

# THE SIMP MIRACLE

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DECEMBER

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# THE UNIVERSE IS DARK

The biggest unexplained mystery of the Universe is  
Dark Matter

It is physics strictly beyond the Standard Model

It requires at least one new degree of freedom to exist

At least one incredibly long lived particle  
that exists in our galaxy today

DM Lifetime  $> 10^7$  Age of Universe



# THE LONG LIST OF DARK MATTER PROPERTIES

- 1.) Dark Matter has 5 times the mass density of Baryons

$$\frac{\rho_{\text{dm}}}{\rho_{\text{b}}} \equiv \xi \simeq 5$$

- 2.) It is a massive particle  
of unknown mass

- 3.) It has suppressed interactions with QED & QCD  
could have milli-charge  
or interact through higher dim operators

- 4.) It doesn't strongly self-interact  
Limits on  $\sigma/m_{\text{dm}} < 1$  barn/GeV  
neutron scattering is 0.1 barn/GeV



# OUTLINE

\* L E E - W E I N B E R G & W I M P S

\* T H E S I M P M I R A C L E

\* T H E S E A R C H F O R S I M P S

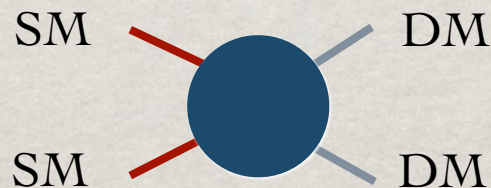
\* O U T L O O K



# EARLY UNIVERSE COSMOLOGY AND DARK MATTER



Lee & Weinberg in 1977 elegantly  
linked Dark Matter genesis  
and Early Universe Cosmology



If a new stable particle has 2-to-2 interactions with SM,  
and Universe has hotter than its mass,  
there will be a relic density left over

# DARK MATTER FREEZE OUT

$$\dot{n} + 3Hn = (\cancel{n_{\text{eq}}^2} - \cancel{n^2}) \langle \sigma_{\text{ann}} v \rangle$$

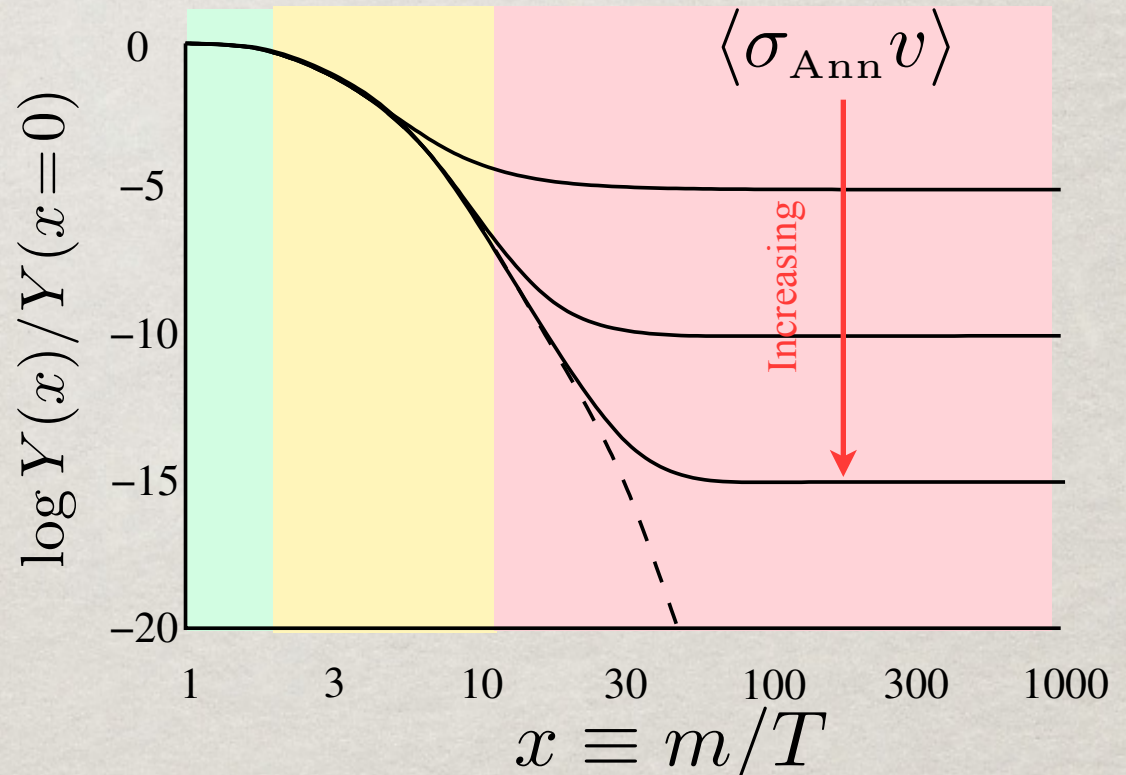
$n$  ~ number of DM per volume

$$n_{\text{eq}} \sim e^{-m/T} s$$

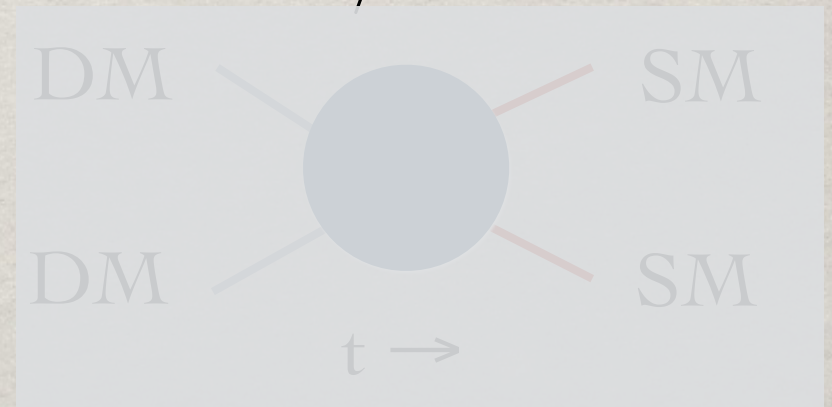
$s$  ~ number of photons per volume

$$Y_{\text{dm}} = n_{\text{dm}}/s$$

number of DM per photon



$$\Gamma_{\text{pro}} = n_{\text{sm}} \langle \sigma v \rangle$$



$$\Gamma_{\text{ann}} = n_{\text{dm}} \langle \sigma v \rangle$$



# WIMPs

If the interactions are through the weak interactions,

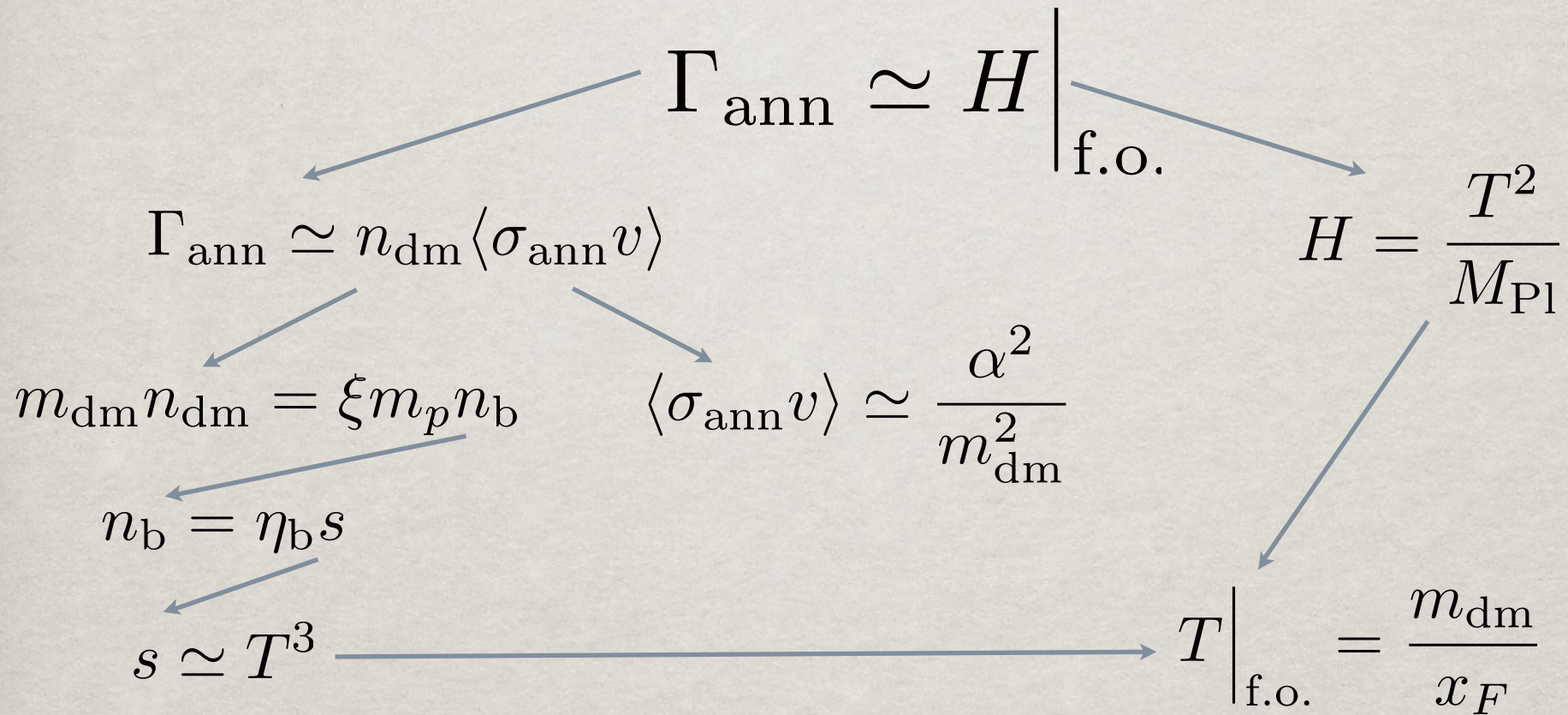
$m_{\text{dm}}$  should be between 100 GeV and 3 TeV

Coincidence if the interactions are weak,  
dark matter should be at the weak scale

WIMPs have been the dominant model for 35+years



# BACK OF THE ENVELOPE SOLUTION



$$\frac{\xi m_p \eta_b \alpha^2}{x_F^3} \simeq \frac{m_{\text{dm}}^2}{x_F^2 M_{\text{Pl}}} \quad m_{\text{dm}} \simeq \alpha \left( \xi \eta_b m_p M_{\text{Pl}} / x_F \right)^{\frac{1}{2}}$$



