



# Precision Measurement of the W Boson Mass at CDF

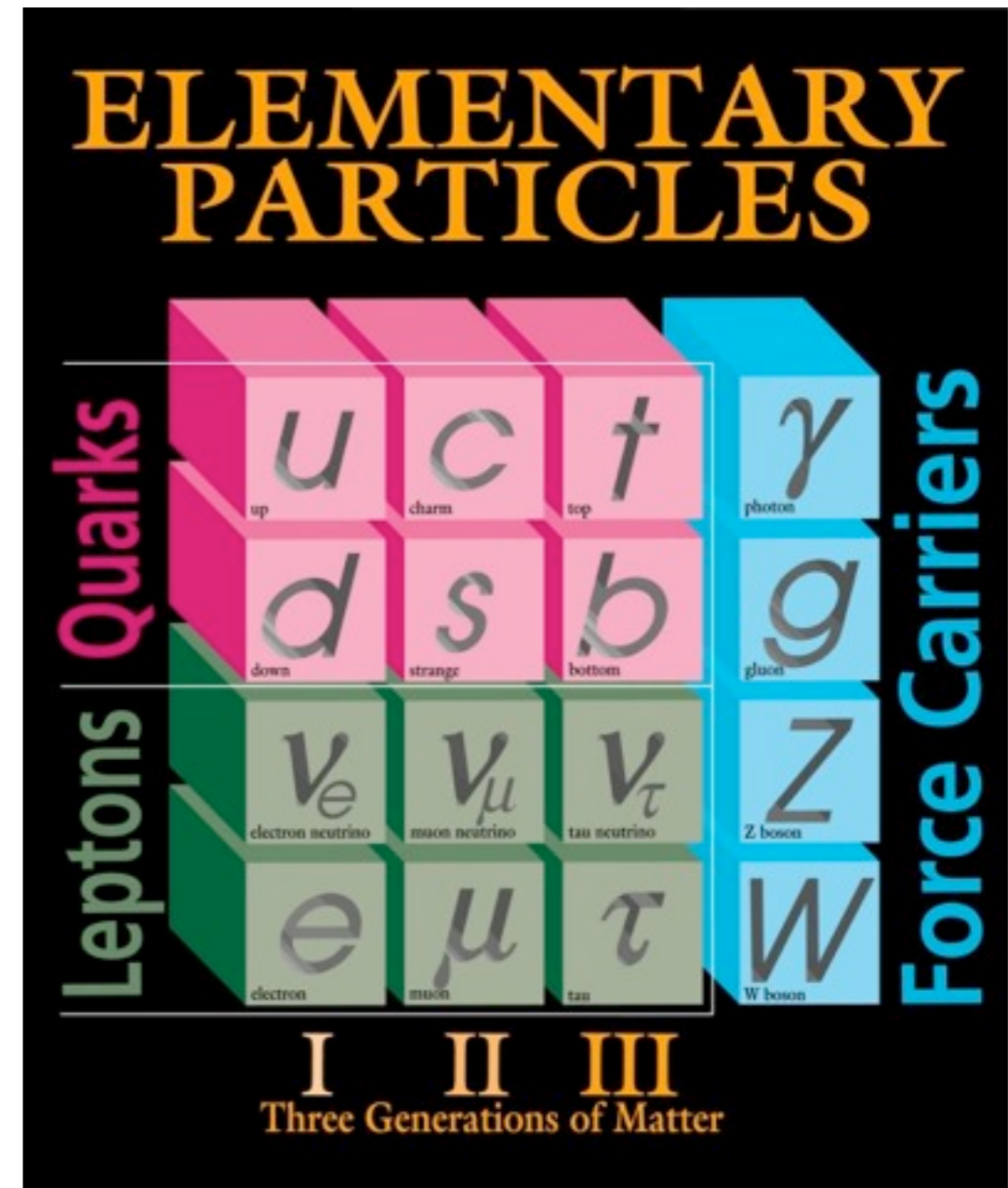
Bodhitha Jayatilaka  
*Duke University*

High Energy Physics Seminar  
University of California, Davis

June 4, 2012

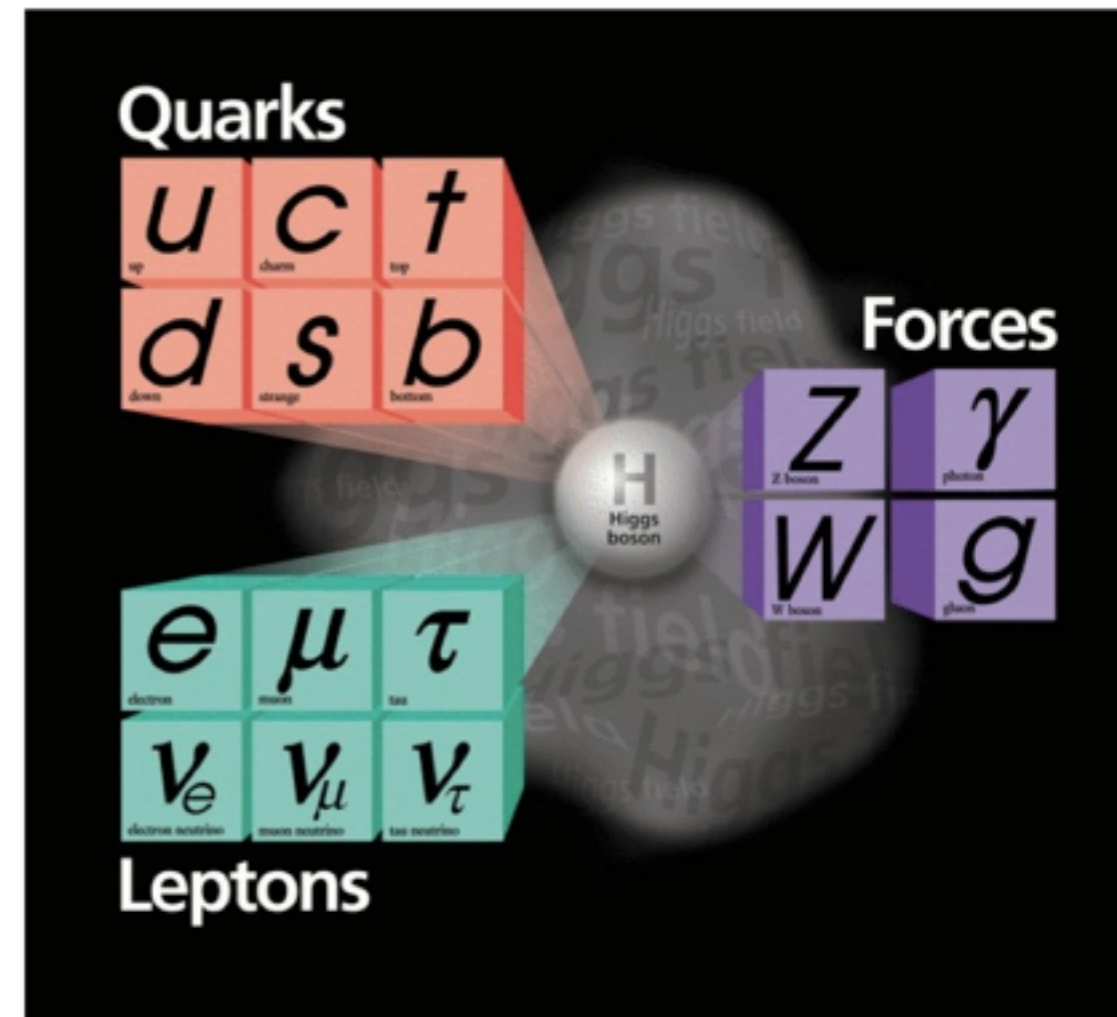
# Motivation: a picture to start with

- The standard model
  - Describes known particles and interactions
  - Does not (verifiably) describe
    - Spontaneous symmetry breaking of  $U(1) \times SU(2)$
    - Fermion masses



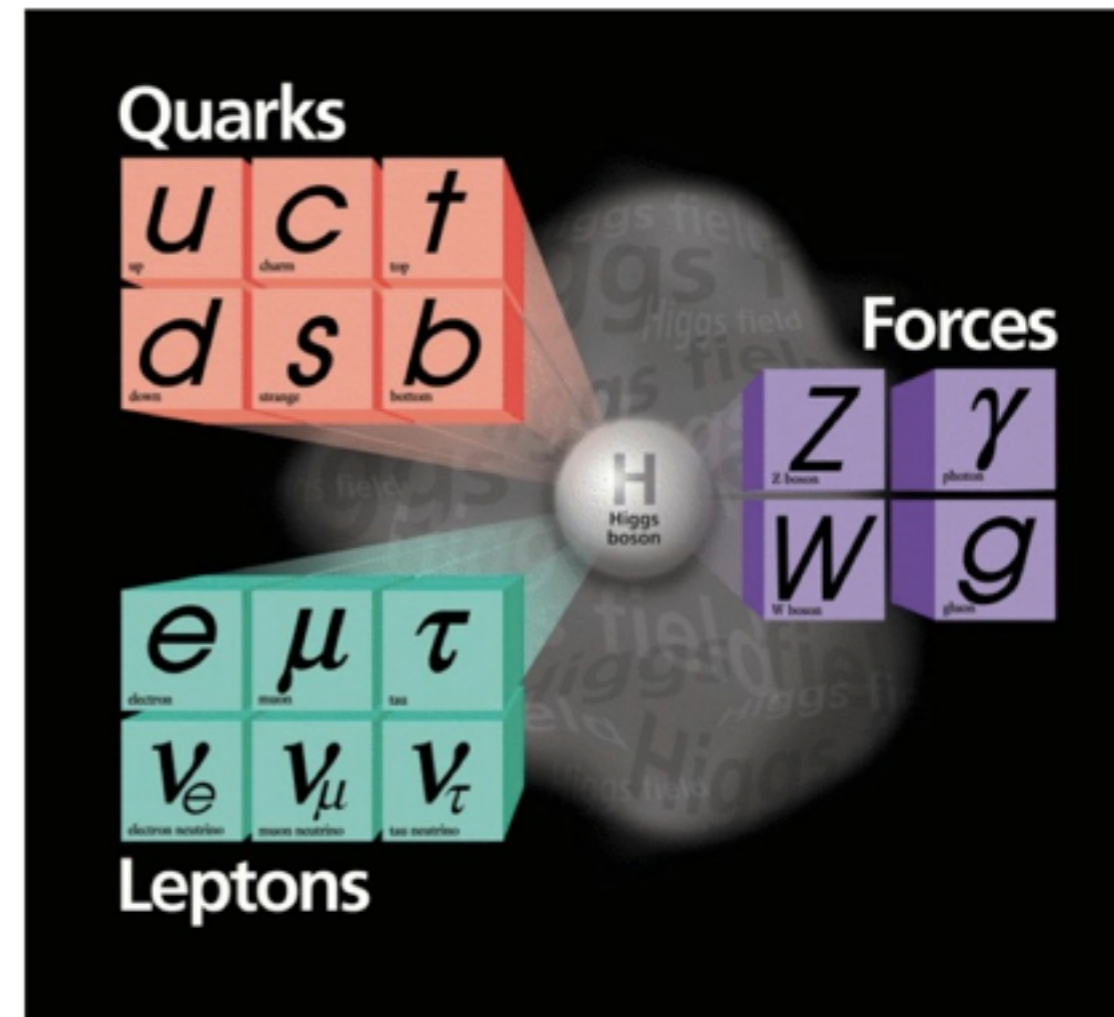
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- Simple explanation: **Higgs mechanism**
  - Explains EWSB and fermion masses
  - Physical manifestation of Higgs boson



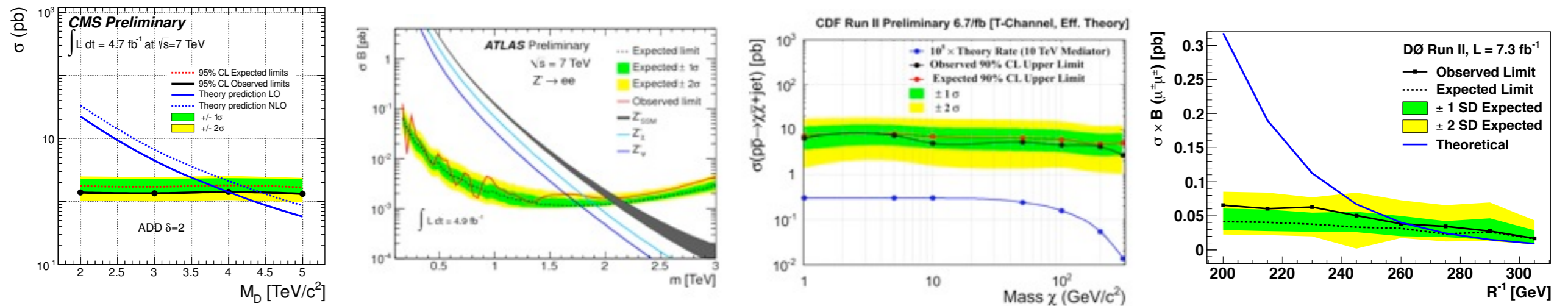
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- Alternatively: ?????

