!



## ALMA Cycle 0 Band 7350 GHz 2 minute snapshots



8" x 8" boxes



SPT 2147-50
$\mathrm{z}=3.761$ VLT/ISAAC

Only through the combination of strong gravitational lensing, the SPT selection, and ALMA followup is this result possible


## Lens models

dirty image model image residual source model
SPT 0346－52
$z_{\mathrm{S}}=5.67 ; z_{\mathrm{L}} \sim 0.8$
$r_{E}=1.1 \mathrm{arcsec}$
$\mathrm{M}=3.7 \times 10^{11} \mathrm{M}$ 。
$\mu=5.4$
$\Sigma_{\mathrm{FIR}}=24 \times 10^{12} \mathrm{~L}_{\circ} / \mathrm{kpc}^{2}$
$\mathrm{R}_{1 / 2}=0.6 \mathrm{kpc}$
$\mathrm{L}_{\mathrm{FIR}}=3.7 \times 10^{13} \mathrm{~L}$ 。 $\mathrm{S}_{850 \mu \mathrm{~m}}=25.5 \mathrm{mJy}$


SPT 418－47
$z_{S}=4.22 ; z_{L}=0.27$
$\mathrm{r}_{\mathrm{E}}=1.4 \mathrm{arcsec}$
$\mathrm{M}=2.4 \times 10^{11} \mathrm{M}$ 。
$\mu=21$
$\Sigma_{\mathrm{FIR}}=0.74 \times 10^{12} \mathrm{~L}$ 。／kpc ${ }^{2}$
$\mathrm{R}_{1 / 2}=1.1 \mathrm{kpc}$
$\mathrm{L}_{\mathrm{FIR}}=3.8 \times 10^{12} \mathrm{~L}$ 。
$\mathrm{S}_{850 \mu \mathrm{~m}}=4.8 \mathrm{mJy}$


SPT 0529－54
$z_{\mathrm{S}}=3.37 ; \mathrm{zL}_{\mathrm{L}}=0.13$
$r_{\mathrm{E}}=1.5 \mathrm{arcsec}$
$\mathrm{M}_{\mathrm{L}}=1.6 \times 10^{11} \mathrm{M}$ 。
$\mu=9.4$

SPT 0538－50
$z_{\mathrm{S}}=2.782 ; z_{\mathrm{L}}=0.4$
$\mathrm{r}_{\mathrm{E}}=2.0 \mathrm{arcsec}$
$\mathrm{M}_{\mathrm{L}}=7.2 \times 10^{11} \mathrm{M}$ 。 $\mu=20.5$

Hezaveh et al．（2013）
$\Sigma_{\text {FIR }}=0.15 \times 10^{12} \mathrm{~L} \odot / \mathrm{kPC}^{2}$
$\mathrm{R}_{1 / 2}=2.4 \mathrm{kpc}$
$\mathrm{L}_{\text {FIR }}=3.8 \times 10^{12} \mathrm{~L}$ 。
$\mathrm{S}_{850 \mu \mathrm{~m}}=13 \mathrm{mJy}$

$\Sigma_{\text {FIR }}=1.0 \times 10^{12} \mathrm{~L} 。 / \mathrm{kpc}_{5}^{2}$
$\mathrm{R}_{1 / 2}=1.0 \mathrm{kpc}$
$\mathrm{L}_{\mathrm{FIR}}=4.5 \times 10^{12} \mathrm{~L}$ 。
$\mathrm{S}_{850 \mu \mathrm{~m}}=6.1 \mathrm{mJy}$


## okay.... so what?

- lensed SMG's are perfect for detecting substructure!
- theoretically, we expect these galaxies to contain many compact star-forming clumps (~10-I00pc) inside much bigger GMC's ( $\sim \mathrm{kpc}$ ). see also local analogues like Arp 220
- clumps are extremely bright in lines like CO 7-6
- example: high resolution SMA imaging of lensed SMG reveals compact source clumps
(Swinbank et al. 2010)



## The Strength of Substructure Lensing Signal Depends on the Source Size



## The Strength of Substructure Lensing Signal Depends on the Source Size



## The Strength of Substructure Lensing Signal Depends on the Source Size



## The Strength of Substructure Lensing Signal Depends on the Source Size



## The Strength of Substructure Lensing Signal Depends on the Source Size



## The Strength of Substructure Lensing Signal Depends on the Source Size



## The Strength of Substructure Lensing Signal Depends on the Source Size



## The Strength of Substructure Lensing Signal Depends on the Source Size



## The Strength of Substructure Lensing Signal Depends on the Source Size



## The Strength of Substructure Lensing Signal Depends on the Source Size

 Compact Sources Are Perturbed More Strongly

## Spatially resolved spectroscopy



Figure 2. SMM J131201: this system displays a complex, irregular morphology; it most likely is an advanced pre-coalescence merger. The RGB image (mapping red, green, and blue parts of the spectrum) shows no indication of rotation. Spectra are, left: northeast (top) and southeast (bottom) arm, right: entire system (top), and central part (bottom). The beam size ( $0^{\prime \prime} 59 \times 0^{\prime} .47$, P.A. $=50: 9$ ) is displayed in the lower left corner of the flux maps. North is up and east is to the left. Scale bar denotes $1^{\prime \prime}$.
(A color version of this figure is available in the online joumal.)

## Velocity decomposition can separate small features of the source



so each SMG is equivalent to having many sources behind each lens!

## Simulations of ALMA observations

* observe high excitation lines (e.g. CO 7-6)
* use most extended configuration in Cycle 1, one hour total integration

$$
\text { e.g. } \mathrm{CO} \quad 1-0 \quad 2-1
$$

Low excitation lines need low temperatures and densities to be excited. The whole molecular reservoirs of the galaxies will be emitting these lines over large extended regions.
e.g. CO 7-6 HCN HCO+ H2O

High excitation lines need higher temperatures and densities to be excited. They are dense gas tracers and are emitted from the compact cores of star forming clumps

## Mean Number of Detections Per Lens (Cycle 1)

expect $\sim \mathrm{O}(1)$ detections in each lens system

even the low-magnification systems can be useful!

## cosmology constraints

- existing sample (DK02) is $\mathbf{7}$ quasar lenses
- from SPT we expect $\sim 100$ SMG lenses, and each SMG lens is much more constraining than a quasar
- How do these measurements translate into bounds on cosmology?


## cosmology constraints

- existing sample (DK02) is $\mathbf{7}$ quasar lenses
- from SPT we expect ~100 SMG lenses, and each SMG lens is much more constraining than a quasar
- How do these measurements translate into bounds on cosmology?
- We don't know - currently limited by theory! we don't know how to calculate substructure as a function of WDM, etc.
- we're working on it (Arka Banerjee)
- other statistics besides mass function might be more useful, e.g. substructure power spectrum


## Conclusion:

- SMG lensing is great for DM substructure
- stay tuned!