# EXAMINATION OF LEE-WEINBERG

$$m_{\text{dm}} \simeq \alpha \left( \xi \eta_b m_p M_{\text{Pl}} / x_F \right)^{\frac{1}{2}}$$

$T_{\text{eq}} \simeq 1 \text{ eV}$  Matter-Radiation Equality Temperature

$$m_{\text{dm}} \simeq \alpha \left( T_{\text{eq}} M_{\text{Pl}} / x_F \right)^{\frac{1}{2}}$$

Particle Physics

$\alpha$  unknown strength of  
2-to-2 annihilation  
of DM to SM

Details of solving  
Boltzmann Equation

$$20 \lesssim x_F \lesssim 30$$

$$m_{\text{dm}} \simeq \alpha \times 30 \text{ TeV}$$



# TeV SCALE EMERGED

No Particle Physics went into

$$m_{\text{dm}} \simeq \alpha \times 30 \text{ TeV}$$

$$\alpha_{\text{weak}} = 1/30$$

WIMPs at 1 TeV emerged without input of scale

Truly a coincidence of scales

If interactions are suppressed, then DM could be lighter

e.g. if DM is admixture of singlet & EW-charged state

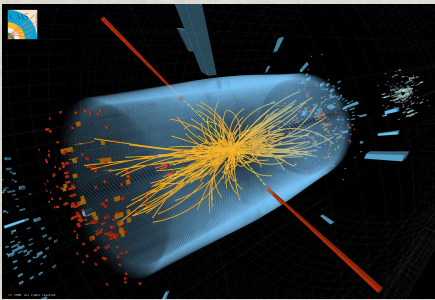
$$\alpha_{\text{eff}} = \alpha_{\text{weak}} \sin^2 \theta_{\text{mix}}$$



# THE SEARCH FOR WIMPS

## 3 Pillars in the Search for DM

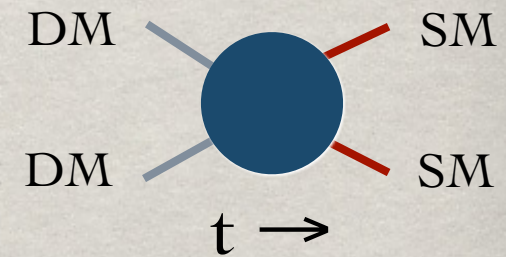
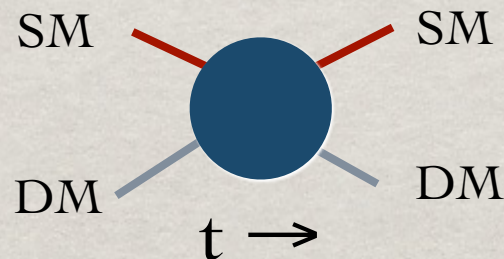
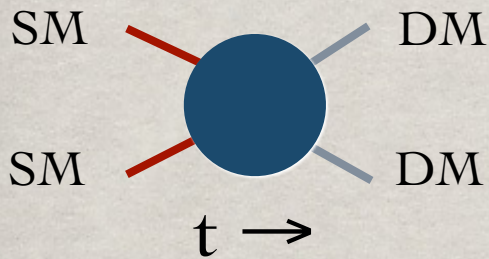
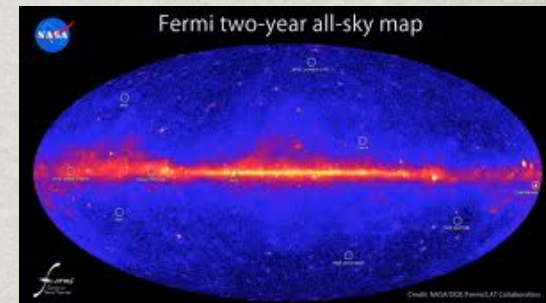
Direct Production



Direct Detection



Indirect Detection

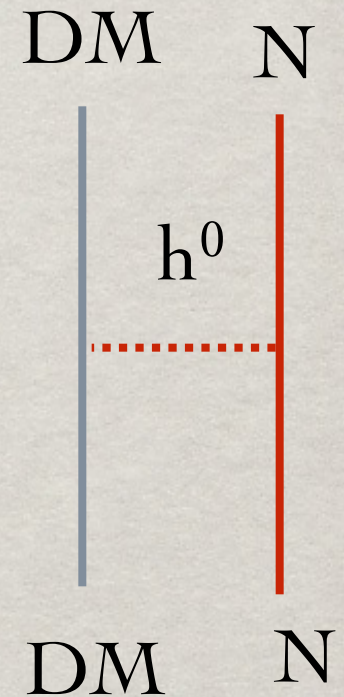
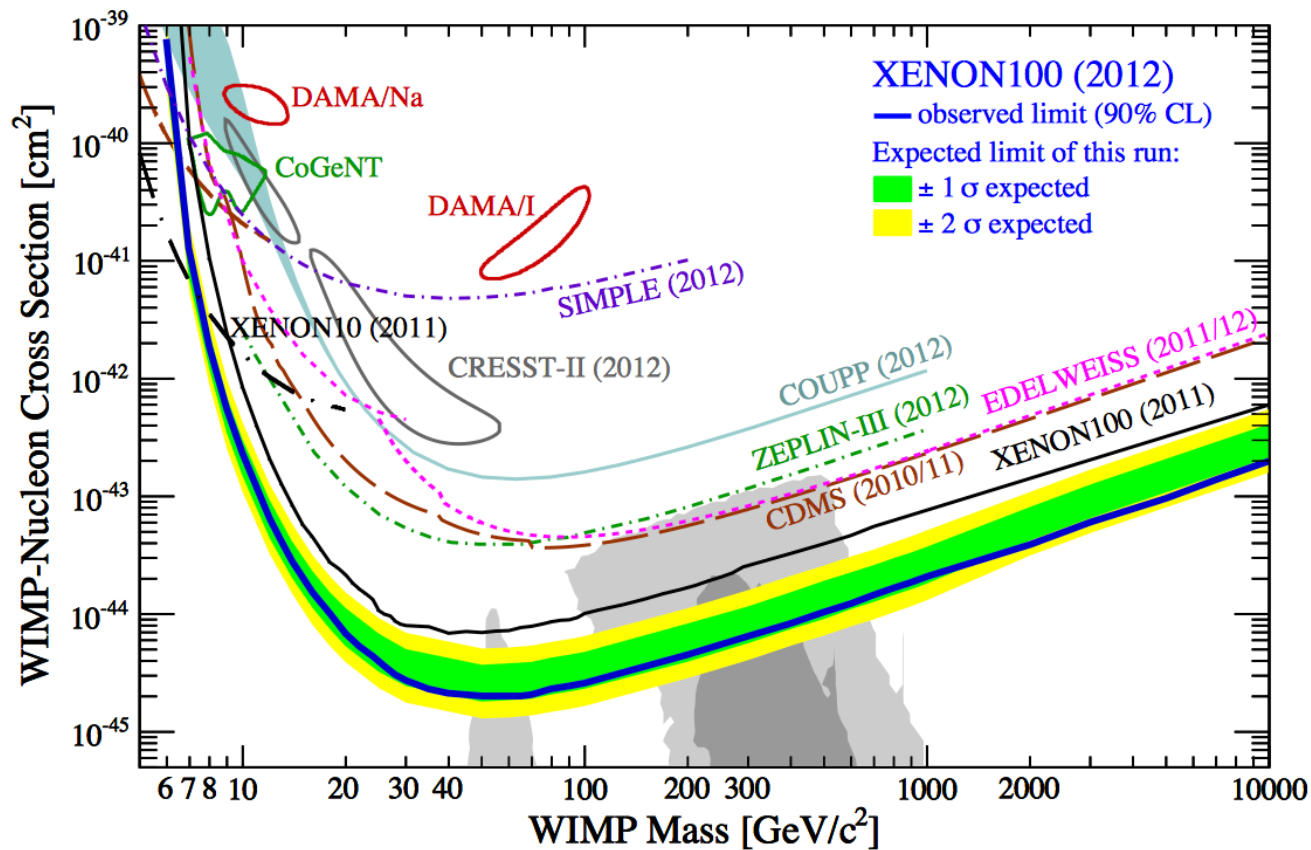