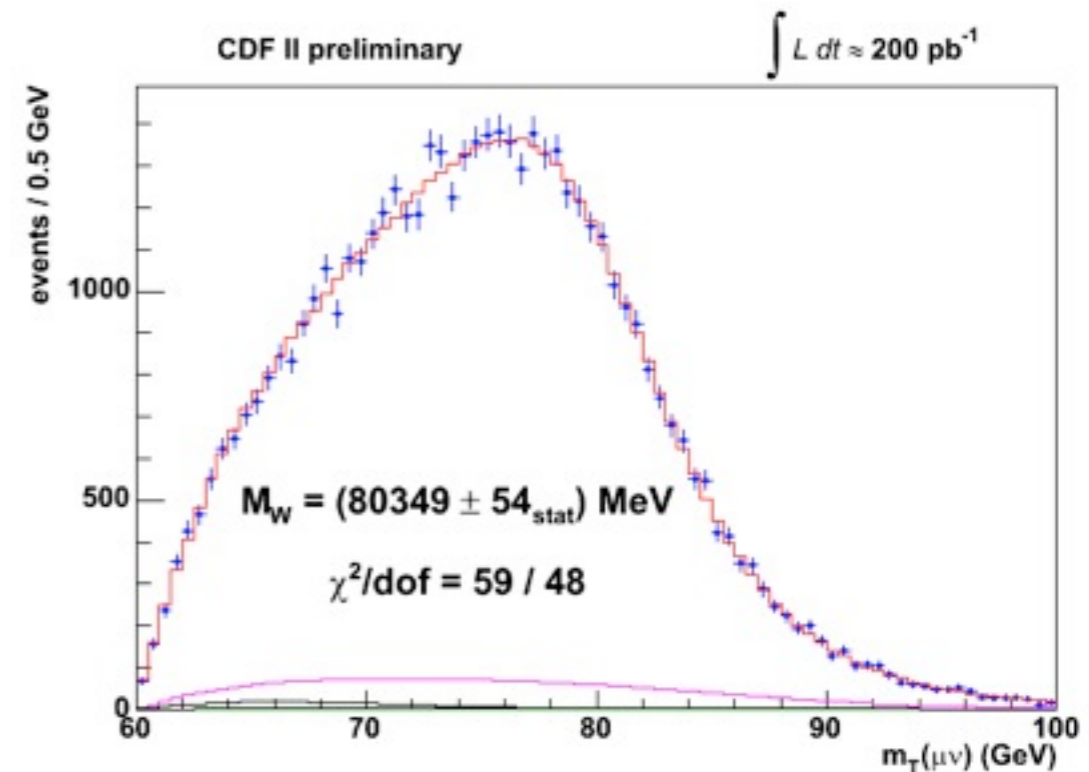
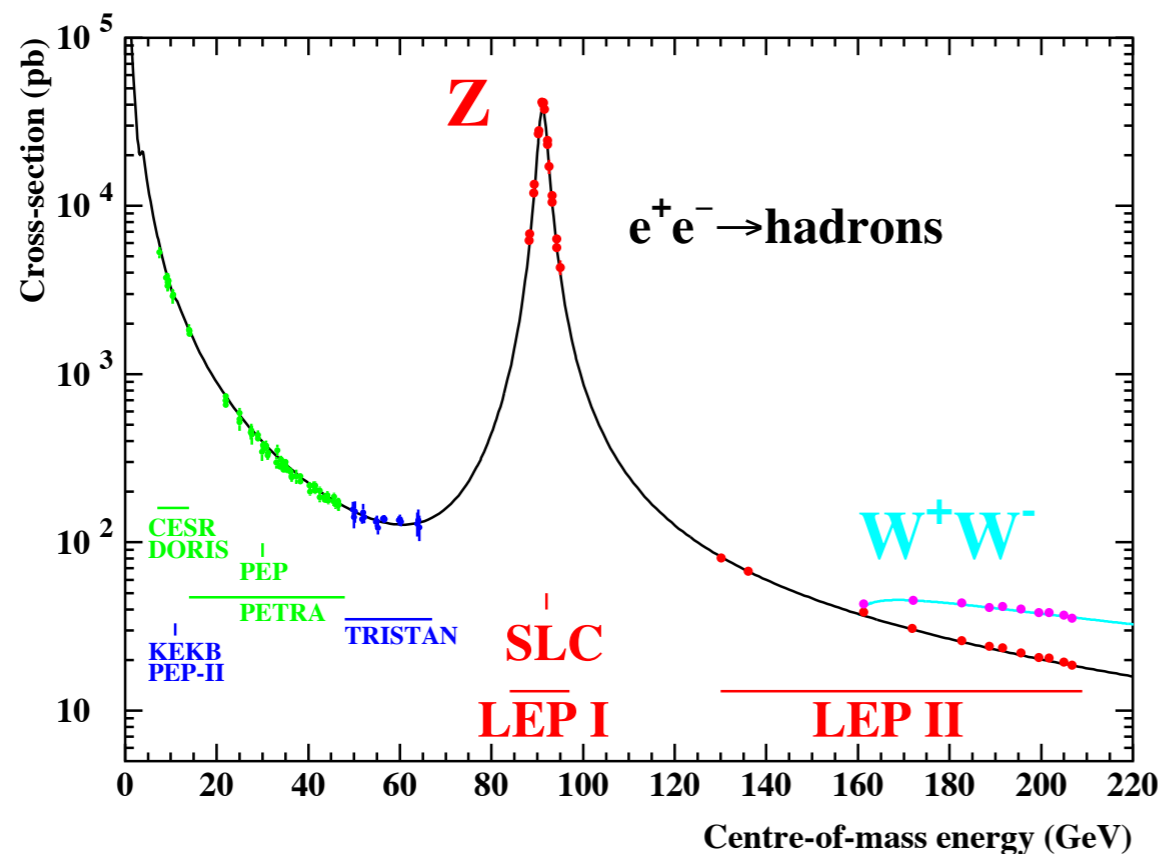


# Cracking/checking the picture with colliders

## 1. Direct searches. e.g.:



## 2. Precision measurements



# What the W mass tells us

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- Electroweak sector of the standard model (SM) is constrained by

$$G_F = 1.16637(1) \times 10^{-5} \text{ GeV}^{-2} \quad \alpha_{EM}(Q^2 = M_Z^2) = 1/127.918(18)$$

$$m_Z = 91.1876(21) \text{ GeV}/c^2$$

- These inputs give a prediction of  $m_W$

$$m_W^2 = \frac{\pi \alpha_{em}}{\sqrt{2} G_F \sin^2 \theta_W (1 - \Delta r)} \quad \sin^2 \theta_W = 1 - \frac{m_W^2}{m_Z^2}$$

- Radiative corrections  $\Delta r$  dominated by top and Higgs loops

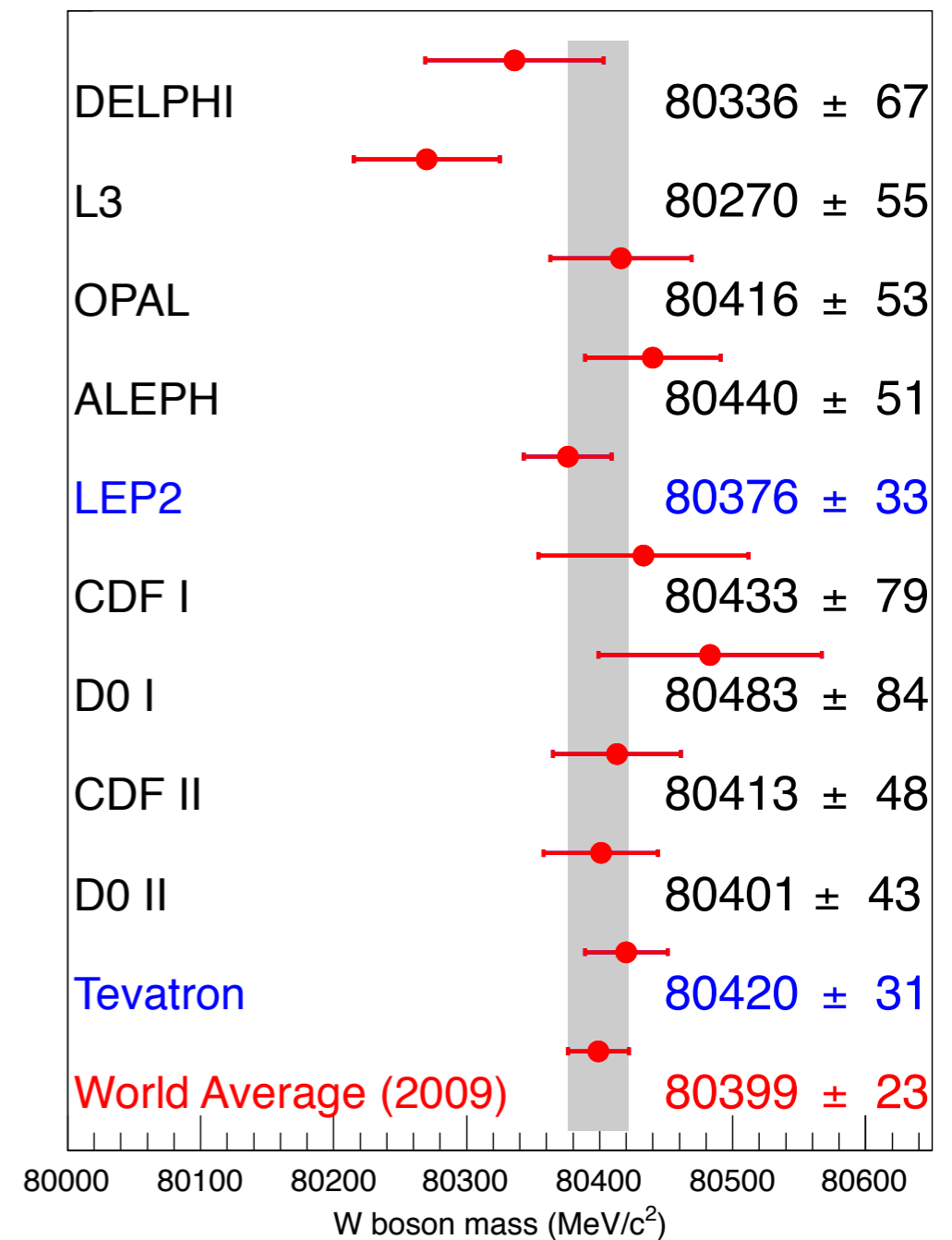


- Precision measurements of  $m_W$  and  $m_{top}$  constrain SM Higgs mass

*Where should the Higgs be?*

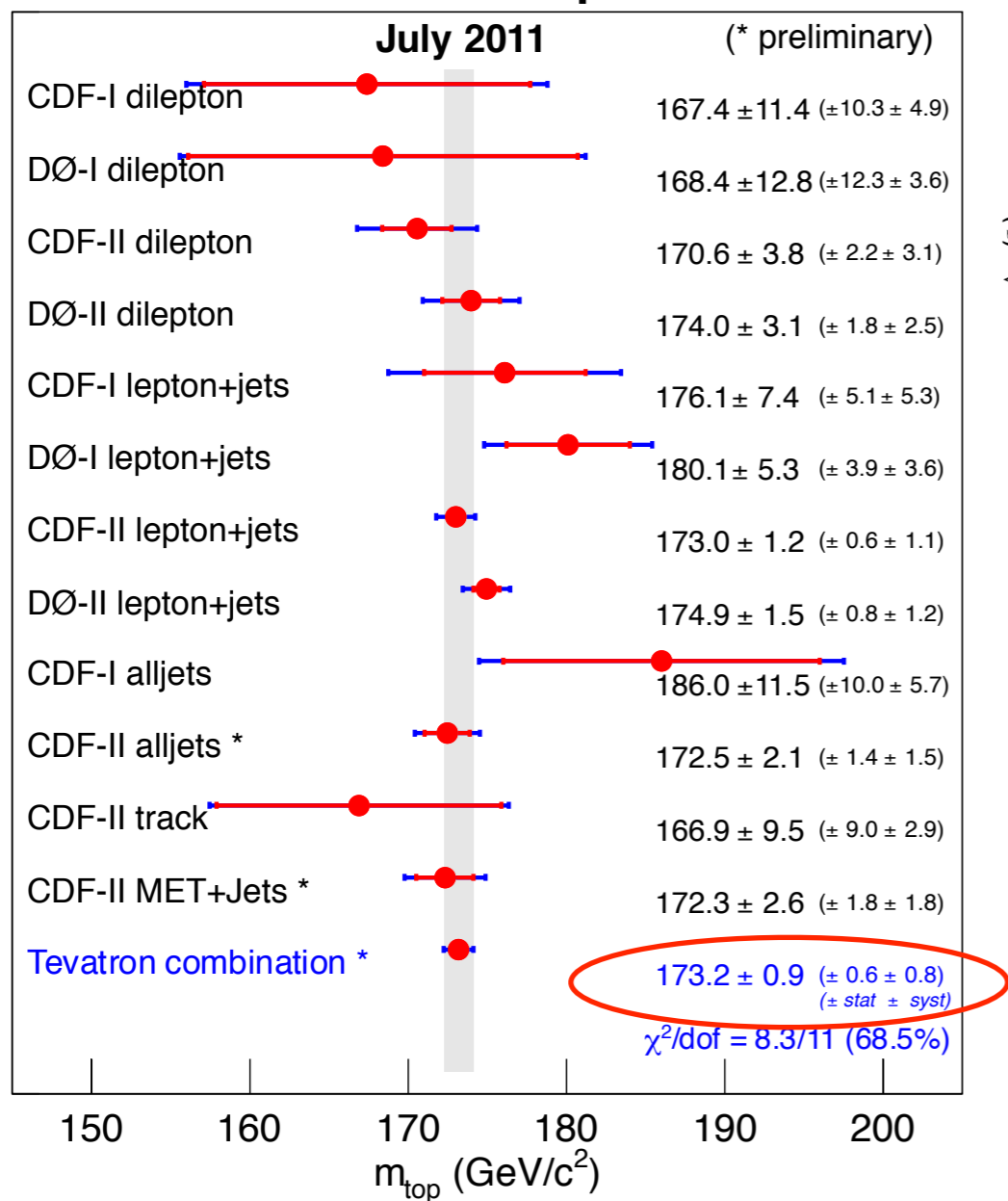
# Measurements of $M_W$

- State-of-the-art (Jan 2012)
  - DØ  $M_W=80401\pm 43$  MeV [1 fb<sup>-1</sup>, e]
  - PRL 103:141801 (2009)*
  - CDF  $M_W=80413\pm 48$  MeV [200 pb<sup>-1</sup>, e+μ]
  - PRL 99:151801 (2007)*
  - PRD 77:112001 (2008)*
  - Combining with LEP  $\Delta M_W = 23$  MeV
- *Achieved:* exceed precision of e<sup>+</sup>e<sup>-</sup> machine measurements with hadron collider
- *Goal:* match precision of all previous measurements with single CDF measurement

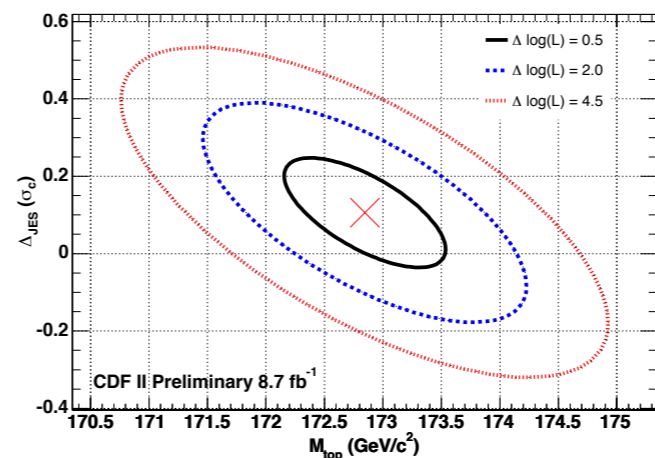


# The top quark mass

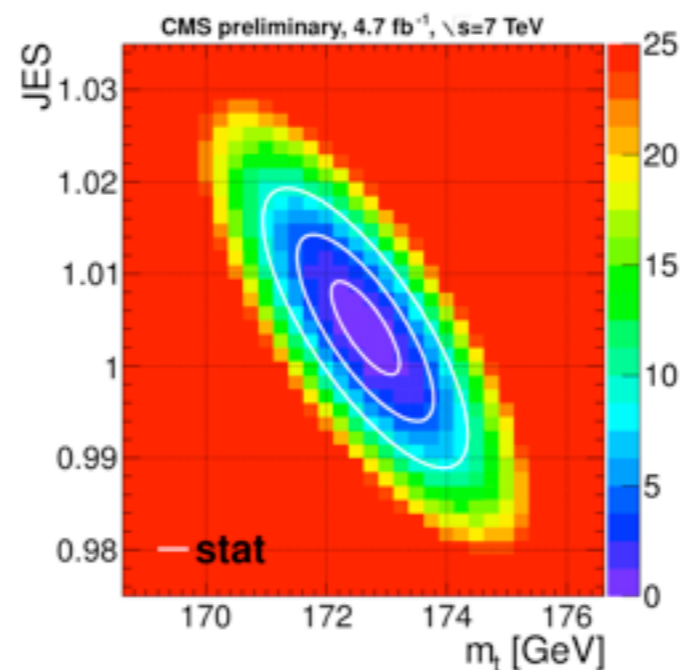
## Mass of the Top Quark



Combination **does not (yet) include**



Single best measurement  
 $m_{top} = 172.8 \pm 1.1$  GeV [CDF]

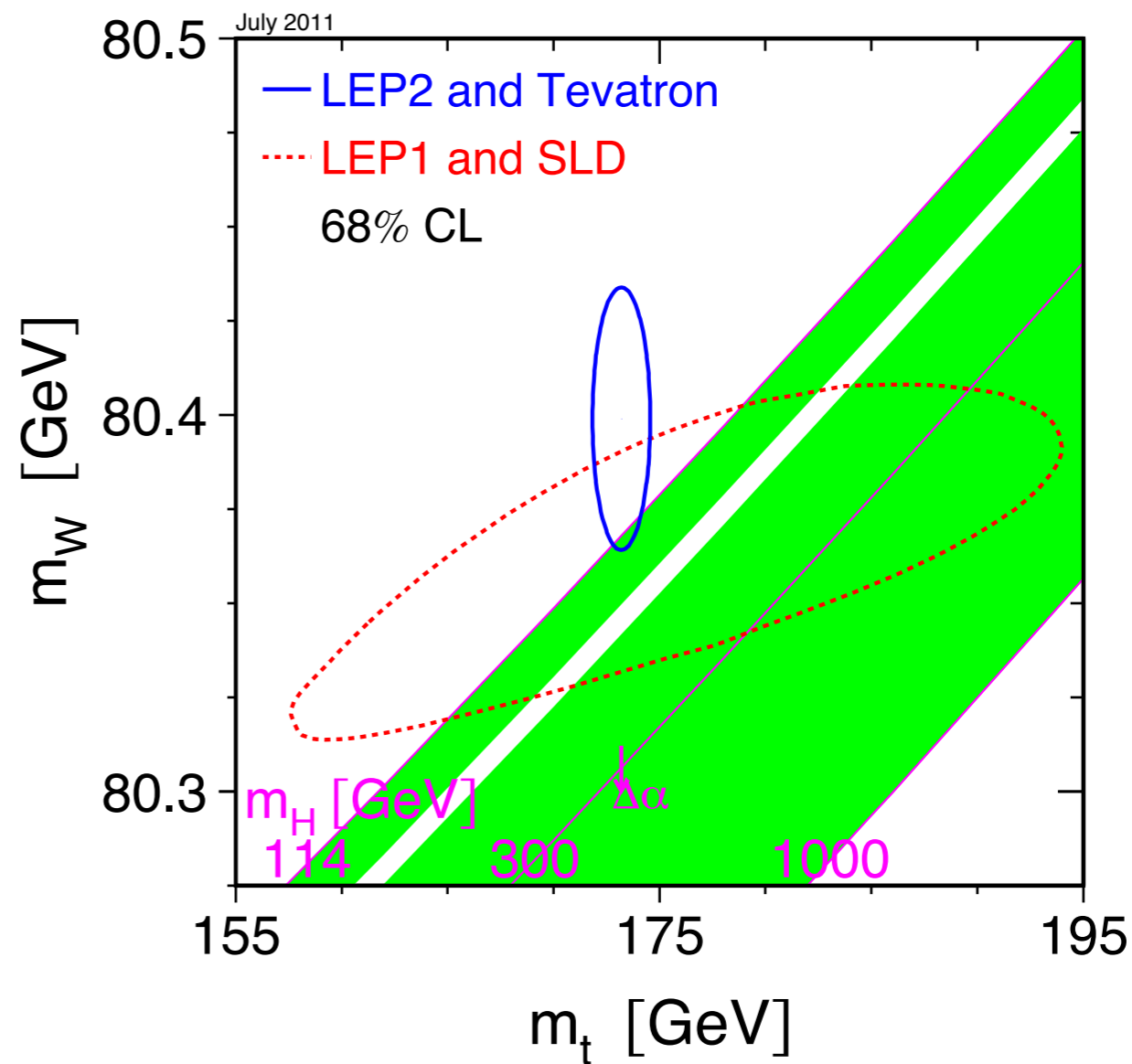
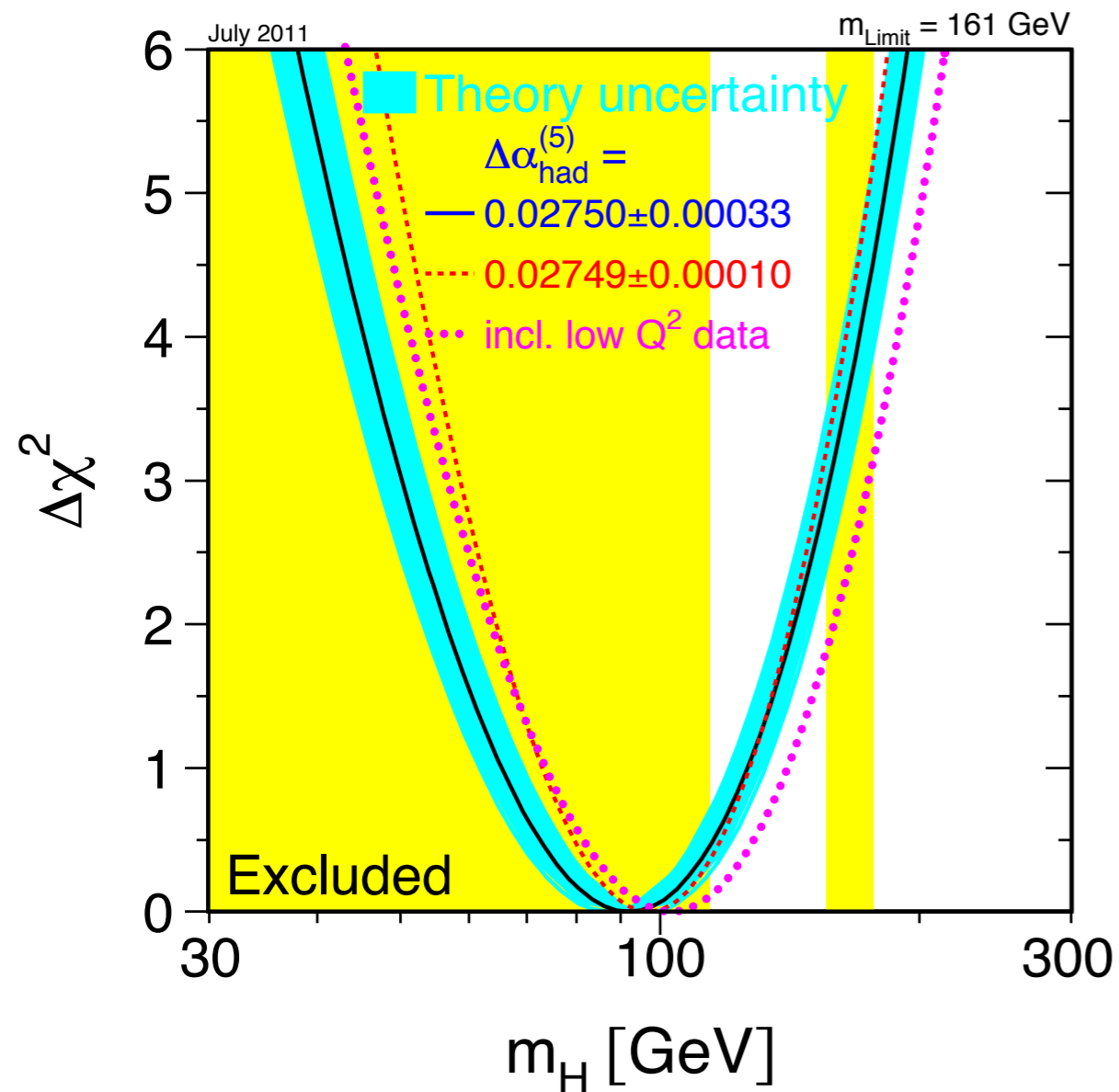


Impressive results from LHC  
 e.g. (single best LHC meas.)  
 $m_{top} = 172.6 \pm 1.3$  GeV [CMS]

- $m_{top} = 173.2 \pm 0.9$  GeV
  - Equivalent to  $\Delta m_W = 6$  MeV on  $m_H$  fit
  - $m_W$  is limiting factor on  $m_H$  prediction!