# WIMPS BEING CHALLENGED

Spin independent  $Z^0$ -mediated interactions long ruled out

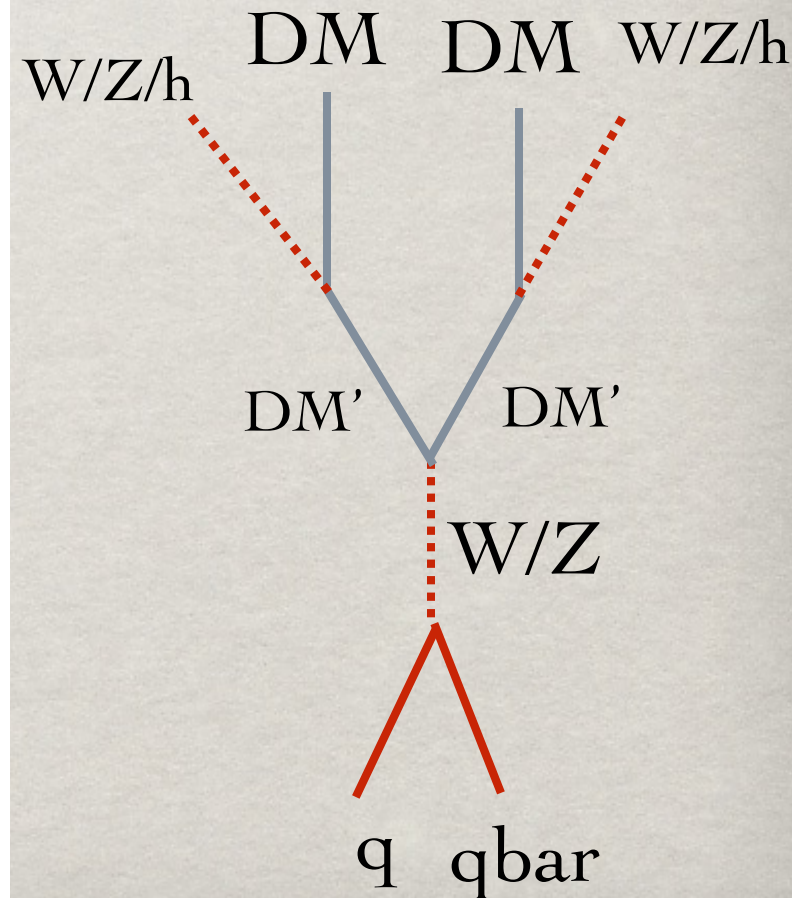
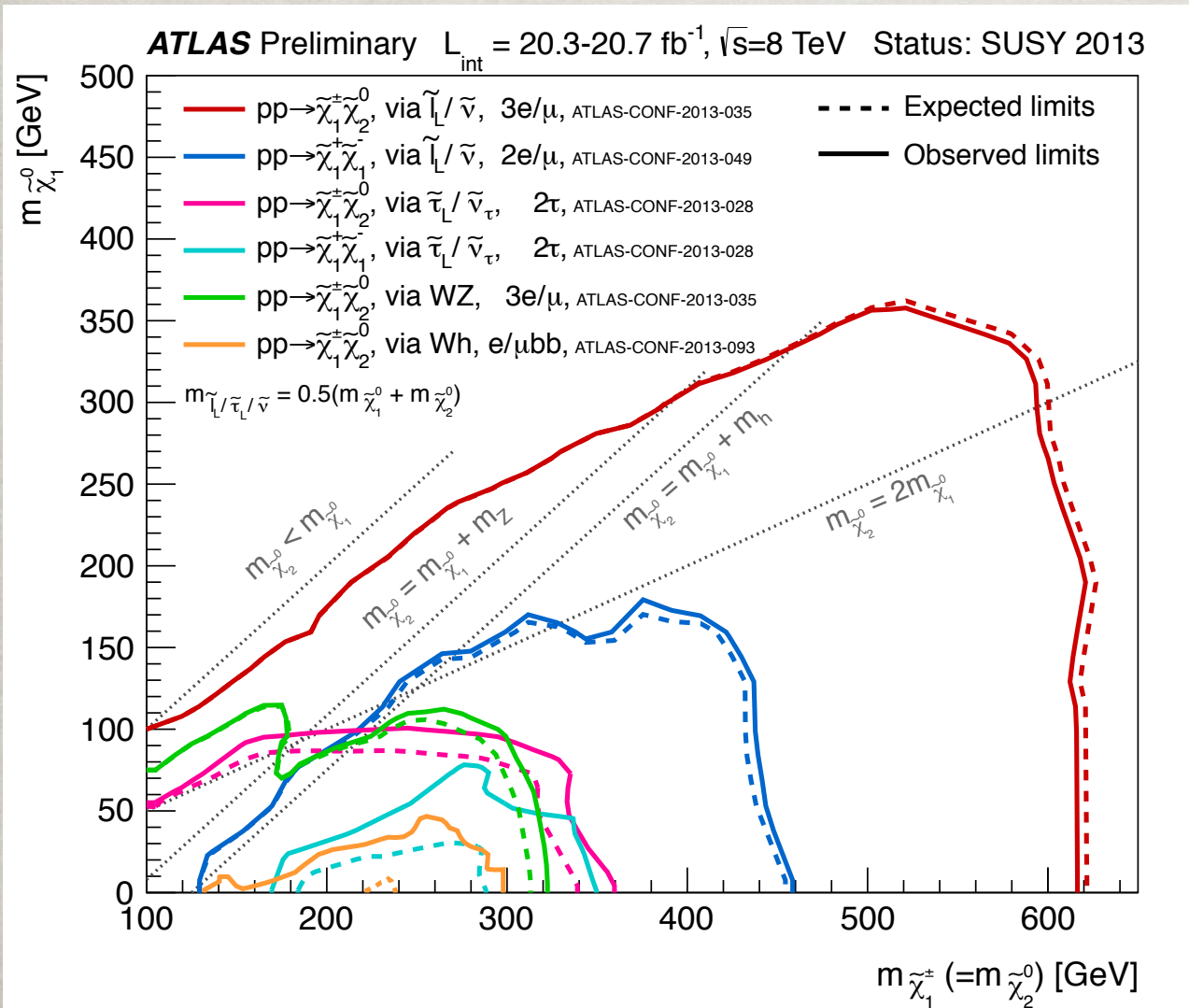
Xe100 greatly constrained  $h^0$ -mediated interactions





# WIMPs BEING CHALLENGED

LHC extending searches for EW DM

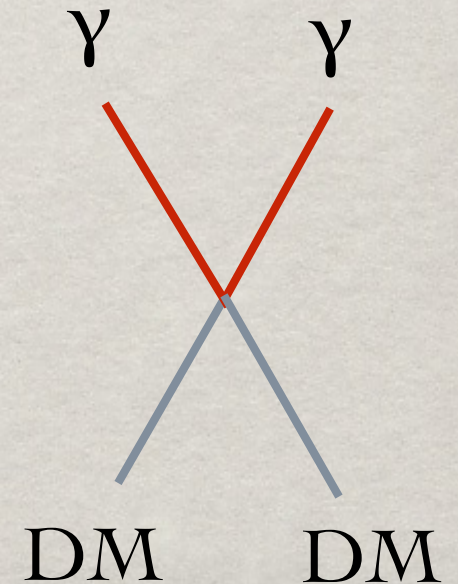
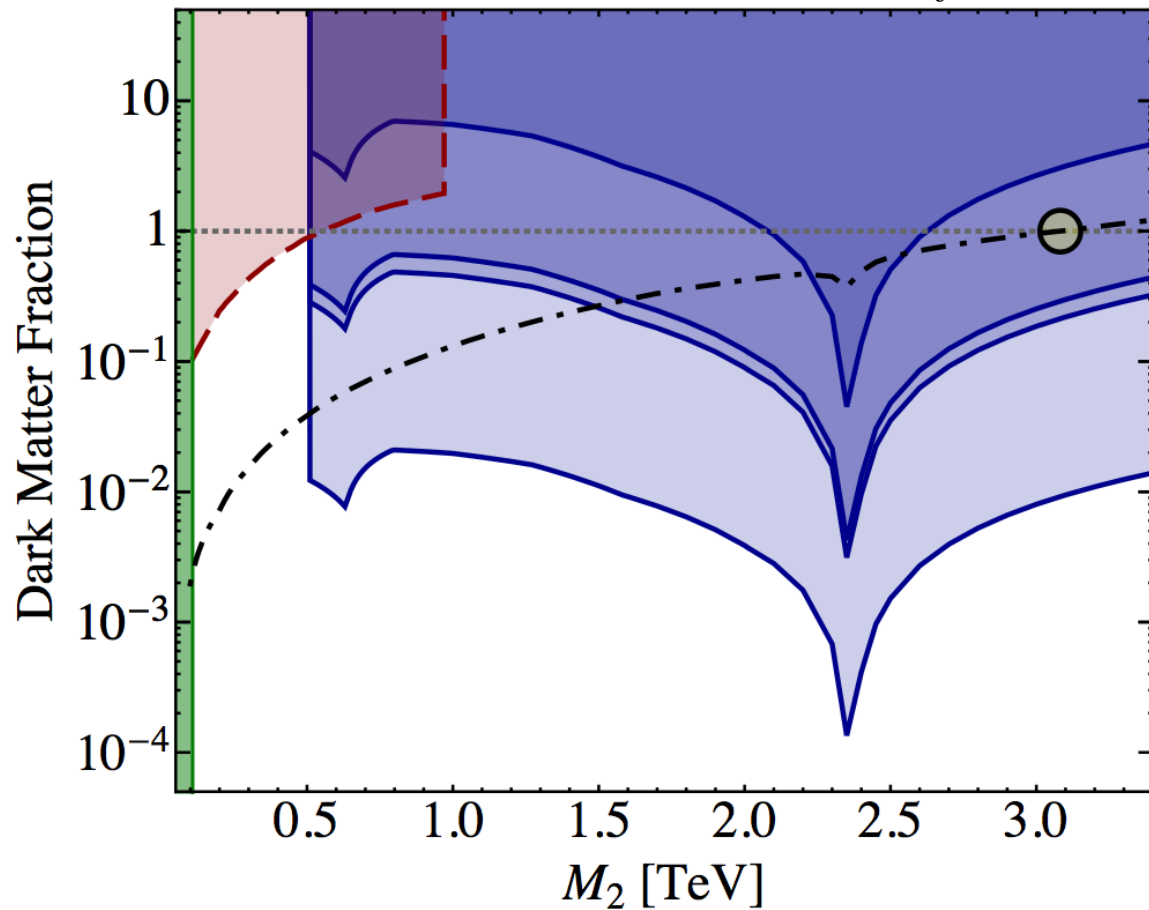




# WIMPS BEING CHALLENGED

HESS ruled out thermal Wino

Cohen, Lisanti Slayter 1307.4082





# WIMPs IN 2013

Dominant paradigm in DM is being challenged

Lots of non-thermal/quasi-thermal mechanisms

Asymmetric DM

Freeze-In DM

Axion DM

Gravitino DM

Is there another simple thermal mechanism that gives qualitatively different signatures?



# OUTLINE

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\* T H E S I M P M I R A C L E

\* T H E S E A R C H F O R S I M P S

\* O U T L O O K



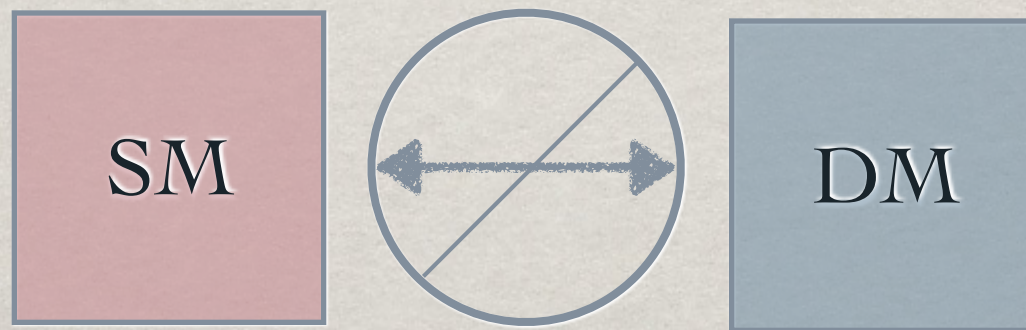
# AN ALTERNATE PARADIGM

Lee-Weinberg assumed unsuppressed interactions with the SM

DM is really part of enlarged SM sector

SM & DM charged under same interactions

What if DM was completely sequestered from SM?