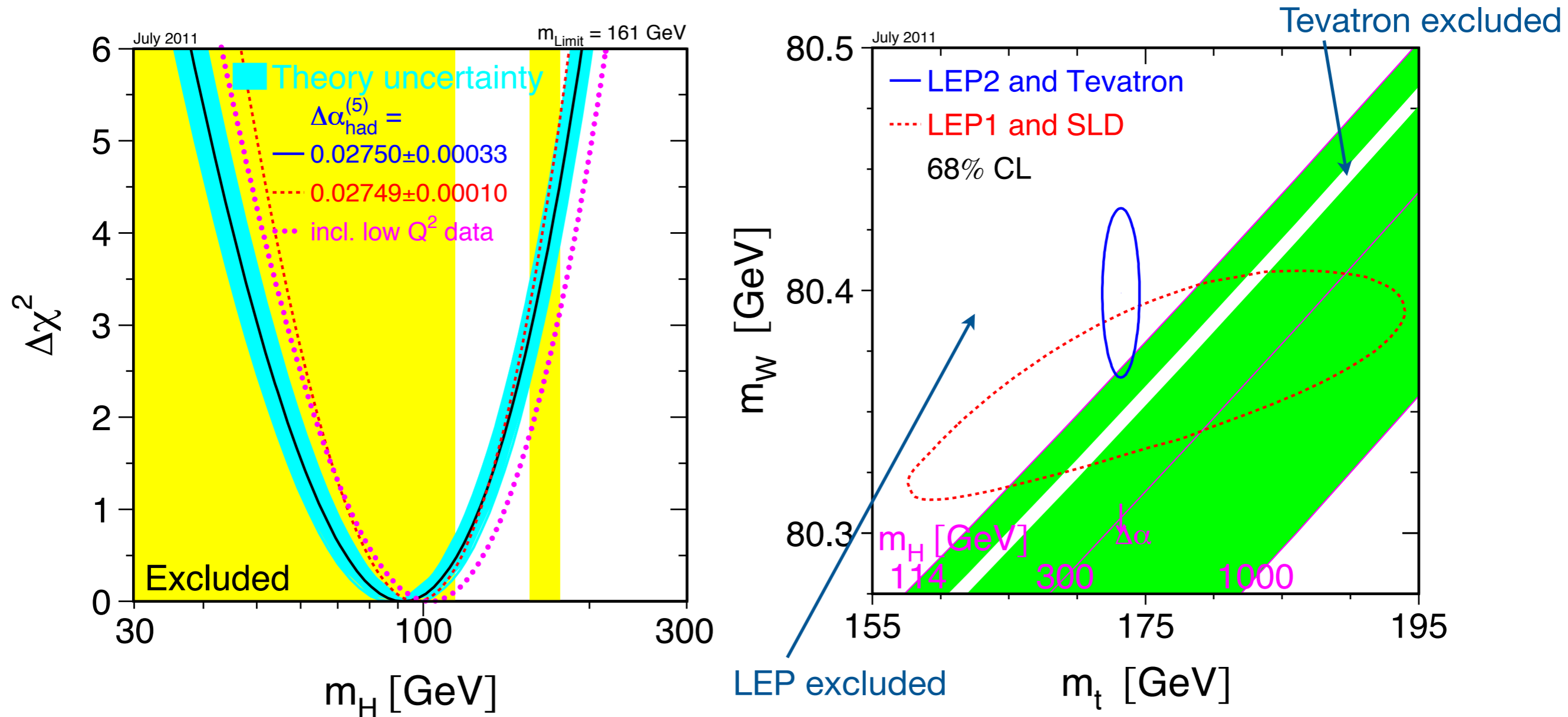
# Putting it together



As of July 2011:  
 $m_H = 92^{+34}_{-26}$  GeV  
 $m_H < 161$  GeV @95% CL

Fits and plots from **LEPEWWG**

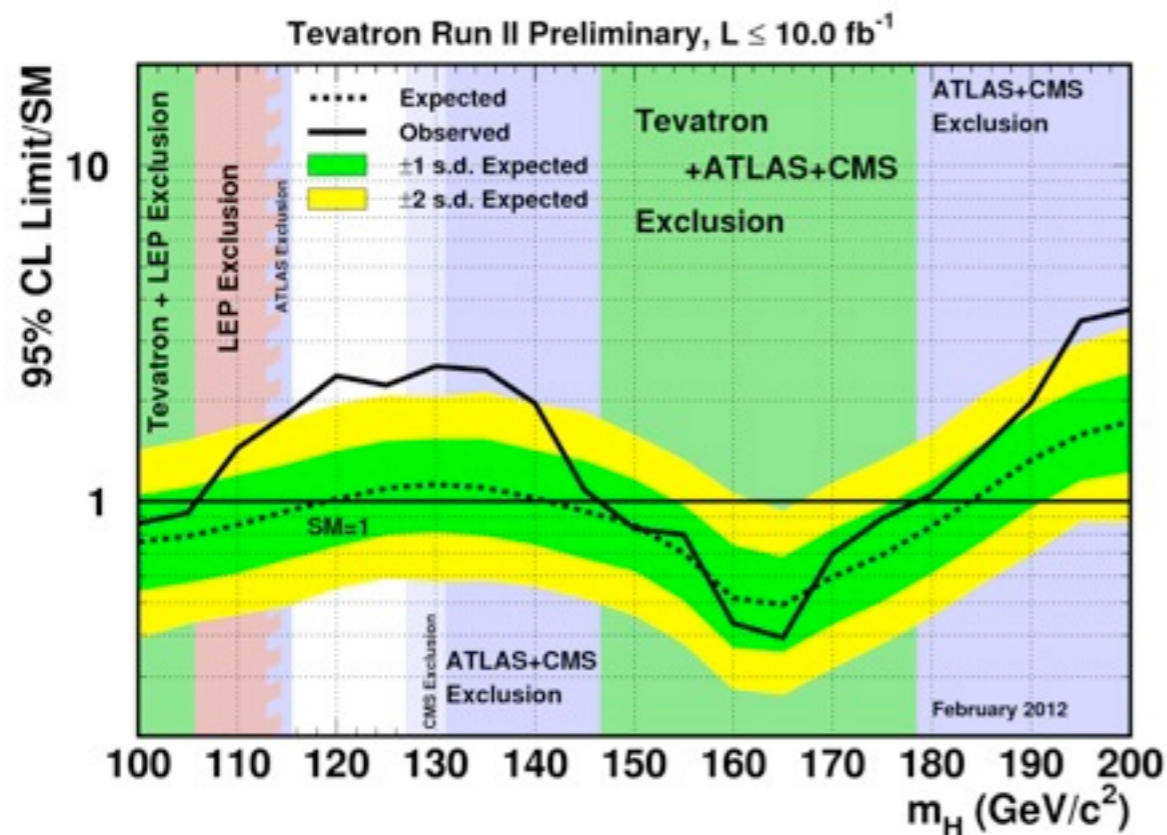
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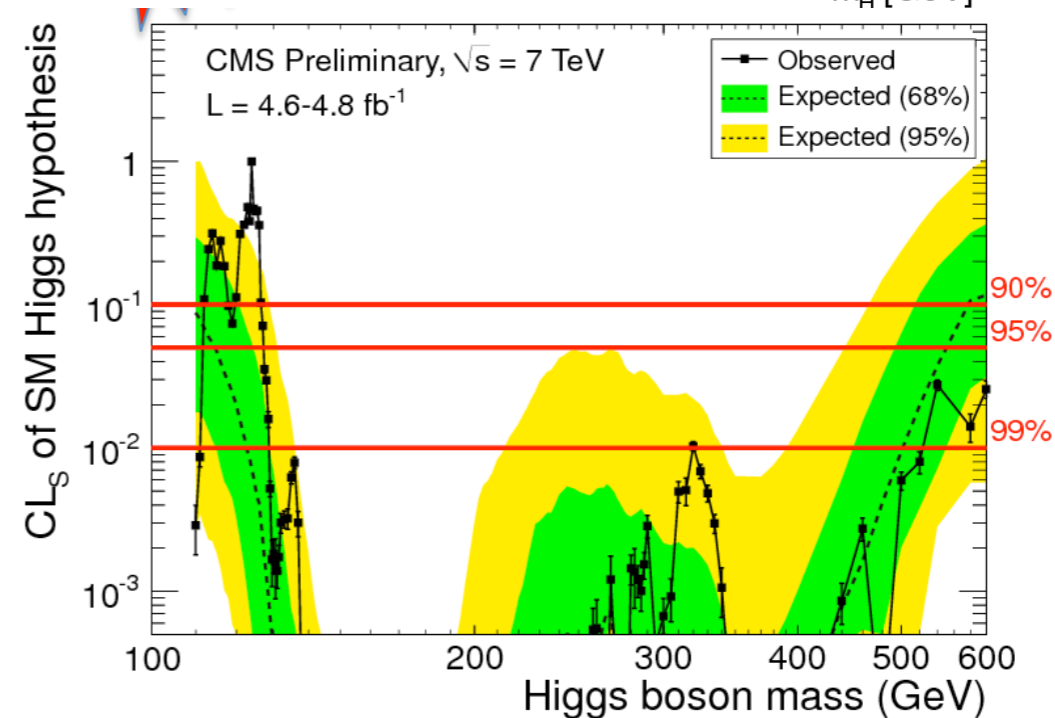
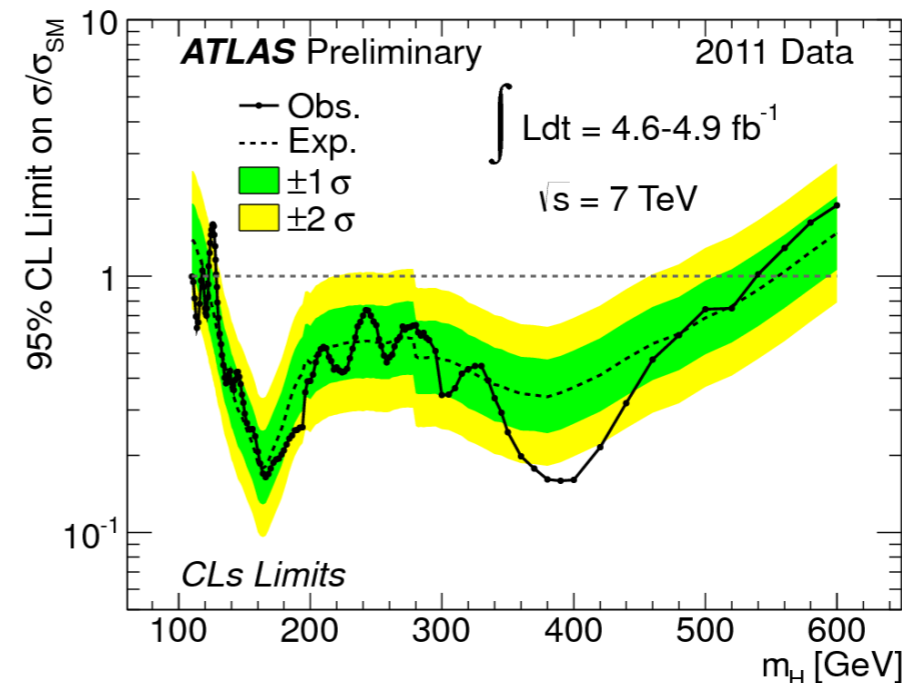
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Fits and plots from **LEPEWWG**

# Since then...



Moriond 2012

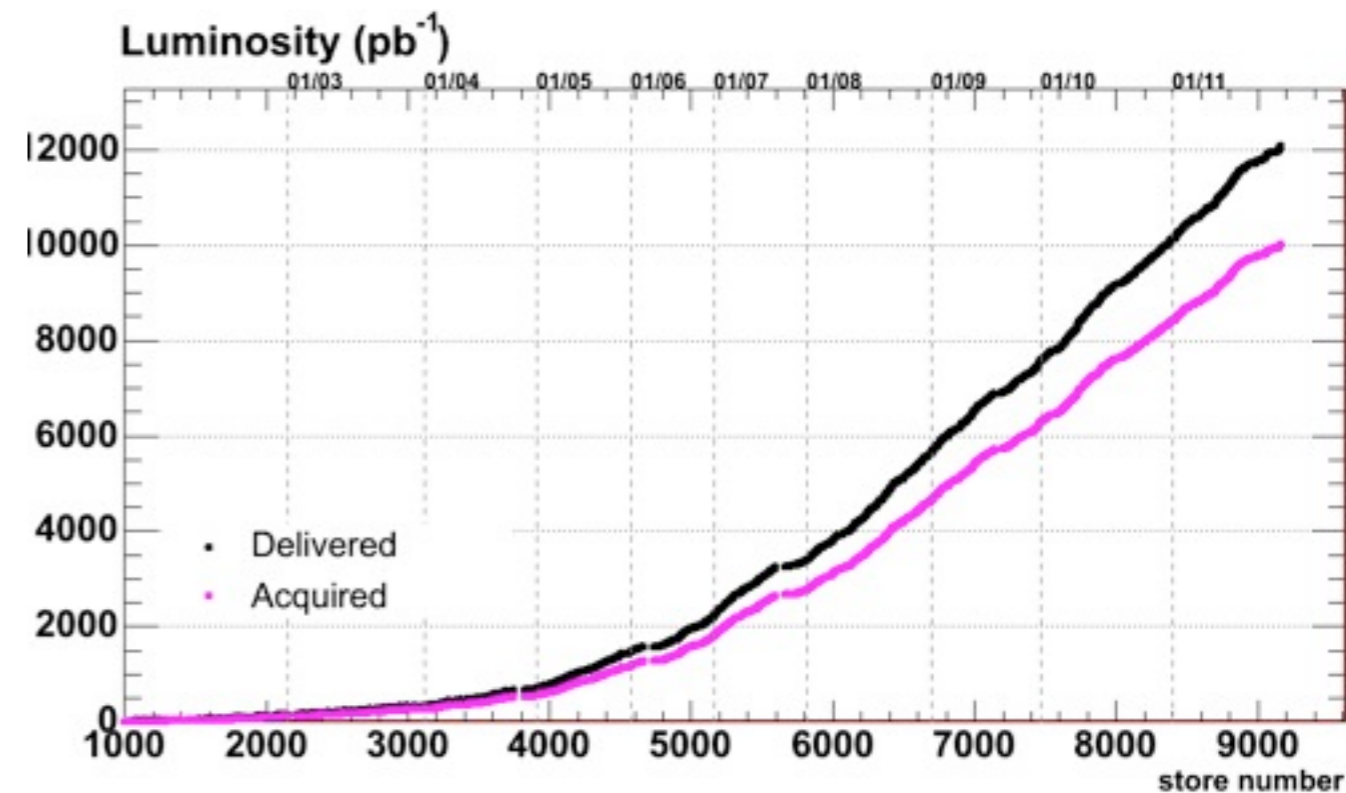


- Direct searches at the LHC and Tevatron restrict SM Higgs to narrow range
  - $m_H \sim 118-127 \text{ GeV}$

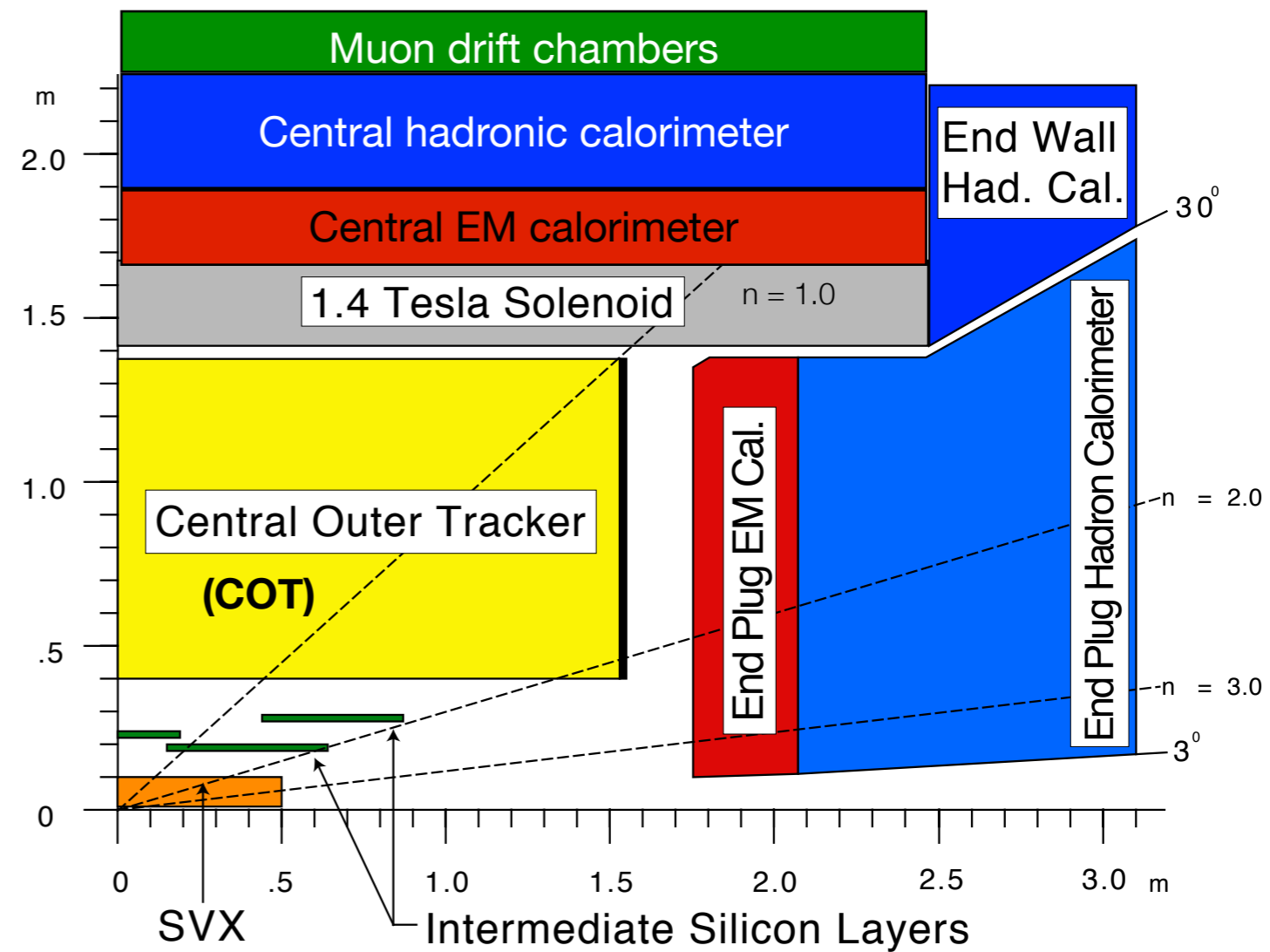
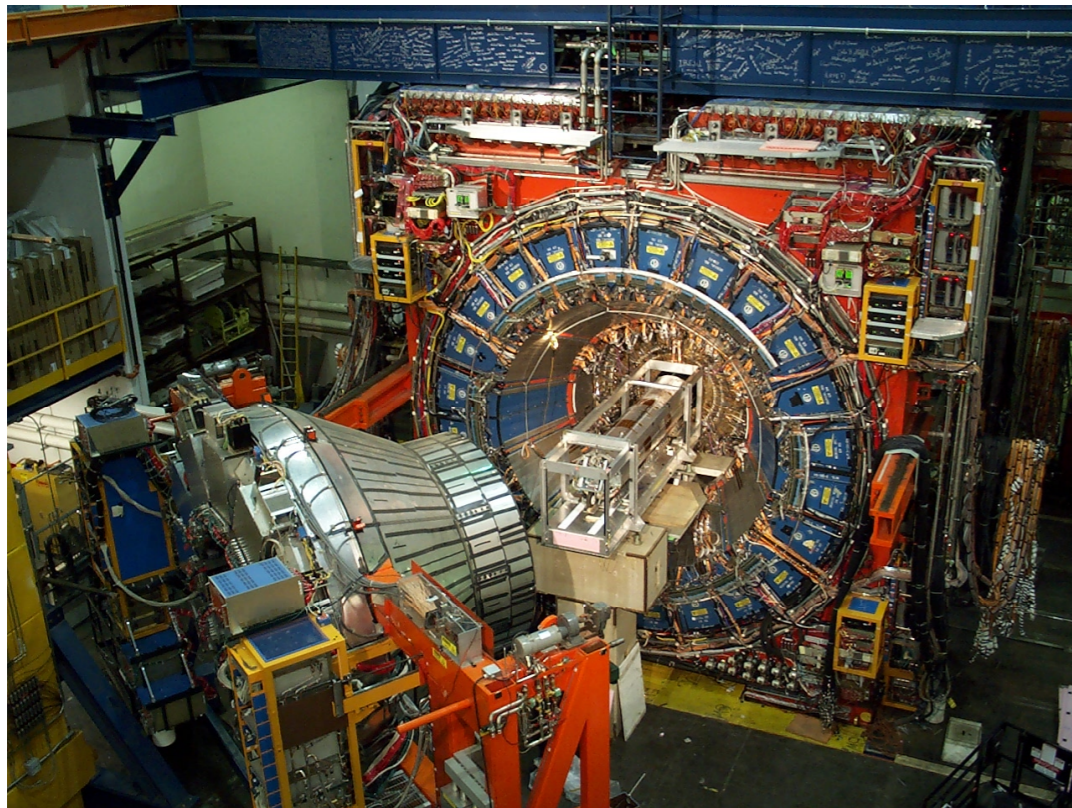
Analysis strategy

# The Tevatron at Fermilab

- 1.96 TeV ppbar collider
  - Highest energy <sup>p-pbar</sup> collider in the world
  - Typical inst. lumi.:  $3 \times 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$ 
    - 2011 LHC:  $\sim 3 \times 10^{33} \text{ cm}^{-2} \text{ s}^{-1}$
  - Bunch spacing: 396 ns
    - 2011 LHC: 50 ns
- Ceased operations Sep 30, 2011
  - $\sim 12 \text{ fb}^{-1}$  delivered to CDF and DØ
- Analysis presented utilizes  $2.2 \text{ fb}^{-1}$



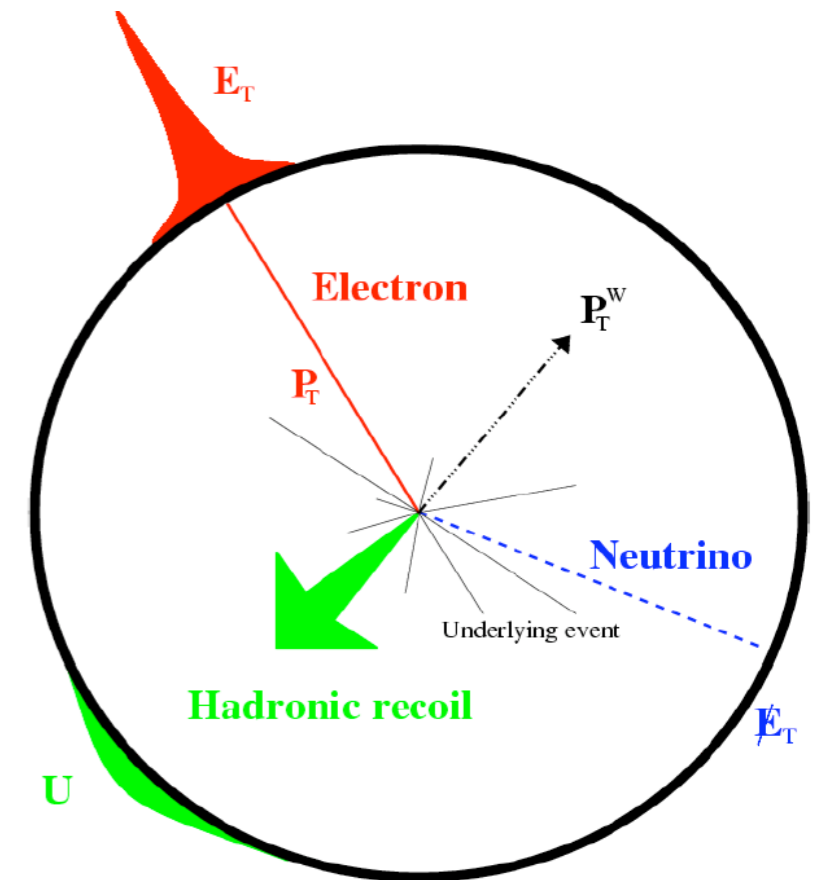
# CDF II (2001-2011)



# Precision?

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- Start with **clean, low-background** events
  - *i.e.*, no taus, no hadronic decays
- **Lepton  $p_T$**  carries most information
  - Precision achieved:  $0.01\%$
- **Hadronic recoil** affects inference of **neutrino energy**
  - Calibrate to  $\sim 0.5\%$
  - Reduce impact by requiring  $p_T(W) \ll M_W$
- Need:
  - Accurate **theoretical model**
    - Including boson  $p_T$  model and QED radiation
  - Tunable **fast simulation**
    - Parameterized detector description for study of systematic effects
  - Large data samples of well-measured states
    - Various dimuon resonances
    - $Z$  boson



# Measurement strategy (broadly speaking)

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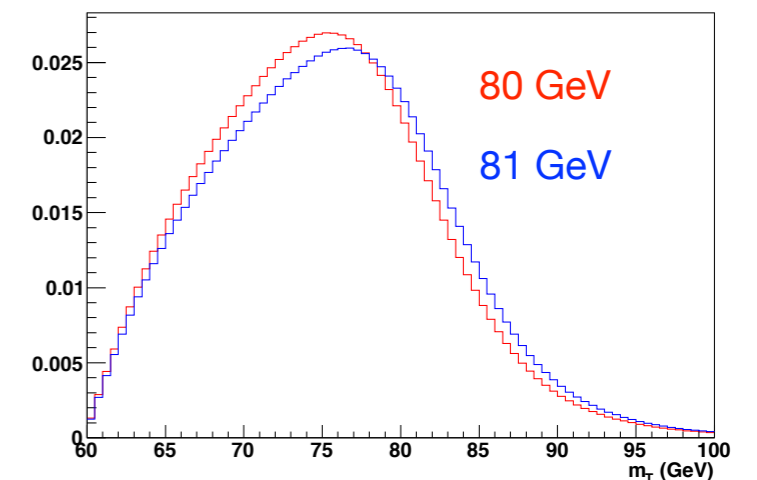
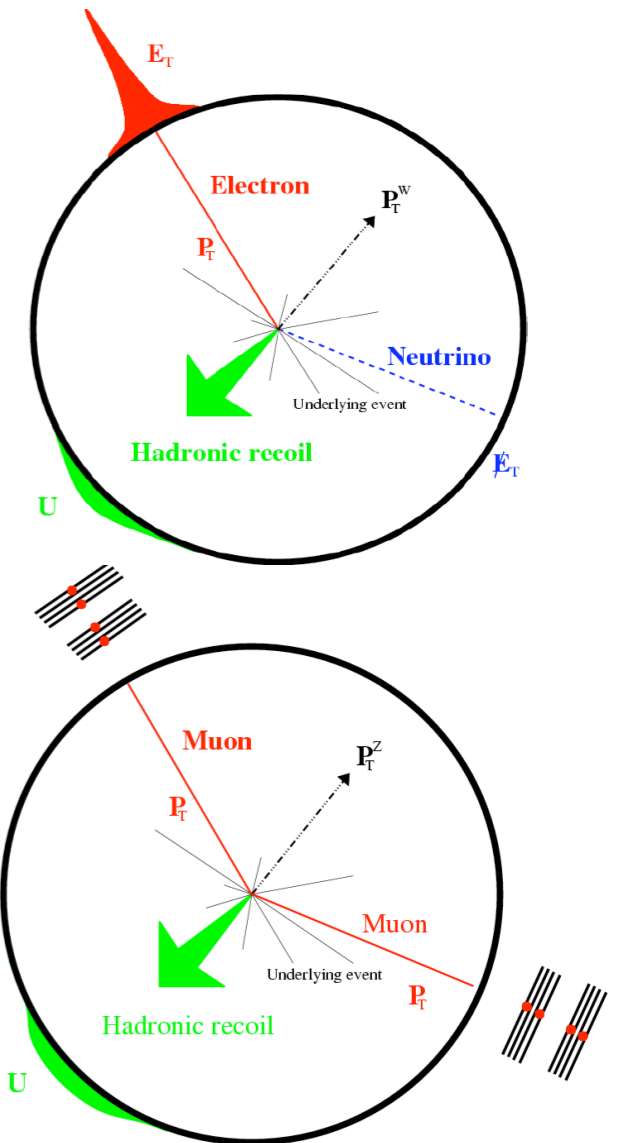
- Maximize internal constraints and cross-checks
- Why?
  1. **Robustness:** Constrain the same parameter multiple ways
  2. **Precision:** After demonstrating 1), combine independent measurements



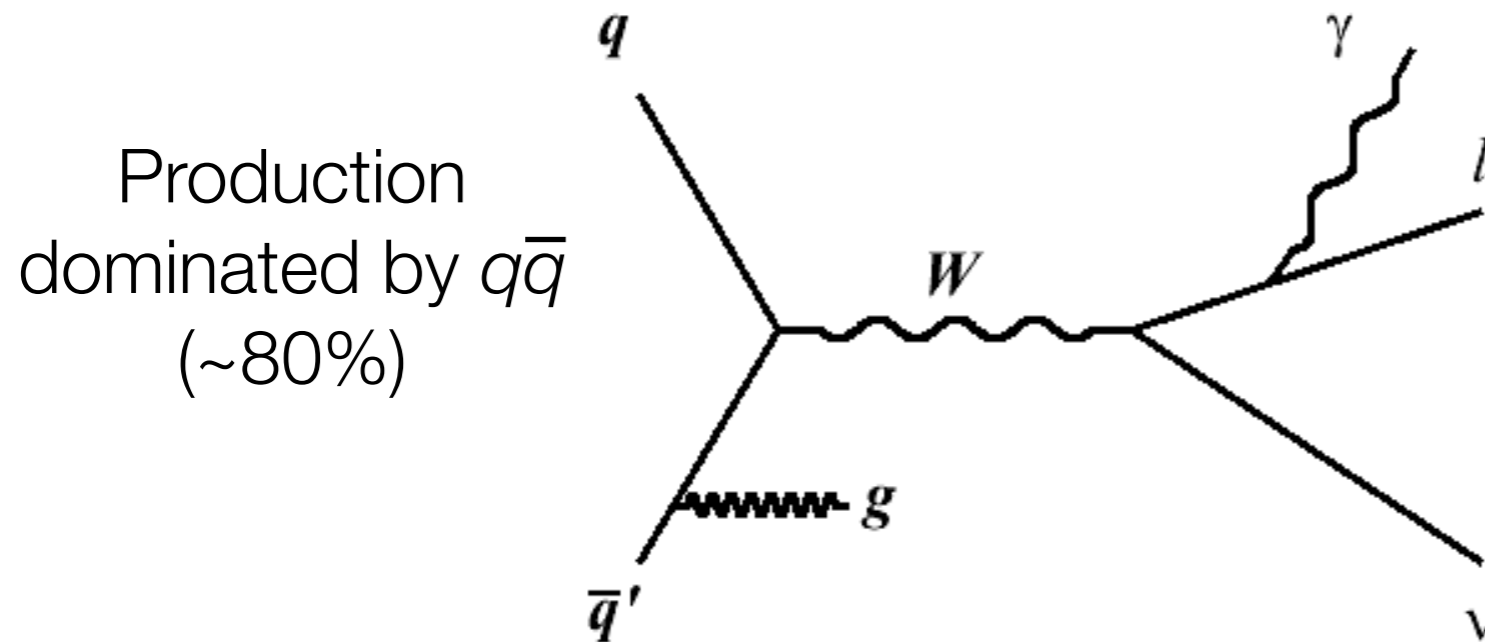
# Measurement strategy (more specifically)