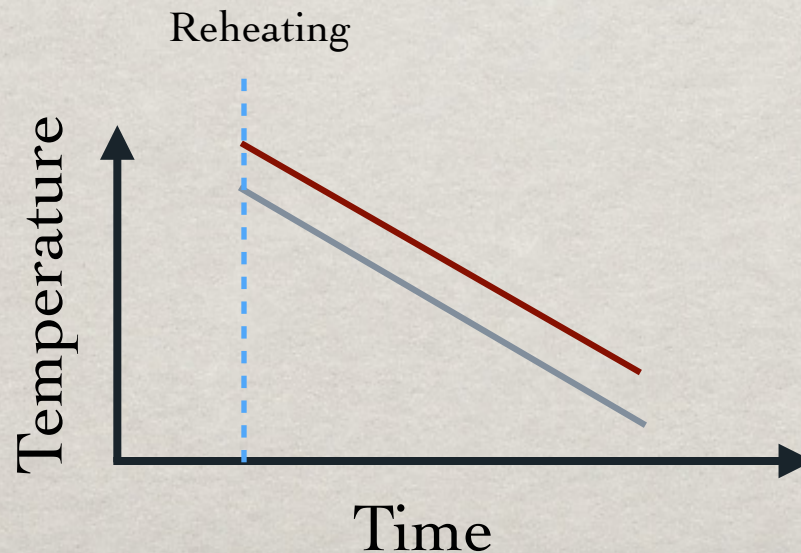


# A HOT HIDDEN SECTOR

Dark Matter is the lightest state in a hot Hidden Sector

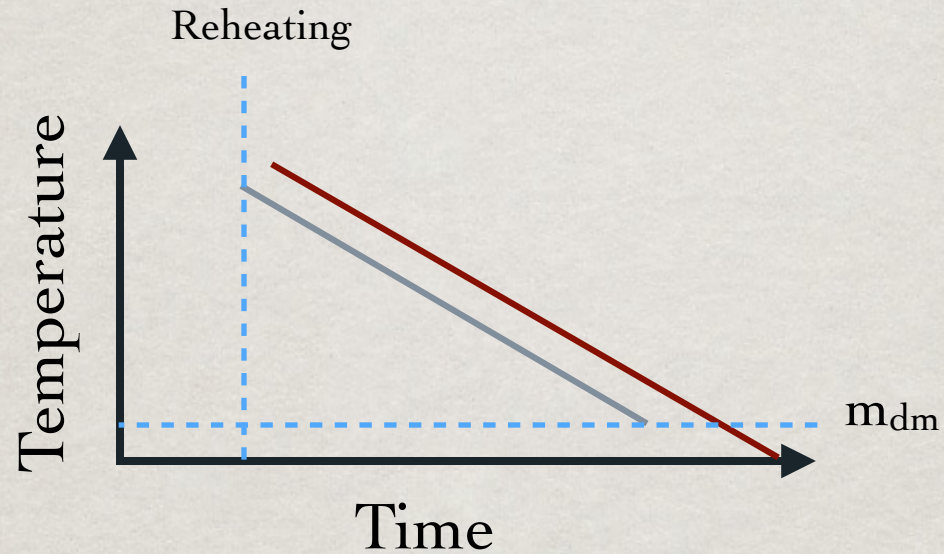
After Inflation, both SM & Dark Sector reheated  
to comparable temperatures

During Radiation Domination, both sectors cool together



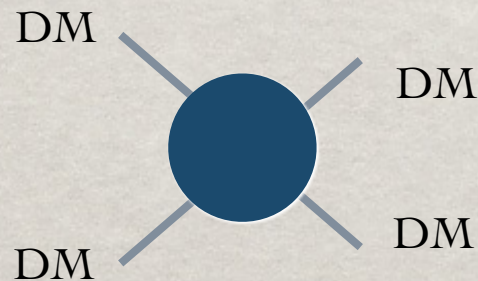


# A HOT HIDDEN SECTOR



When  $T_{dark} \approx m_{dm}$ , dark matter needs to annihilate

but



doesn't change the number density



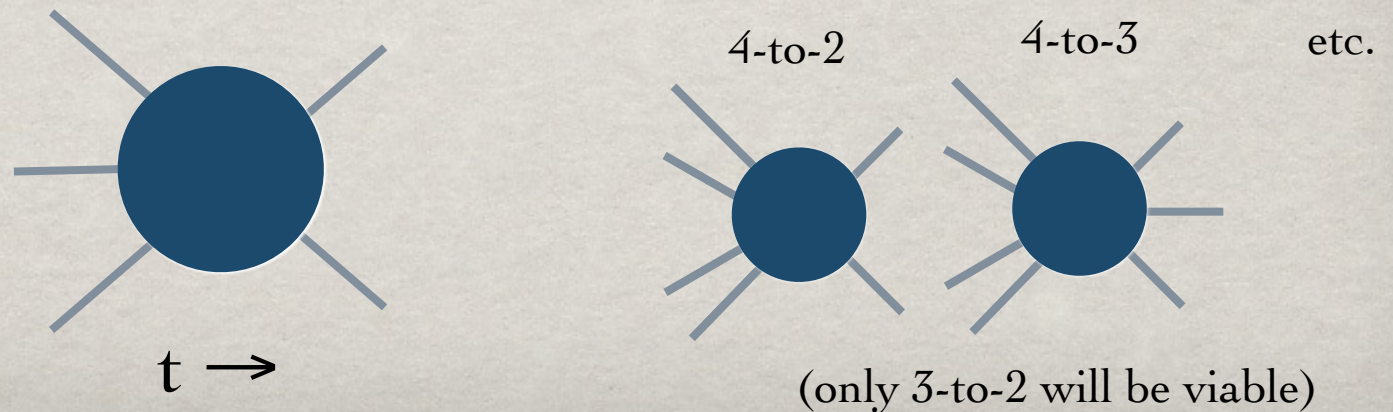
# LIFE WITHOUT 2-2 ANNIHILATION

With no 2-to-2 annihilation possible,  
is the story is over?  $\frac{n_{\text{dm}}}{s} \sim 1$

No...

2-to-2 is the leading interaction that can change number density  
Always absent in a closed system

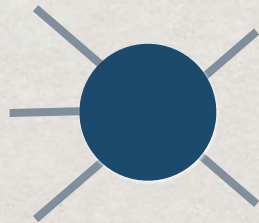
The first process that can change number density in a closed system is a 3-to-2 interaction





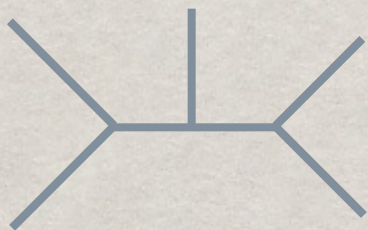
# 5-POINT INTERACTIONS

5-point interactions are a little unfamiliar

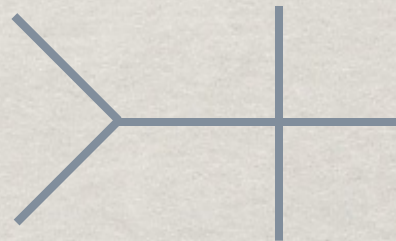


Consider a  $\mathbb{Z}_3$ -symmetric model  $\mathcal{L} \sim m^2|\phi|^2 + \kappa\phi^3 + \lambda|\phi|^4$

DM is stable (proof-in-principle)  $\phi \rightarrow e^{\frac{2\pi i}{3}}\phi$



$$\mathcal{M} \sim \frac{\kappa^3}{m^4}$$



$$\mathcal{M} \sim \frac{\kappa\lambda}{m^2}$$

For single-scale models

$$\kappa \sim gm \quad \lambda \sim g^2$$

$$\mathcal{M} \sim \frac{g^3}{m}$$



# REDOING LEE-WEINBERG

$$\Gamma_{\text{ann}} \simeq H \Big|_{\text{f.o.}}$$
$$\Gamma_{\text{ann}} \simeq n_{\text{dm}}^2 \langle \sigma_{3 \rightarrow 2} v^2 \rangle$$
$$H = \frac{T^2}{M_{\text{Pl}}}$$
$$\langle \sigma_{3 \rightarrow 2} v^2 \rangle \simeq \frac{\alpha^3}{m_{\text{dm}}^5}$$
$$\alpha \sim \frac{g^2}{4\pi}$$

$$m_{\text{dm}} \simeq \alpha \left( T_{\text{eq}}^2 M_{\text{Pl}} / x_F^4 \right)^{\frac{1}{3}}$$

The GeV Scale emerges for Strongly Interacting DM

$$m_{\text{dm}} \simeq \alpha \times 100 \text{ MeV}$$



# THE SIMP MIRACLE

The Lee-Weinberg mechanism leads to the WIMP Miracle

This leads to the SIMP Miracle

Self Interacting Massive Particle

Strongly Interacting Massive Particle

No particle physics went into the derivation of this scale

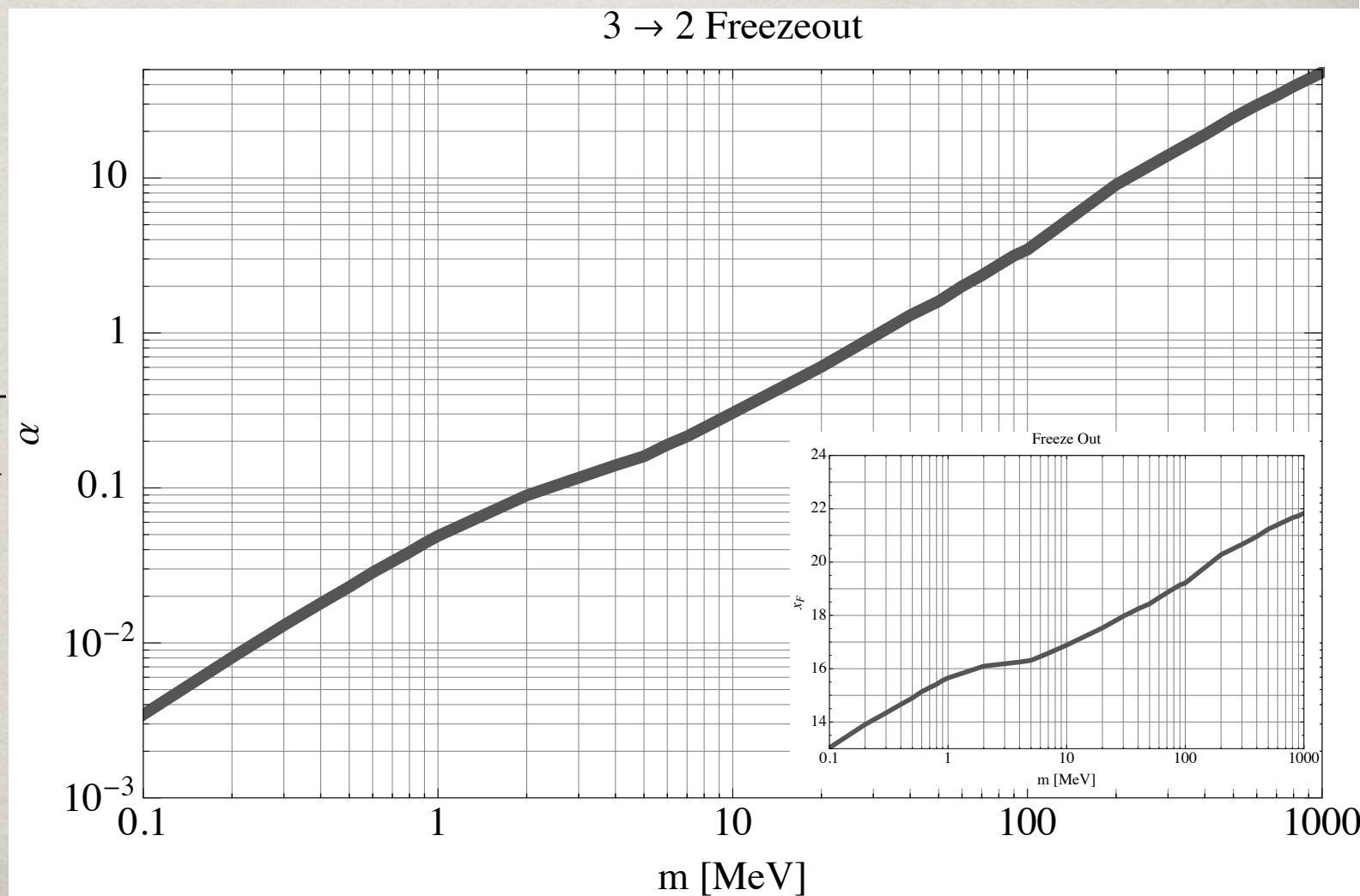
“The second thing you should think of in  
Big Bang Cosmology leads to Dark Matter”