- Perform COT alignment with cosmic ray data
- Calibrate **track momentum scale** using dimuon resonances ( $J/\psi$ ,  $\Upsilon$ ).
  - **Cross-check** with  $Z$  mass measurement and add as further calibration point
- Calibrate **calorimeter energy** using  $E/p$  of  $W$  and  $Z$  decays
  - **Cross-check** with  $Z$  mass measurement
- Calibrate **hadronic recoil** with  $Z$  decays to  $\mu$ ,  $e$ 
  - **Cross-check** with  $W$  recoil distributions
- Perform fits to  $e/\mu p_T$ ,  $\nu p_T$ , and **transverse mass**

$$m_T = \sqrt{2p_T^\ell p_T^\nu (1 - \cos \Delta\theta_{\ell\nu})}$$
  - Binned maximum likelihood fit to templates from tuned simulation
- Combine all **six** fits to yield final answer



# Selecting $W$ (and $Z$ ) bosons at CDF



Select  $e\nu$  and  $\mu\nu$  decays with high- $p_T$  lepton trigger

Lepton candidates:  
Electron  $E_T > 30$  GeV  
(track  $p_T > 18$  GeV)  
or Muon  $p_T > 30$  GeV

$W$  boson candidates:  
1 lepton passing cuts  
 $|\mathbf{u}| < 15$  GeV  
 $p_T^\nu > 30$  GeV  
 $60 < m_T < 100$  GeV

$Z$  boson candidates:  
2 lepton passing cuts  
 $66 < m_{ll} < 116$  GeV

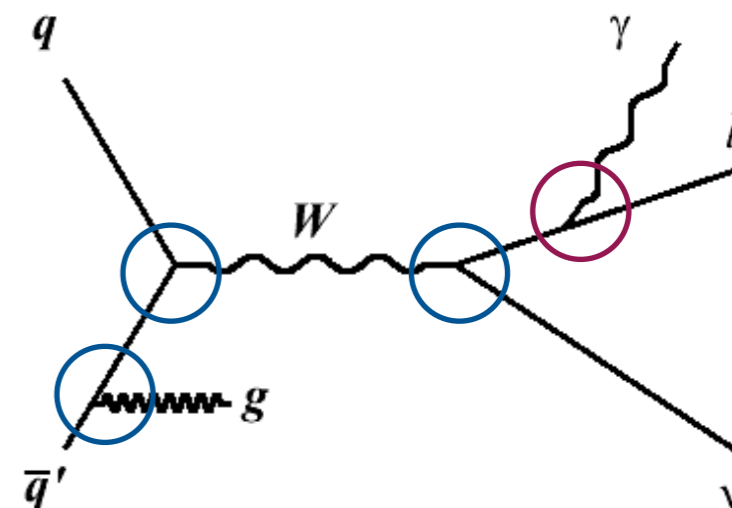
Analysis dataset: **2.2 fb<sup>-1</sup>**

**Candidate events:**  
 $W$ : 470126 (e), 624708 ( $\mu$ )  
 $Z$ : 16134 (e), 59738 ( $\mu$ )

Theoretical model

# Event generation and boson $p_T$

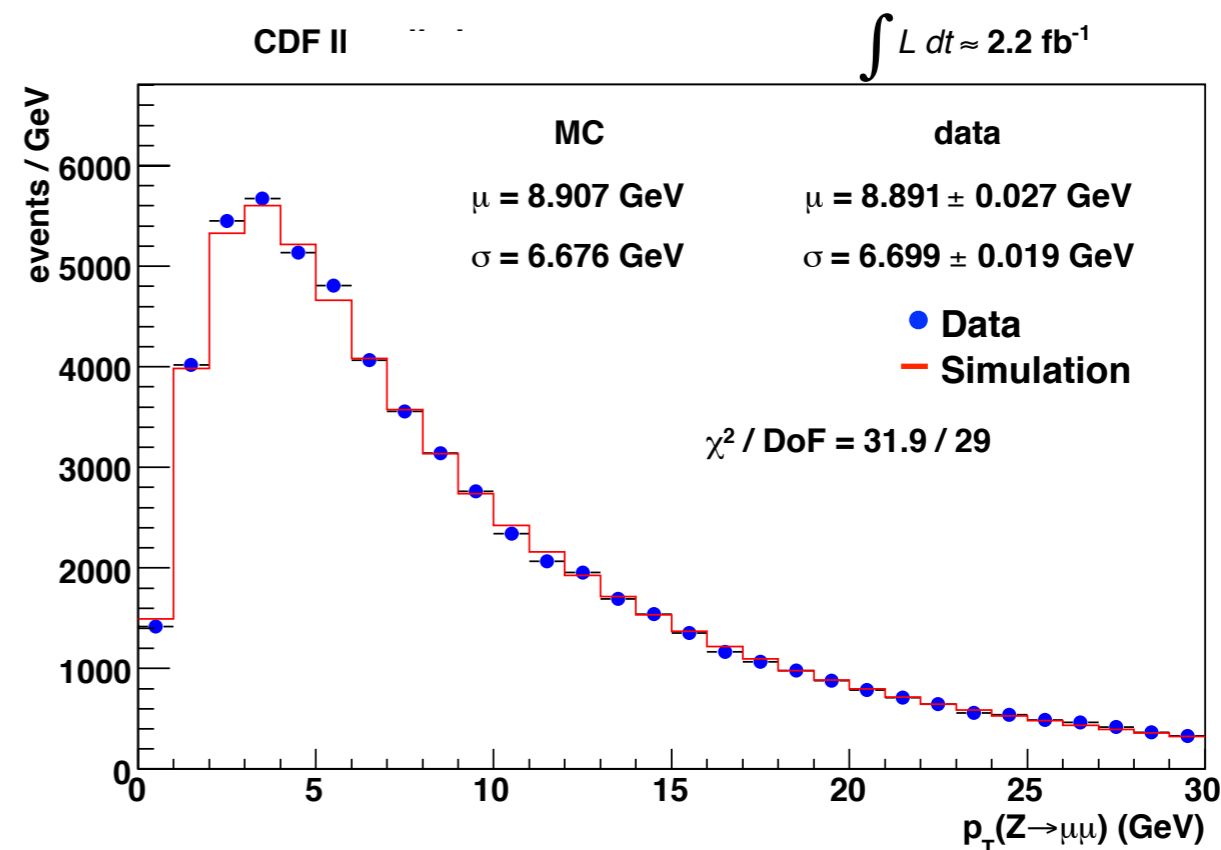
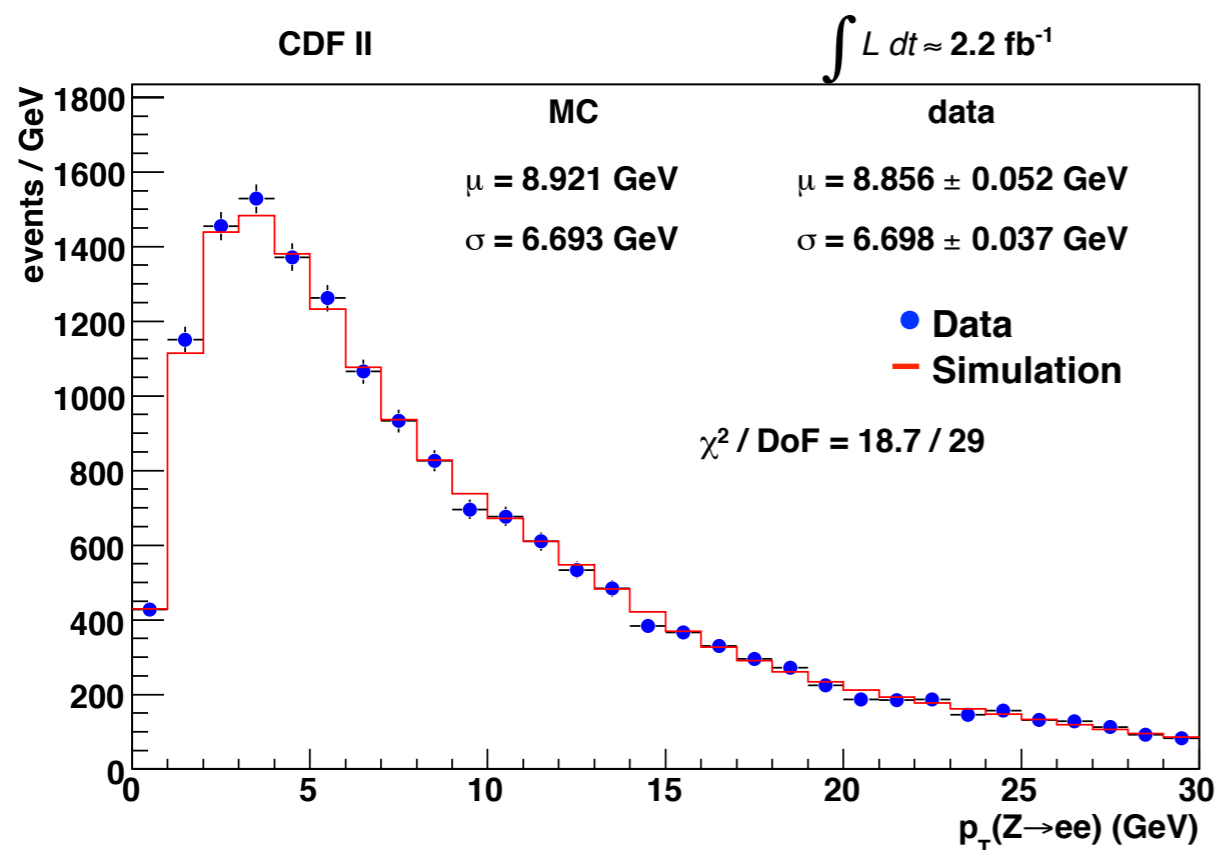
- Generator level simulation from **RESBOS**<sup>1</sup>
  - QCD effects, tunable parameters for non-perturbative regime (low- $p_T$ )
- QED radiation simulated by **PHOTOS**<sup>2</sup>
  - FSR multiphoton simulation
- Fit parameters in boson  $p_T$  shape
  - Low  $p_T$  sensitive to  $g_2$
  - Intermediate-high  $p_T$  sensitive to  $\alpha_s$
- Tuning with  $Z$  data applied to  $W$ s



<sup>1</sup>C Balazs and C-P Yuan, *PRD* **55**, 5558 (1997)

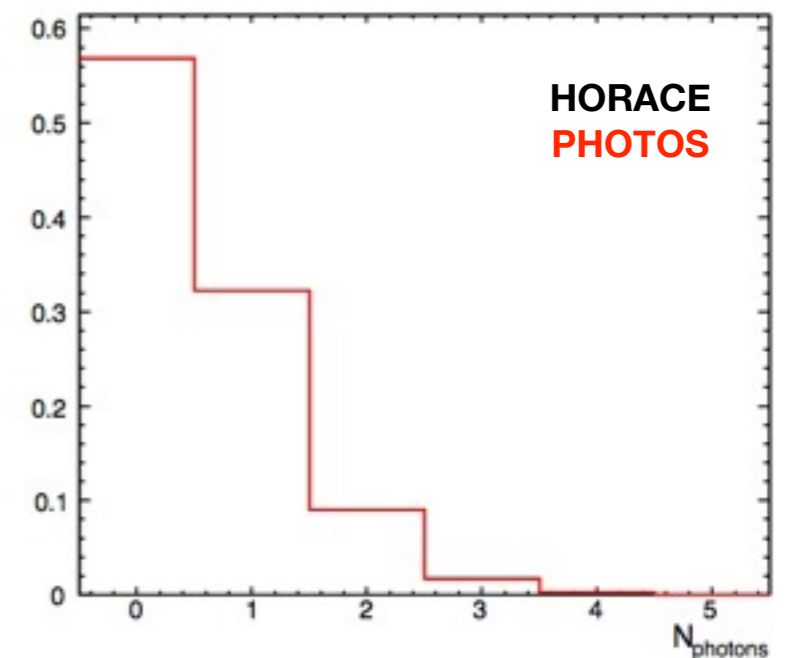
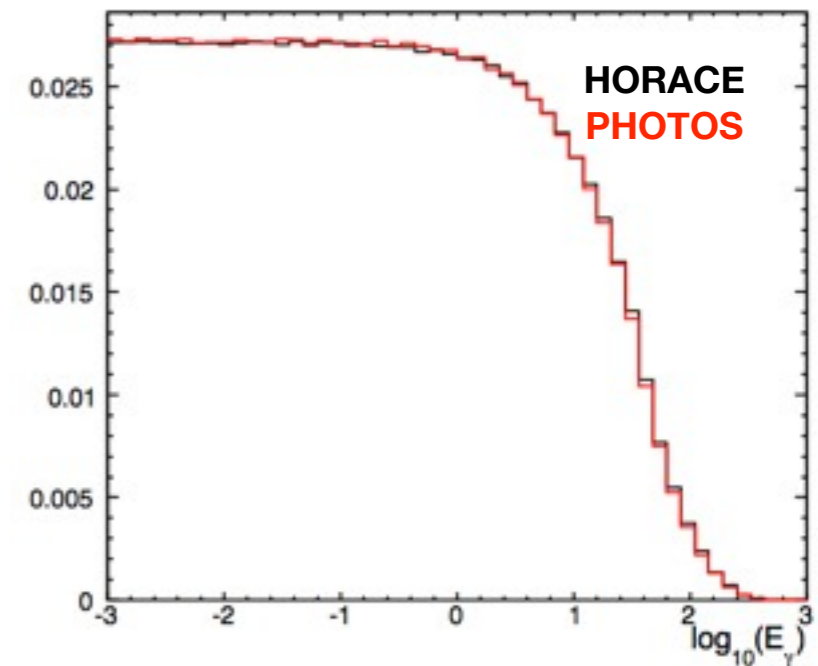
<sup>2</sup>P. Golonka and Z. Was, *Eur. J. Phys. C* **45**, 97 (2006)

$\Delta M_W = 5 \text{ MeV}$



# QED Radiation

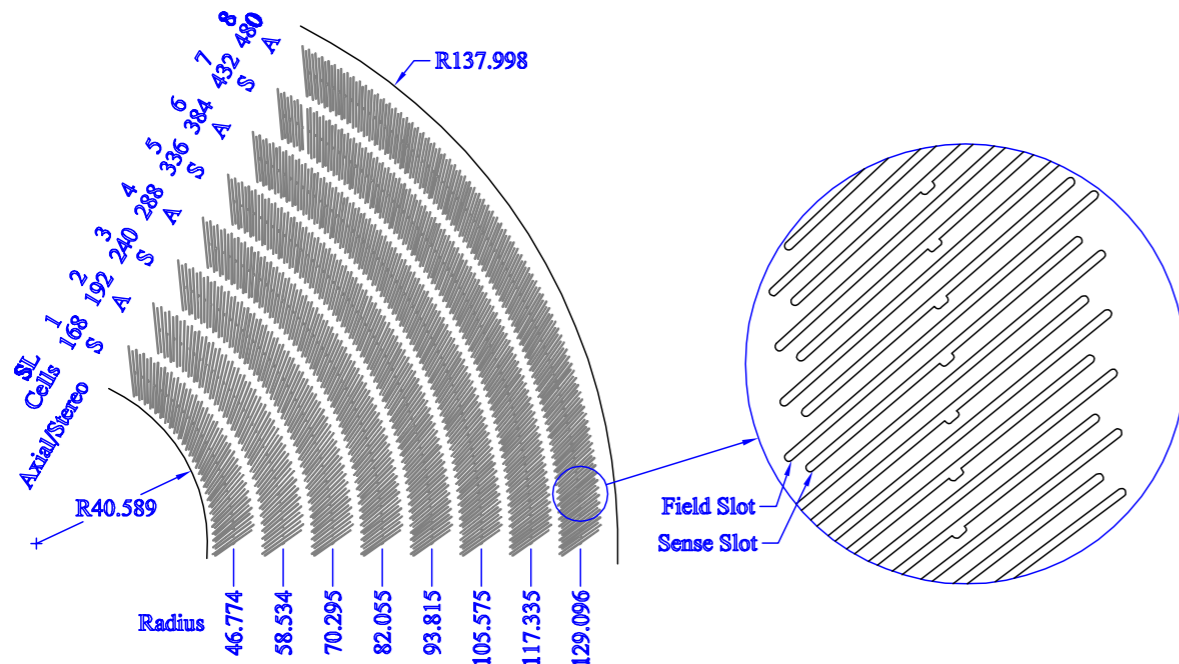
- Extensive studies of QED effects using **HORACE**<sup>1</sup>
  - Leading log approximation vs. exact single photon calculation
  - Multi-photon calculations
  - Higher-order soft/virtual corrections
  - $e^+e^-$  pair creation
  - ISR/FSR interference
  - Dependence on electroweak parameters/scheme
- Detailed comparison of HORACE and PHOTOS
  - Use PHOTOS in final model
- Total systematic uncertainty due to QED  $\Delta M_W = 4 \text{ MeV}$ 
  - *c.f.*  $\Delta M_W = 11 \text{ MeV}$  in 200/pb measurement (uncertainty dominated by subleading photons)



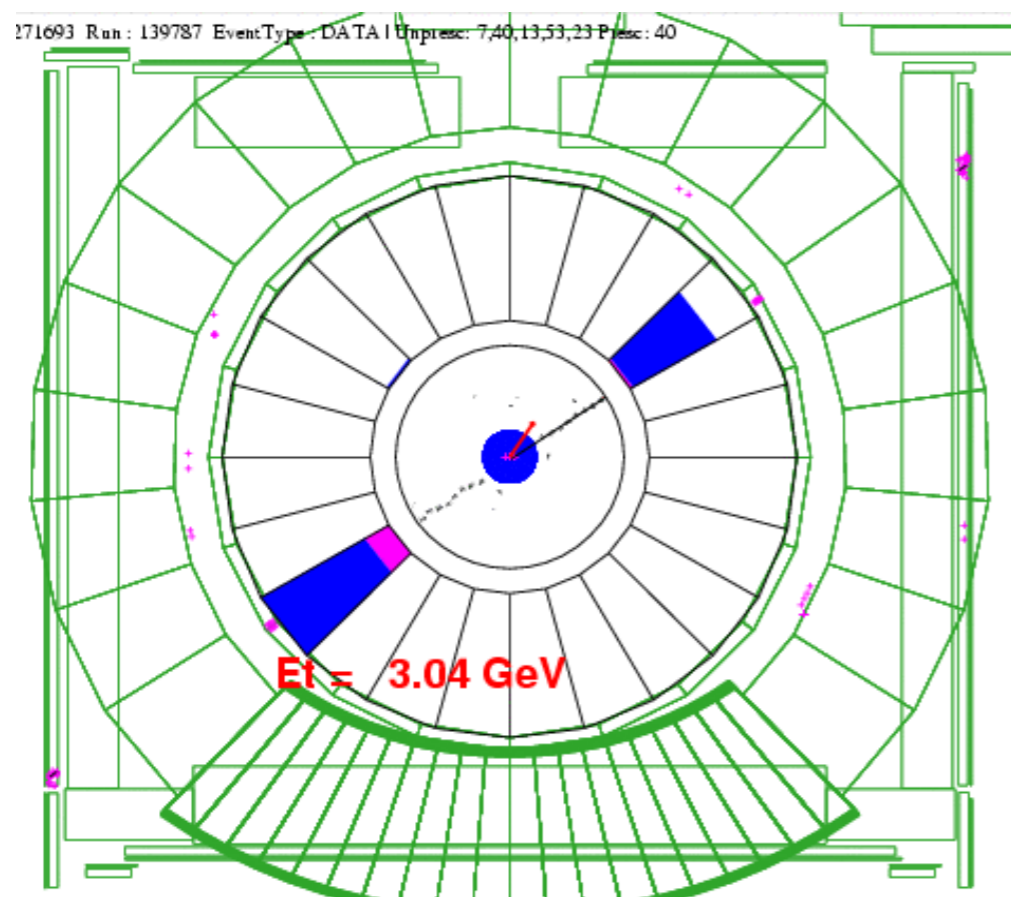
<sup>1</sup>C.M. Carloni Calame, G. Montagna, O. Nicrosini and A. Vicini, *JHEP* **0710**:109 (2007)

Tracker alignment

# COT alignment with cosmic rays

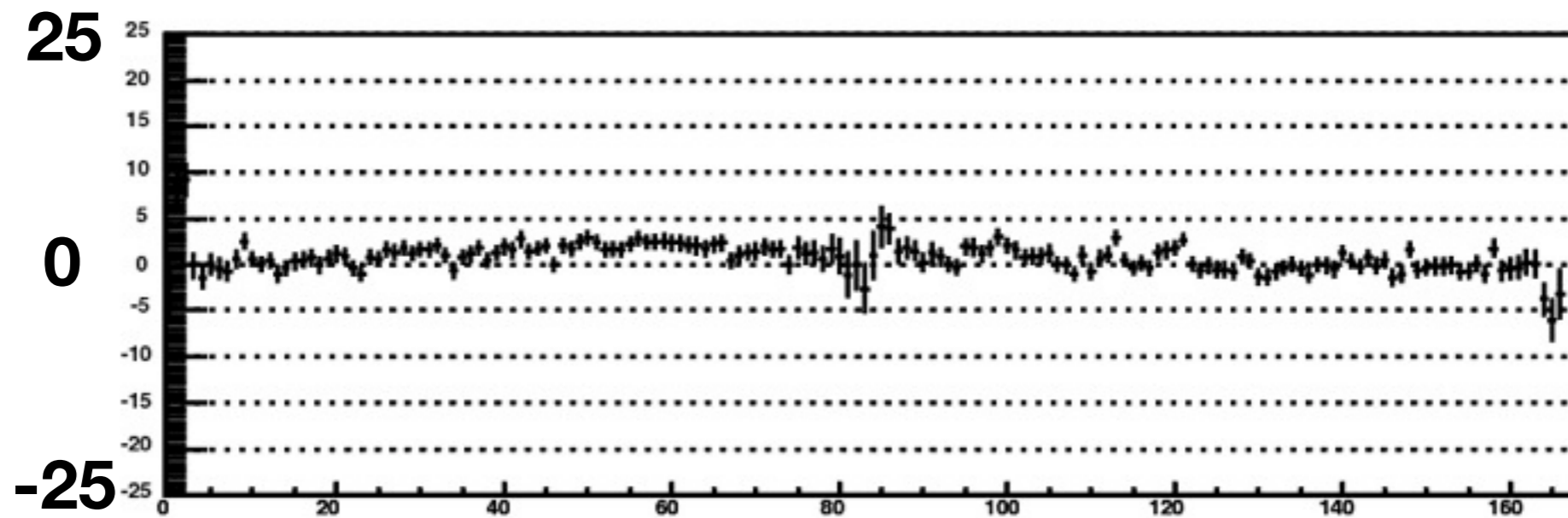
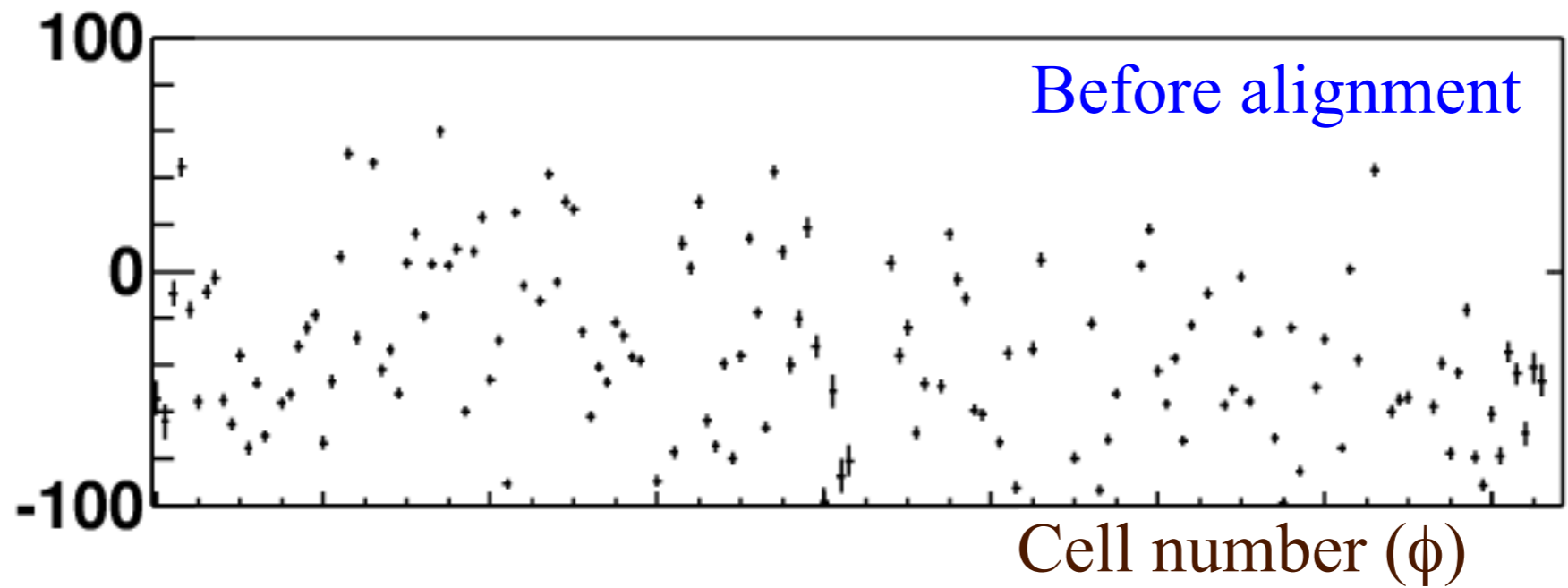


- COT consists of ~30k wires organized into ~2400 “cells”
- Accurate measure of wire positions crucial for precision track  $p_T$
- Use *in-situ* cosmic ray data for alignment
  - Fit of COT hits on either side of vertex to single helix
  - A. Kotwal, H. Gerberich, C. Hays, NIM A **506**, 110 (2003)



# Tracker alignment

- Improve relative alignment precision from  $\sim 50\mu\text{m}$  to  $\sim 2\mu\text{m}$