# BOLTZMANN EQUATION (PART 1)

$$\dot{n} + 3Hn = (n^2 n_{\text{eq}} - n^3) \langle \sigma_{3 \rightarrow 2\nu} \rangle$$

$$\langle \sigma_{3 \rightarrow 2\nu} \rangle = \frac{\alpha^3}{m_{\text{dm}}^5} \alpha$$

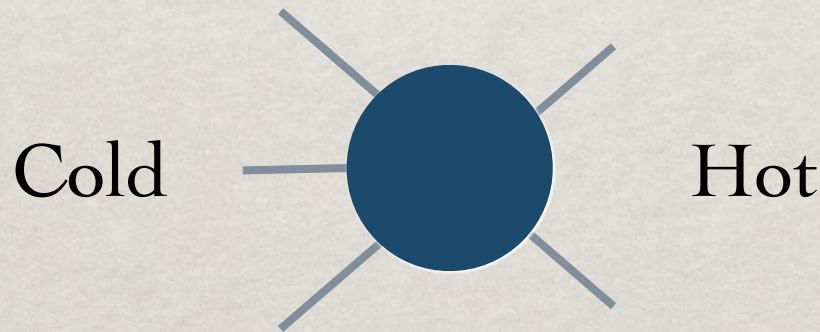




# CAVEAT

Everything about the SIMP Miracle is a not quite right...

Tacitly assumed that the DM temperature  
was following SM temperature



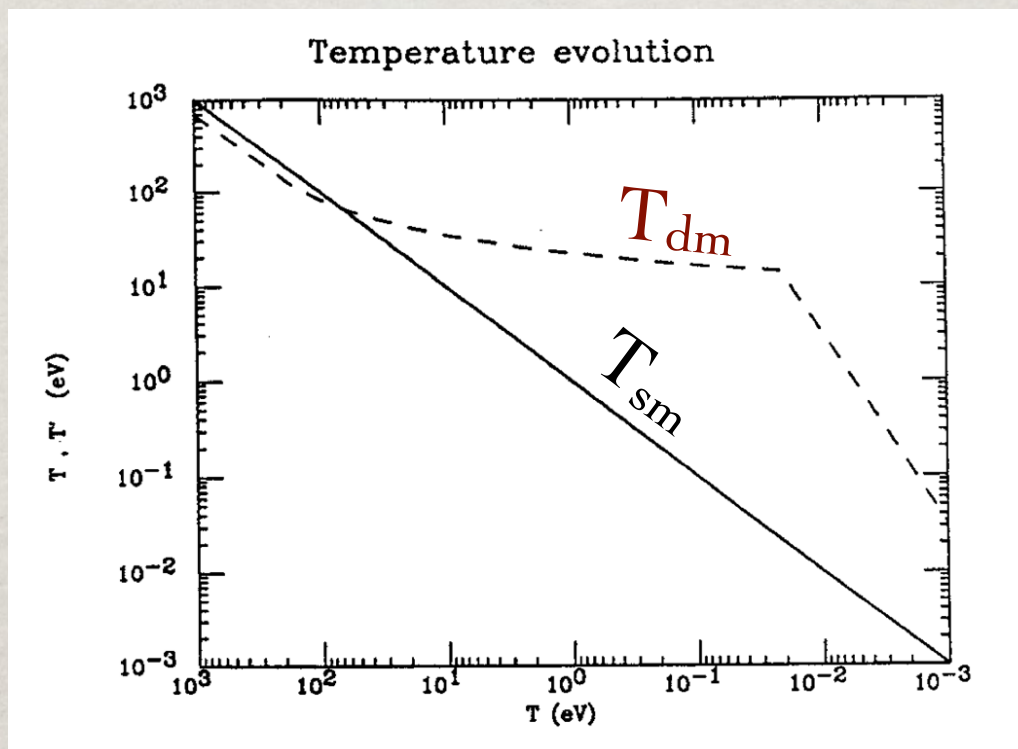
Temperature is approximately constant while freezing out

$$n_{\text{dm}}(t) \propto \exp(-m_{\text{dm}}/T_{\text{dm}}) \neq \exp(-m_{\text{dm}}/T_{\text{sm}})$$

# CARLSON-HALL-MACHACEK

## Selfinteracting dark matter

Eric D. Carlson (Harvard U.), Marie E. Machacek (Northeastern U.), Lawrence J. Hall (UC, Berkeley & LBL, Berkeley). Mar 1992. 31 pp.  
HUTP-91-A066, LBL-32016, UCB-92-06, NUB-3042-92-TH



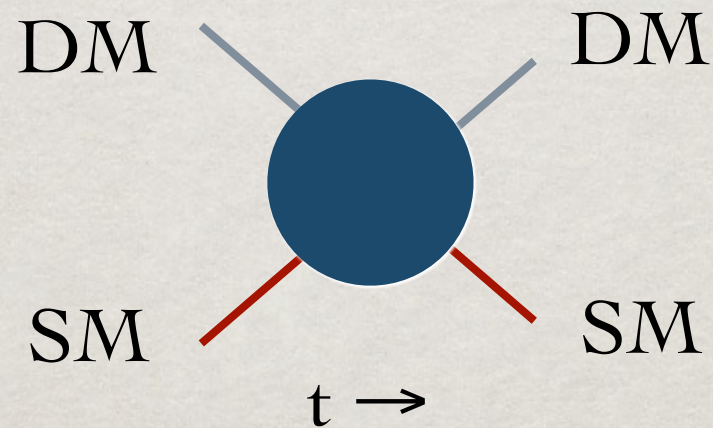
Predicts Light Hot Dark Matter

Disaster! Thoroughly ruled out

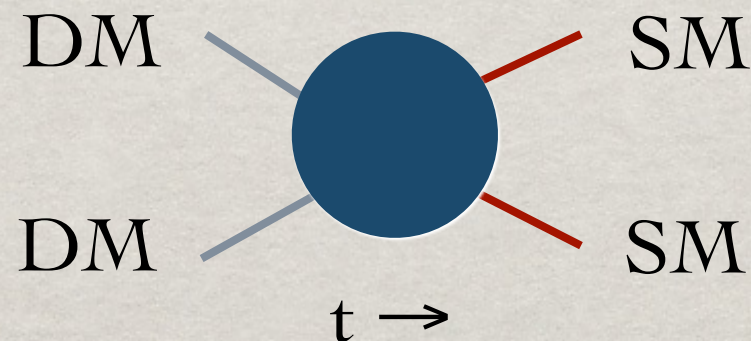


# KEEPING DM & SM IN THERMAL EQUILIBRIUM

Want to cool dark sector

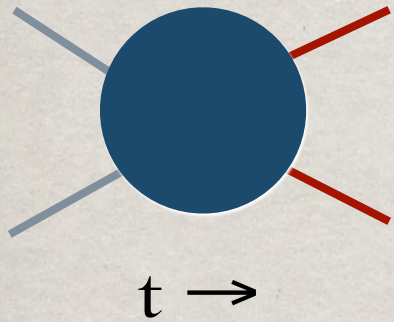


However, don't want Lee-Weinberg Mechanism

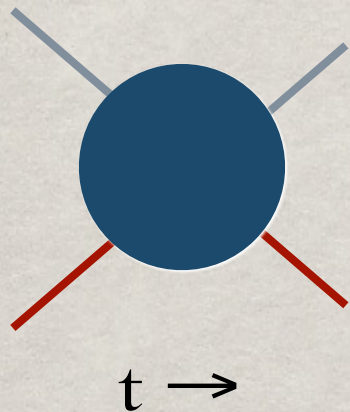


Is this possible?

# COOLING BUT NOT ANNIHILATING



$$\Gamma_{\text{ann}} = n_{\text{dm}} \langle \sigma_{\text{ann}} v \rangle$$



$$\Gamma_{\text{cool}} = n_{\text{sm}} \langle \sigma_{\text{ann}} v \rangle$$

$$\frac{n_{\text{dm}}}{n_{\text{sm}}} \sim e^{-m_{\text{dm}}/T}$$

Need to scatter off light SM species:

$e, \gamma, \nu$



# MODEL OF SIMP INTERACTIONS

Simple model for the interaction

$$\sigma_{\text{SM int}} = \frac{\epsilon^2}{m_{\text{dm}}^2}$$

Assume DM dominantly interacts with electrons

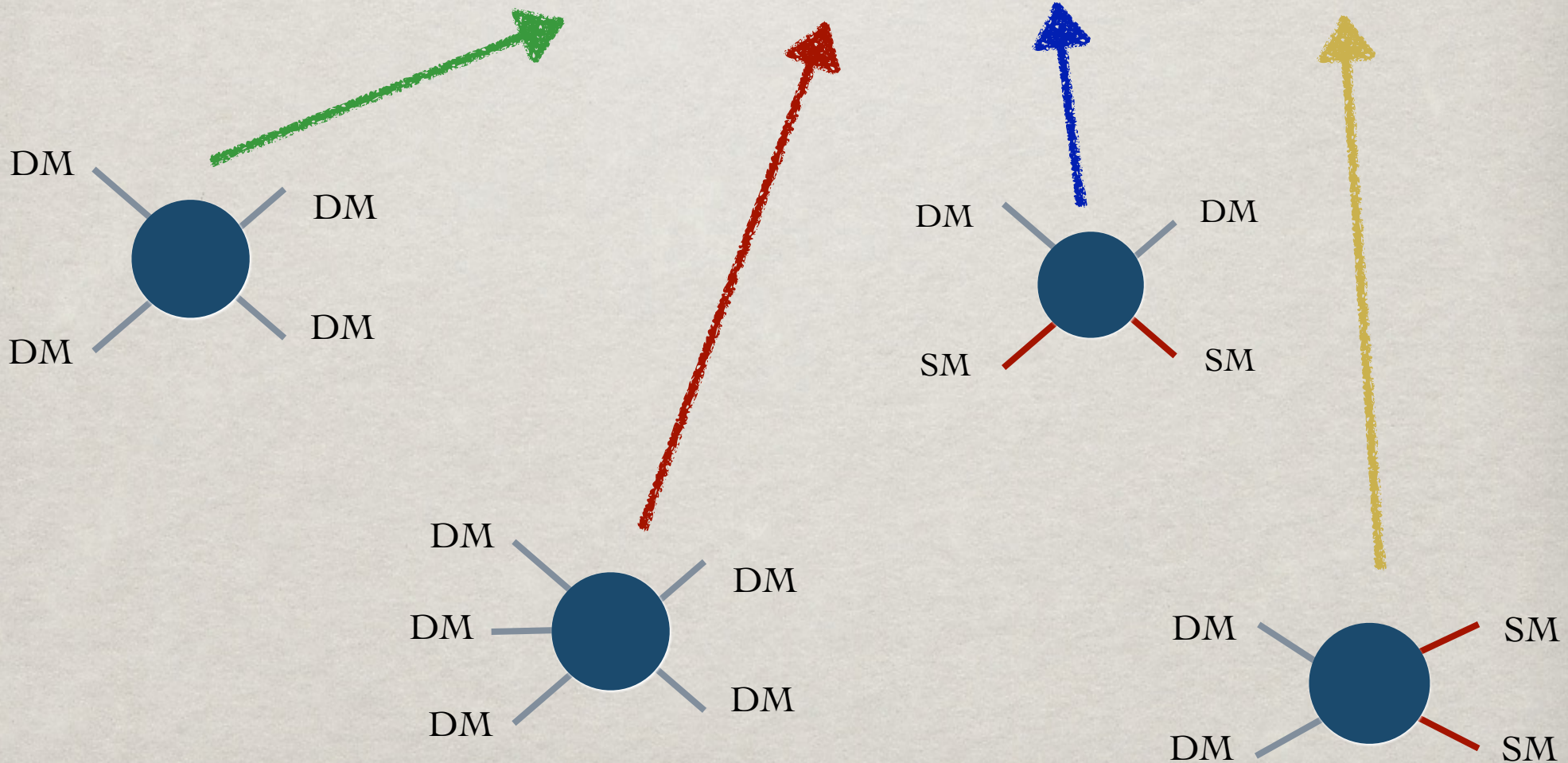
$$\mathcal{L}_{\text{int}} \simeq \frac{\epsilon}{m_{\text{dm}}} |\phi|^2 \bar{e}e$$

(note: does not have to lead to DM decay)



# BOLTZMANN EQUATION (PART 2)

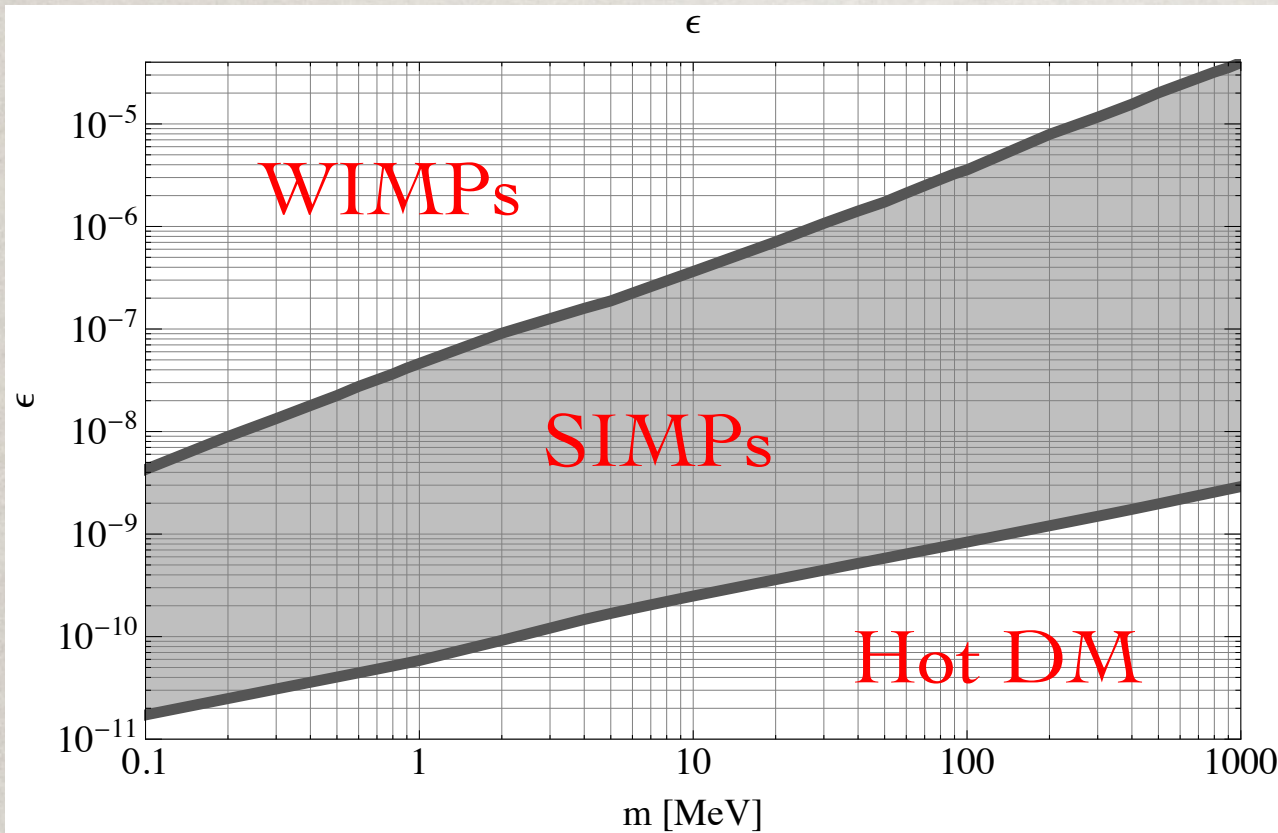
$$E\partial_t f - Hp^2\partial_E f = \gamma_{\text{self kin}} + \gamma_{3\rightarrow 2} + \gamma_{\text{SM kin}} + \gamma_{\text{ann SM}}$$





# NEEDED SIZE OF $\epsilon$

Points to new physics in the 10 GeV to 10 TeV



$$\mathcal{L}_{\text{int}} \simeq \frac{\epsilon}{m_{\text{dm}}} |\phi|^2 \bar{e}e$$

$$\Lambda_{\text{NP}} \sim \sqrt{m_{\text{dm}} m_e / \epsilon}$$

Could be Higgs portal interaction

$$\mathcal{L} \sim \mu s |h|^2 + y_e h \bar{e}e + \kappa s |\phi|^2$$

# THE SIMP MIRACLE REQUIRES SM INTERACTIONS

Dark Matter cannot be completely sequestered from the SM

Some residual interactions, smaller than WIMPs,  
but not arbitrarily small

SIMPs are visible through cadre of standard experiments,  
but a lower interaction rates than standard WIMPs



# OUTLINE

\* L E E - W E I N B E R G & W I M P S

\* T H E S I M P M I R A C L E

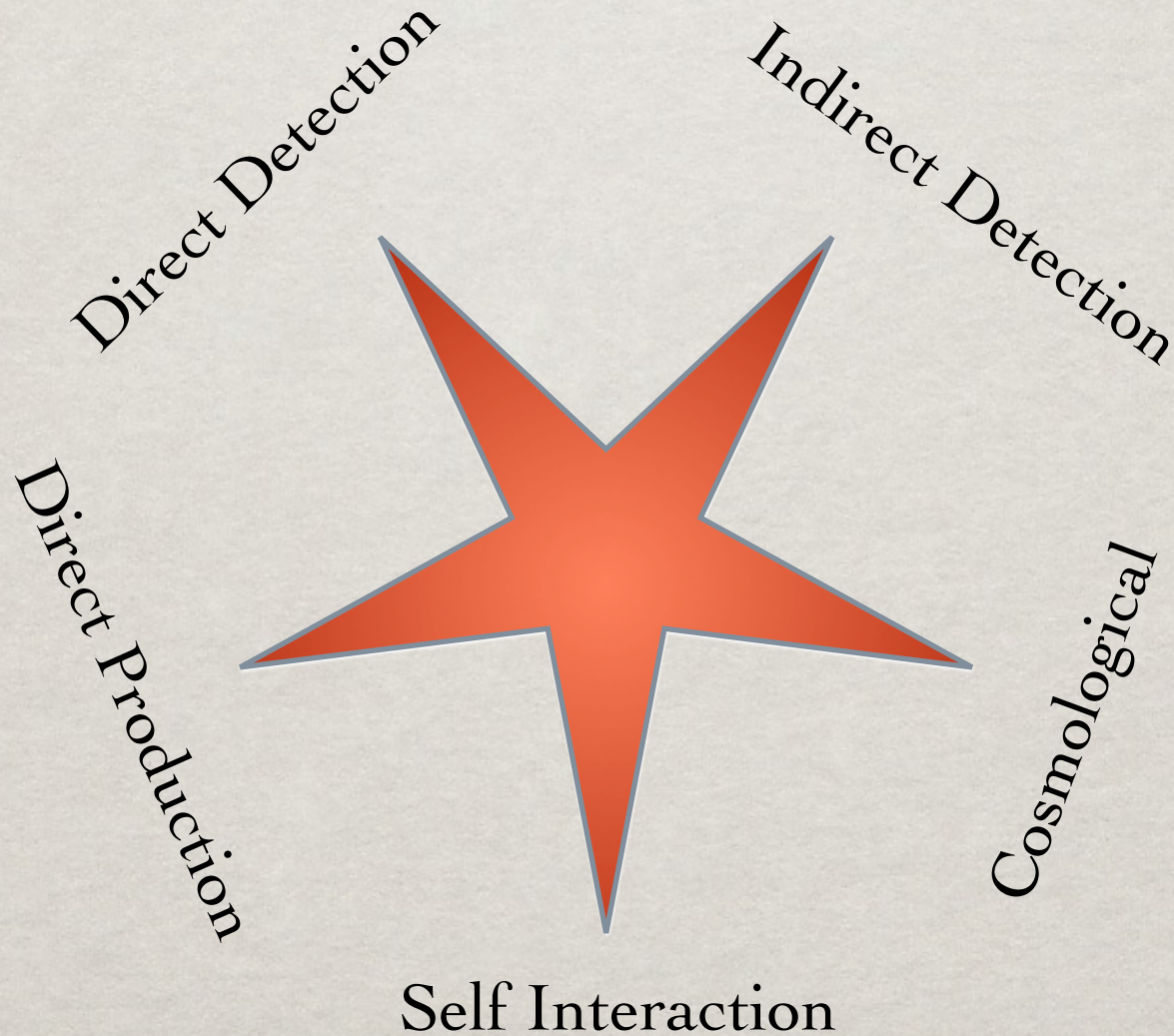
\* T H E S E A R C H F O R S I M P S

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# LIMITS ON SIMP INTERACTIONS

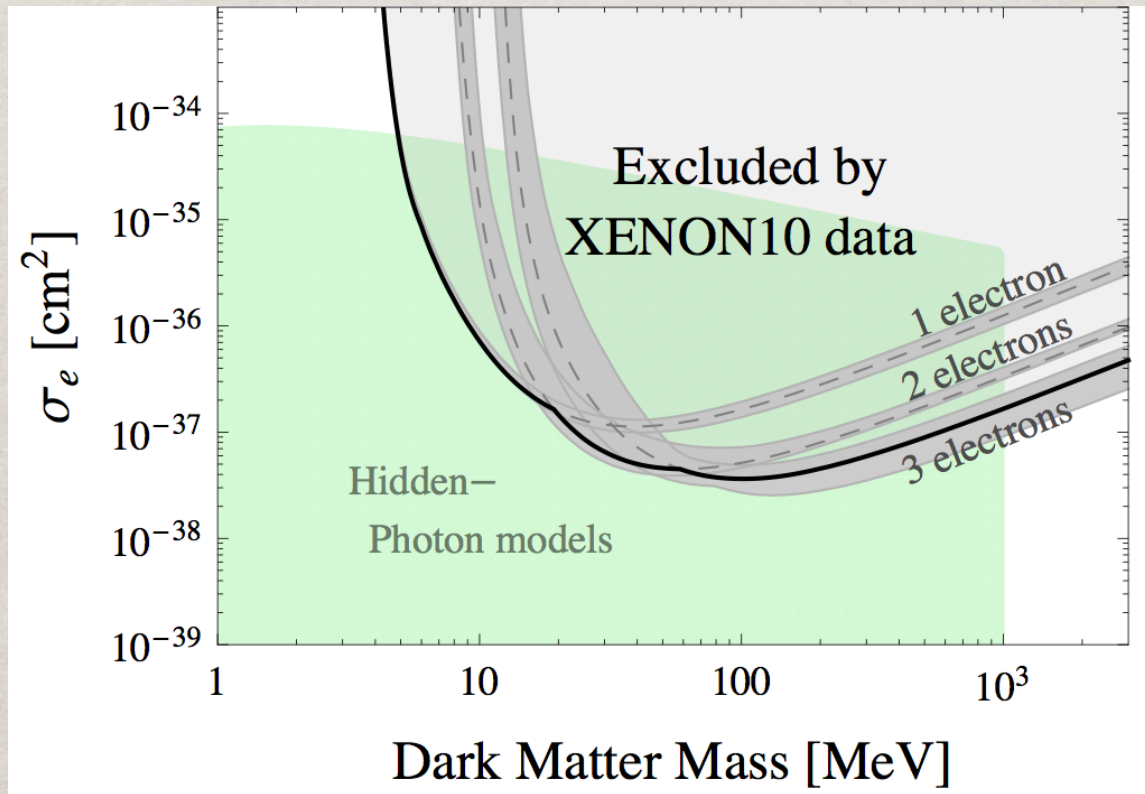
## 5 Classes of Limits





# DIRECT DETECTION

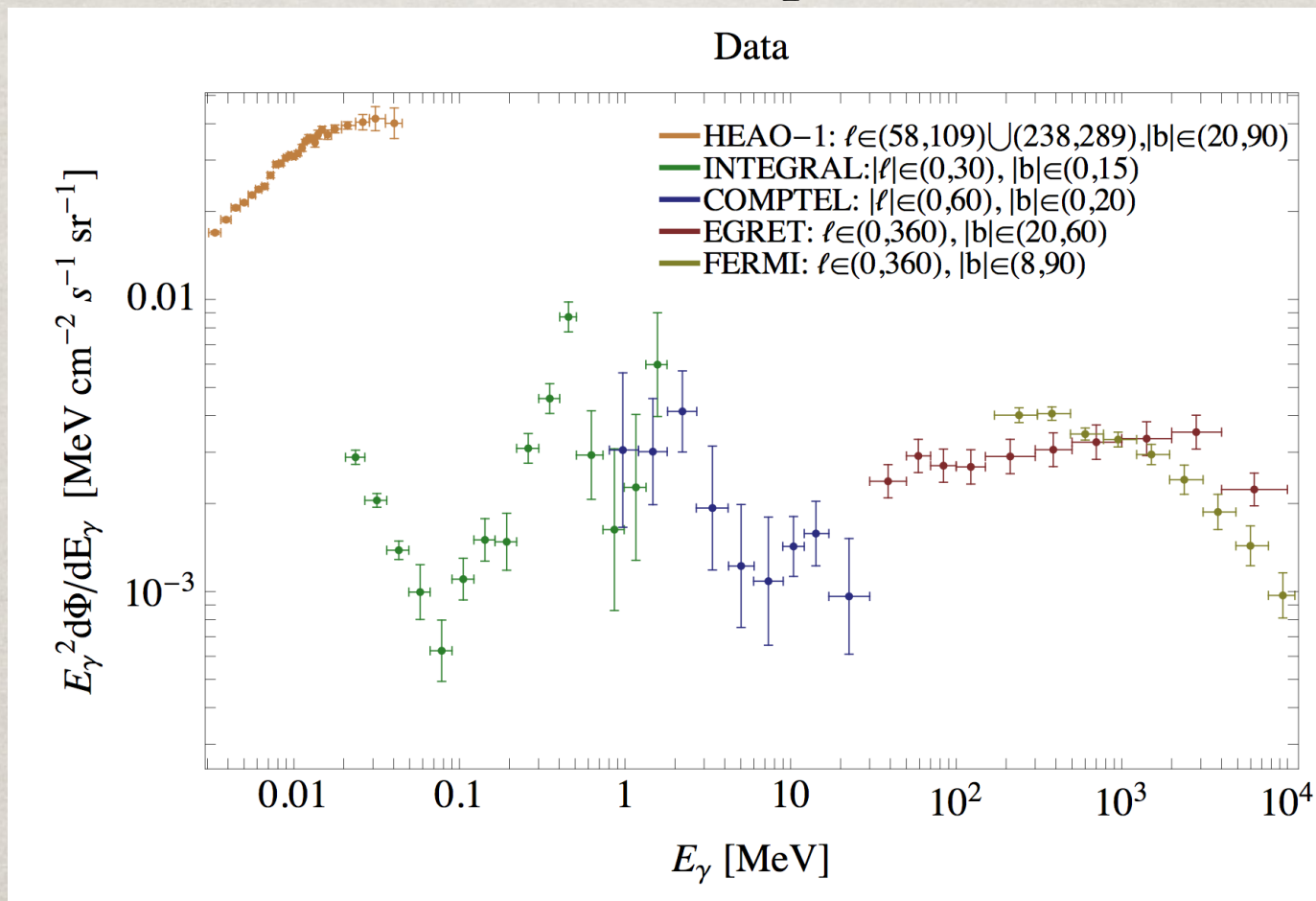
Nucleon scattering kinematically suppressed for  $m_{\text{dm}} < 5 \text{ GeV}$ , better to scatter off electrons



# INDIRECT DETECTION

## Cosmic Ray Flux Provides Limits

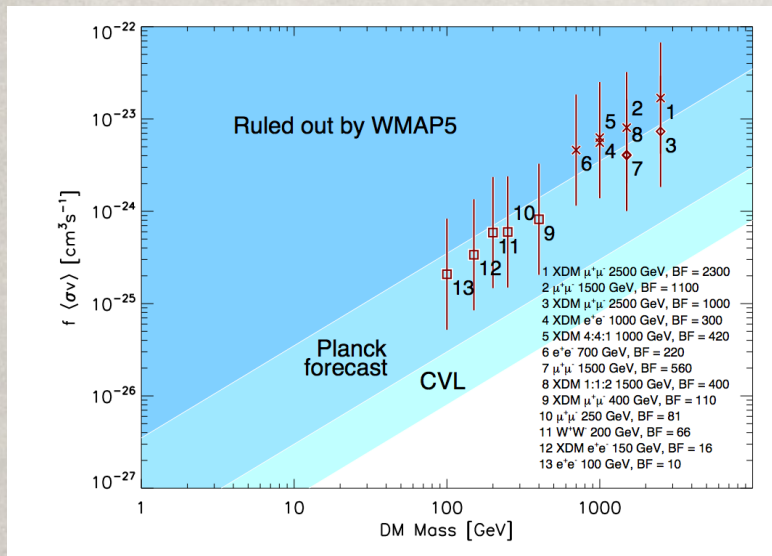
EGRET & COMPTEL provide best limits





# COSMOLOGICAL SEARCHES

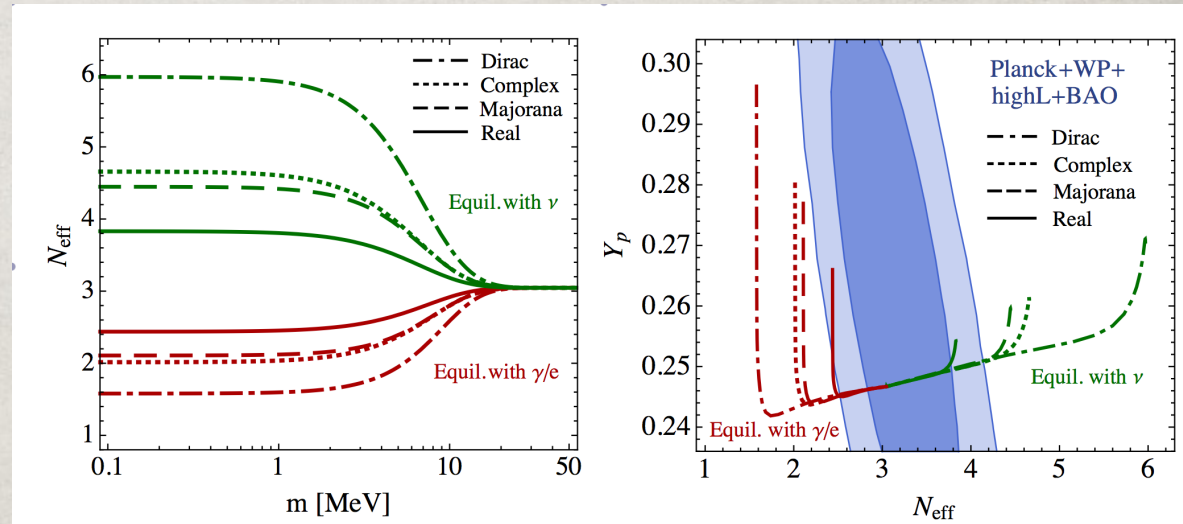
## CMB Distortion



Slatyer, Padmanabhan, Finkbeiner 0906.1197

Late DM annihilations  
add energy into CMB

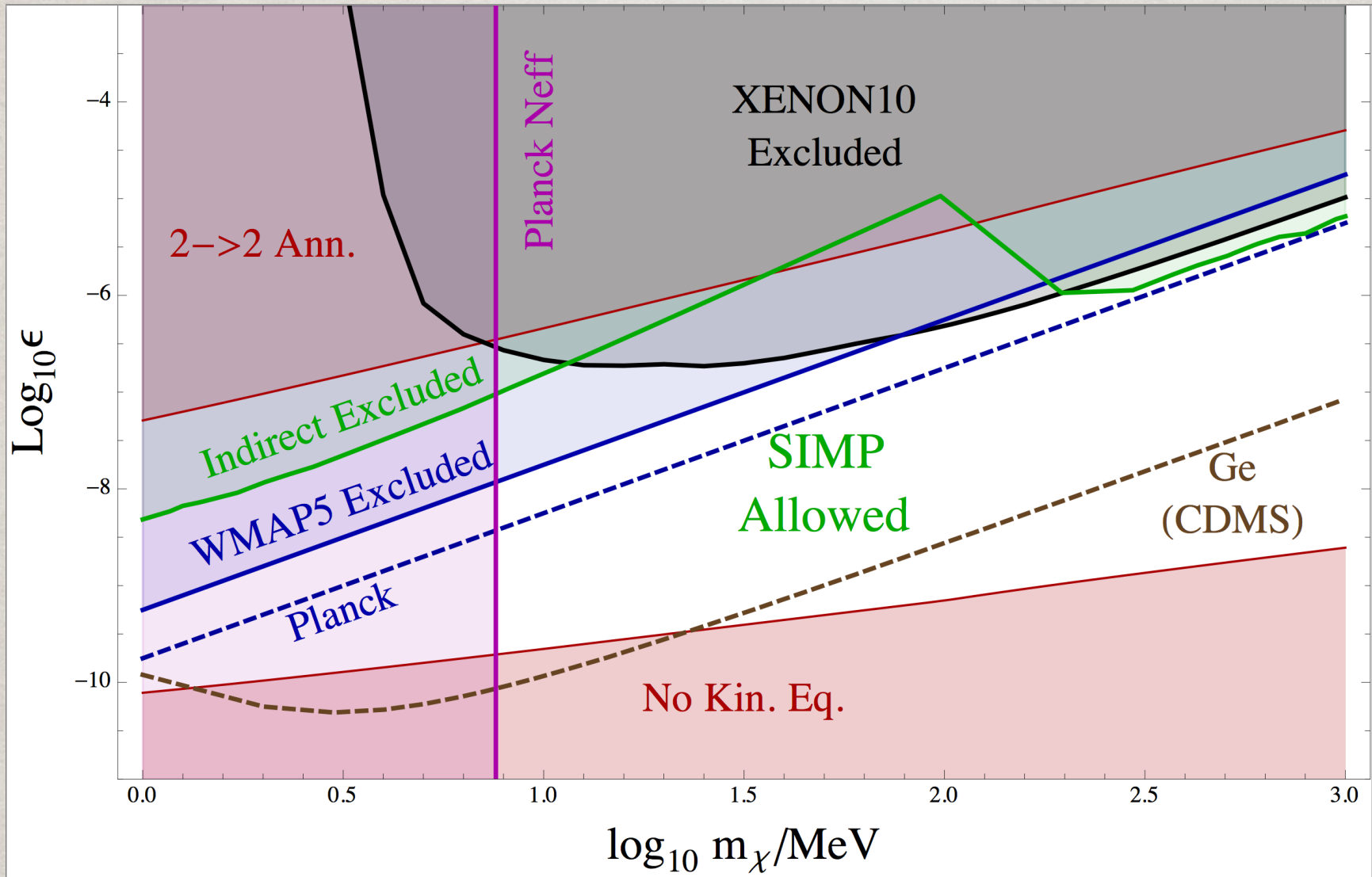
## $N_{\nu \text{ eff}}$ Modification



Boehm, Dolan, McCabe 1303.6270

If in equilibrium with  
QED sector beneath  $\nu$ -freeze out  
 $N_{\nu \text{ eff}}$  will be modified

# COMBINED LIMITS





# SELF INTERACTION

Long standing structure formation problem

Cored DM Profiles & Missing Satellite (or now TBTF)

Recent analyses showed DM self-interaction of

$$\frac{\sigma}{m} \sim 0.2 \frac{\text{barn}}{\text{GeV}} \sim 500 \text{ GeV}^{-3} \quad \text{can solve problem}$$

and allowed by Galactic Shape analysis and Bullet Cluster bounds

Strong-Scale Cross Sections!

Just Perfect!

$$\frac{\sigma_{\text{int}}}{m_{\text{dm}}} \sim \frac{\alpha^2}{m_{\text{dm}}} \sim 500 \frac{1 \text{ GeV}}{m_{\text{dm}}}$$



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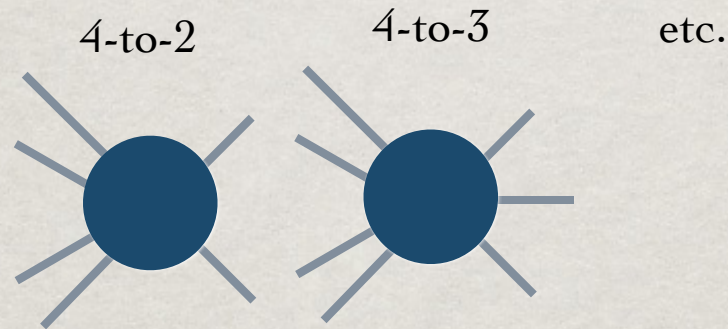
\* T H E S E A R C H F O R S I M P S

\* O U T L O O K



# HIGHER POINT INTERACTIONS

What about higher point interactions?

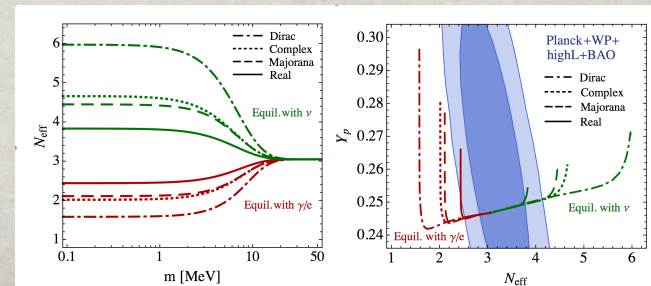


(only 3-to-2 will be viable)

6 point interactions automatically conserve  $\mathbb{Z}_2$  symmetry

$$m_{\text{dm}} \simeq \alpha \left( T_{\text{eq}}^{n-1} M_{\text{Pl}} \right)^{\frac{1}{n}} \quad \langle \sigma_{n \rightarrow 2\nu} \rangle = \frac{\alpha^n}{m^{2+3n}}$$

$n=4$  corresponds to 10 keV  
dead by  $N_{\nu \text{ eff}}$



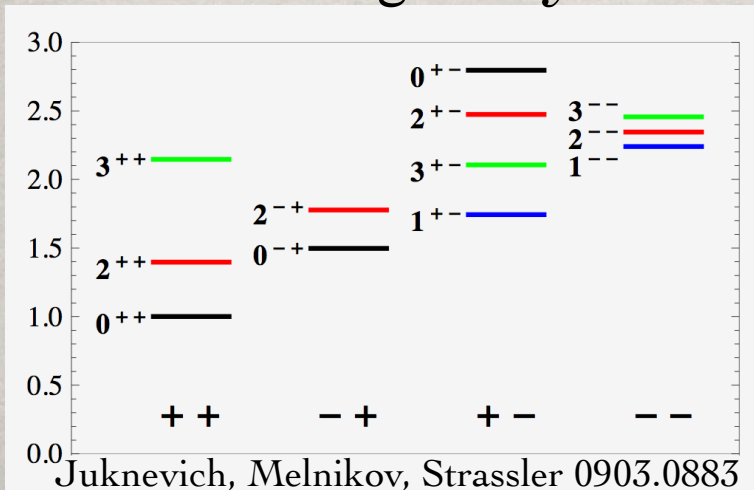
# HIDDEN GLUEBALL DM

Hidden pure SU(N) sector that confines

$$\mathcal{L}_{\text{dark}} \sim G_{\mu\nu}^2 + (\partial a)^2 + m_a^2 a^2 + \frac{a}{f} G\tilde{G} + \frac{a}{f'} F\tilde{F}$$

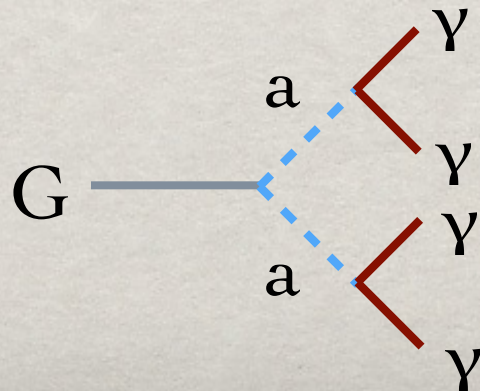
Confines at  $\Lambda_{\text{dark}}$

O(10) states stable to strong decays



Axion heavier than glueball  $\epsilon \sim \frac{\Lambda_{\text{dark}}^4}{f f' m_a^2}$

Scalar Glueball decays through 4 body



$\sim \epsilon^4$  borderline  
 $10^{25}$  seconds

electrons safer



# OUTLOOK

SIMPs offer a new window to DM

Points to different physical scales

Truly a miracle that it isn't ruled out

Lighter DM that self-interacts

Discovery of the particle physics of DM  
could be through long standing structure formation problems

New model building challenges

Simplest models still need to be discovered