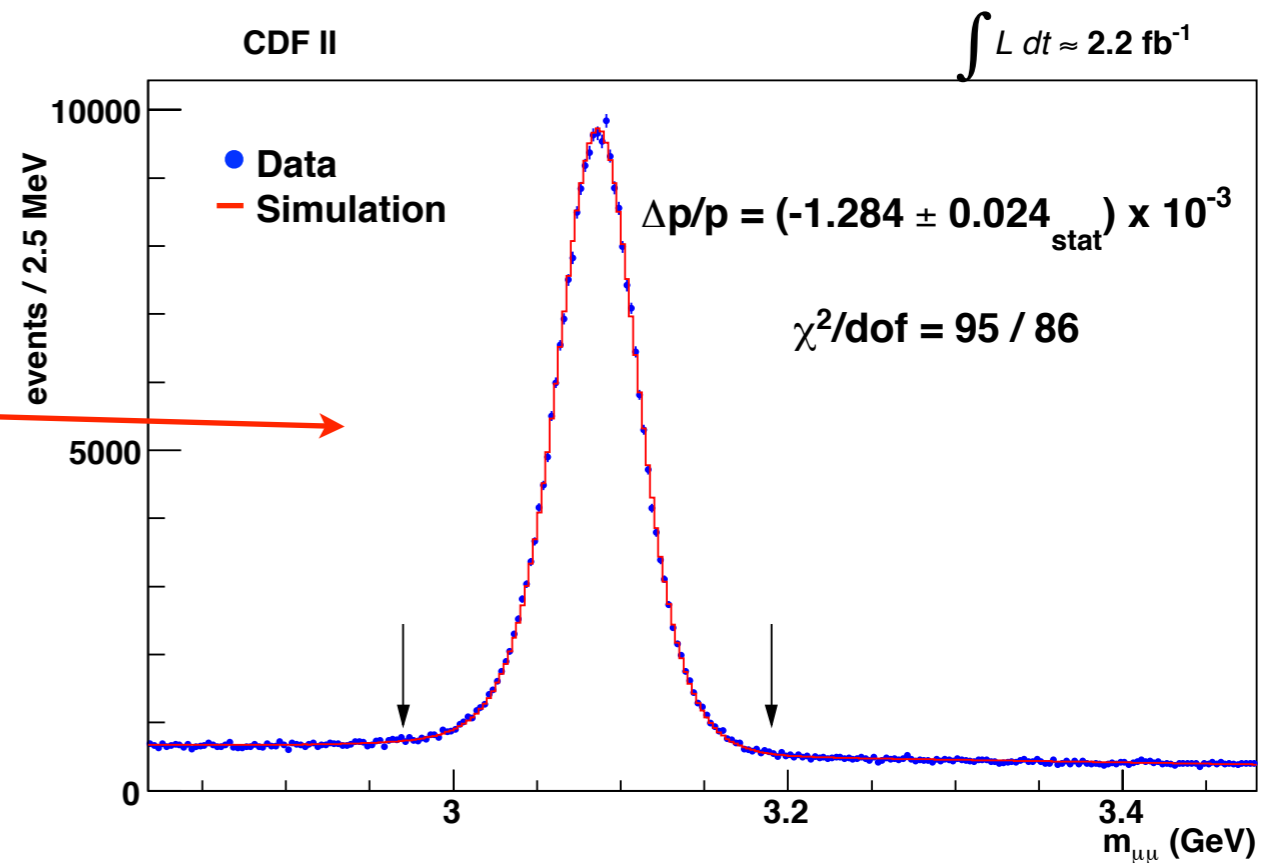
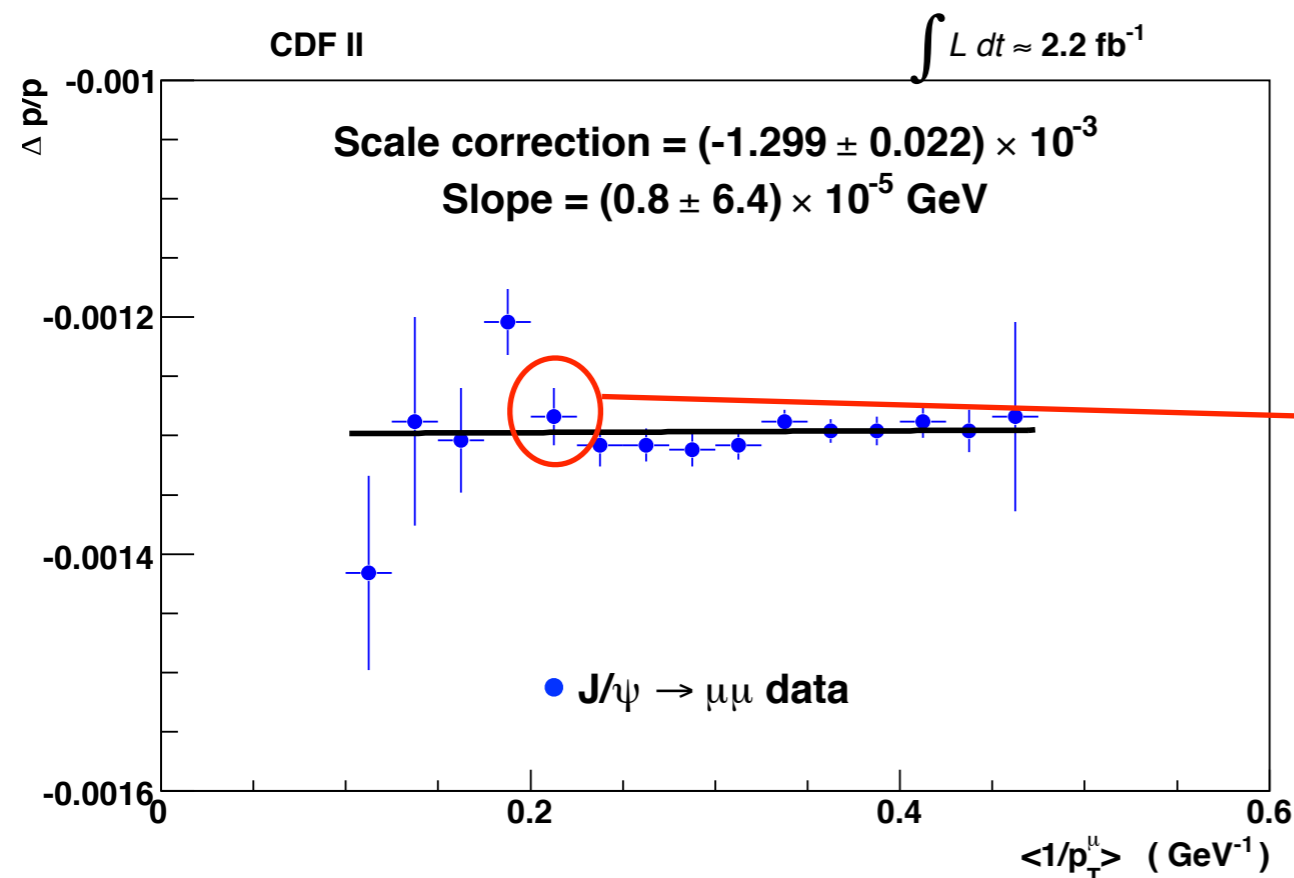




Track momentum scale

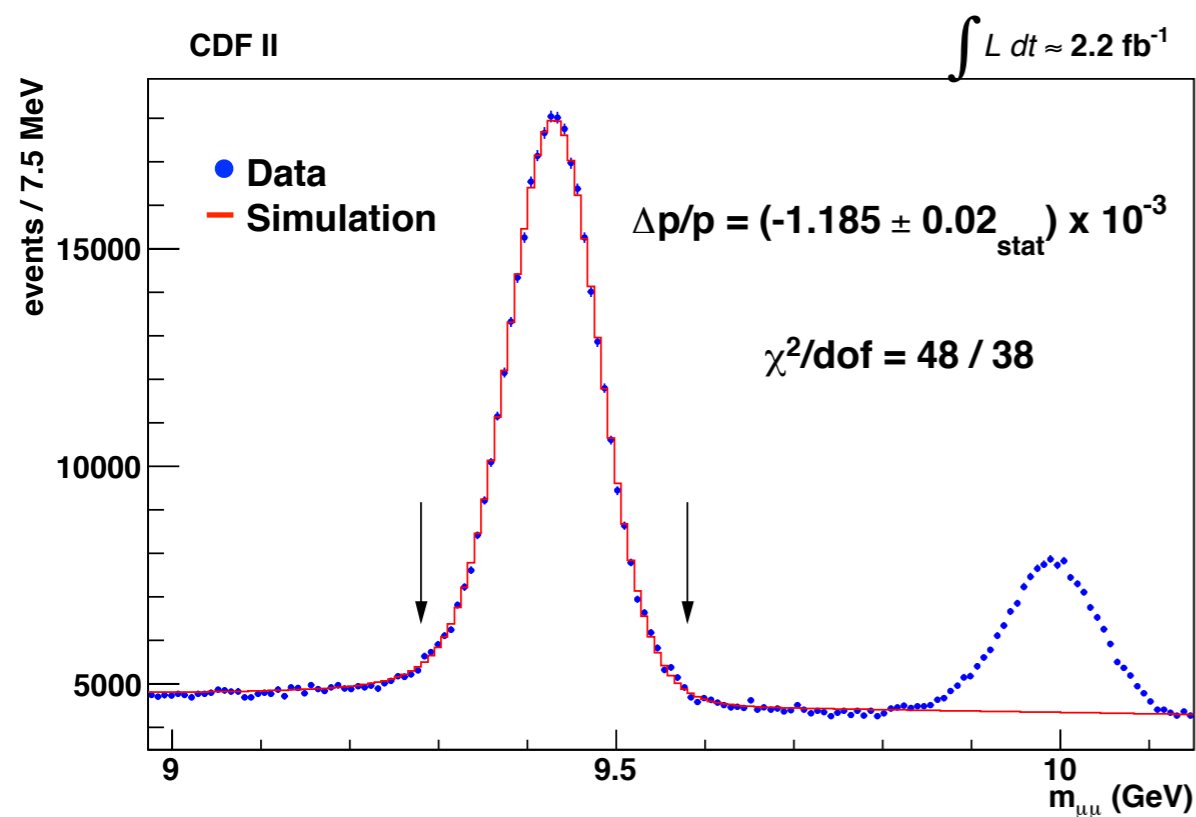
# Track momentum scale: $J/\psi$

- Utilize large samples of  $\mu\mu$  resonances ( $J/\psi$ ,  $Y$ ,  $Z$ ) to set overall scale
- Size of  $J/\psi$  sample allows subsample fits
  - Fit  $J/\psi$  mass in bins of  $\langle 1/p_T(\mu) \rangle$  and apply material scale calibration (4%) to remove dependence
- Apply calibration from  $J/\psi$  to  $Y$

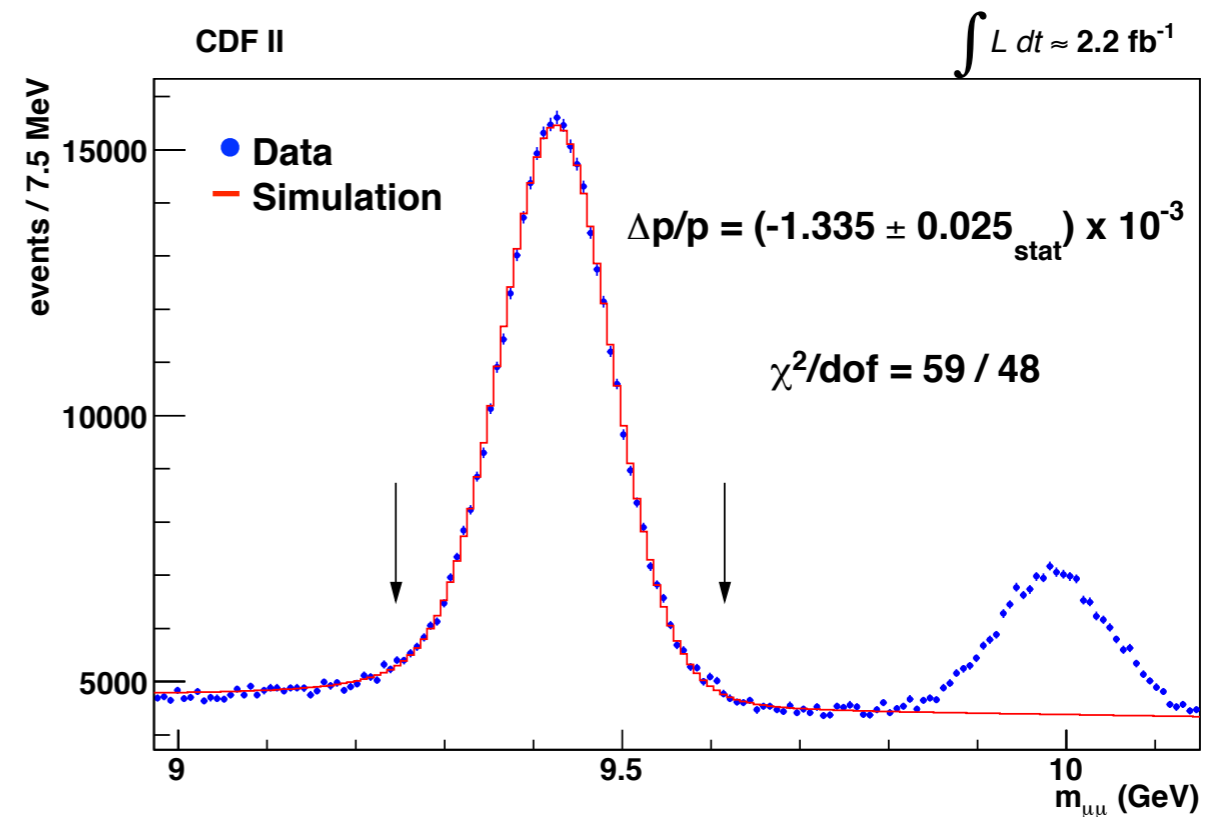


# Track momentum scale: $\Upsilon$

- $\Upsilon$  sample provides higher- $p_T$  sample
- $\Upsilon$ s produced promptly: validation of beam-constraining (BC) procedure
  - Perform fit with BC and non-BC tracks
    - Take average of two fits, assign systematic
- Combine  $J/\psi$  and  $\Upsilon$  scales and apply to  $Z$ s



Beam constrained tracks



Non-beam constrained tracks

# Track momentum scale: systematic uncertainties

---

Source	$J/\psi$ ( $\cdot 10^{-3}$ )	NBC- $\Upsilon$ ( $\cdot 10^{-3}$ )	common ( $\cdot 10^{-3}$ )
QED	0.080	0.045	0.045
B field non-uniformity	0.032	0.034	0.032
Ionizing material	0.022	0.014	0.014
Resolution	0.010	0.005	0.005
Backgrounds	0.011	0.005	0.005
Misalignment	0.009	0.018	0.009
Trigger efficiency	0.004	0.005	0.004
Fitting window	0.004	0.005	0.004
$\Delta p/p$ step size	0.002	0.003	0
World-average	0.004	0.027	0
Total systematic	0.092	0.068	0.058
Statistical	0.004	0.025	0
Total	0.092	0.072	0.058

- Dominated by QED and B-field non-uniformity
  - BC vs NBC comparison contributes additional  $0.036 \times 10^{-3}$

# Track momentum scale: systematic uncertainties

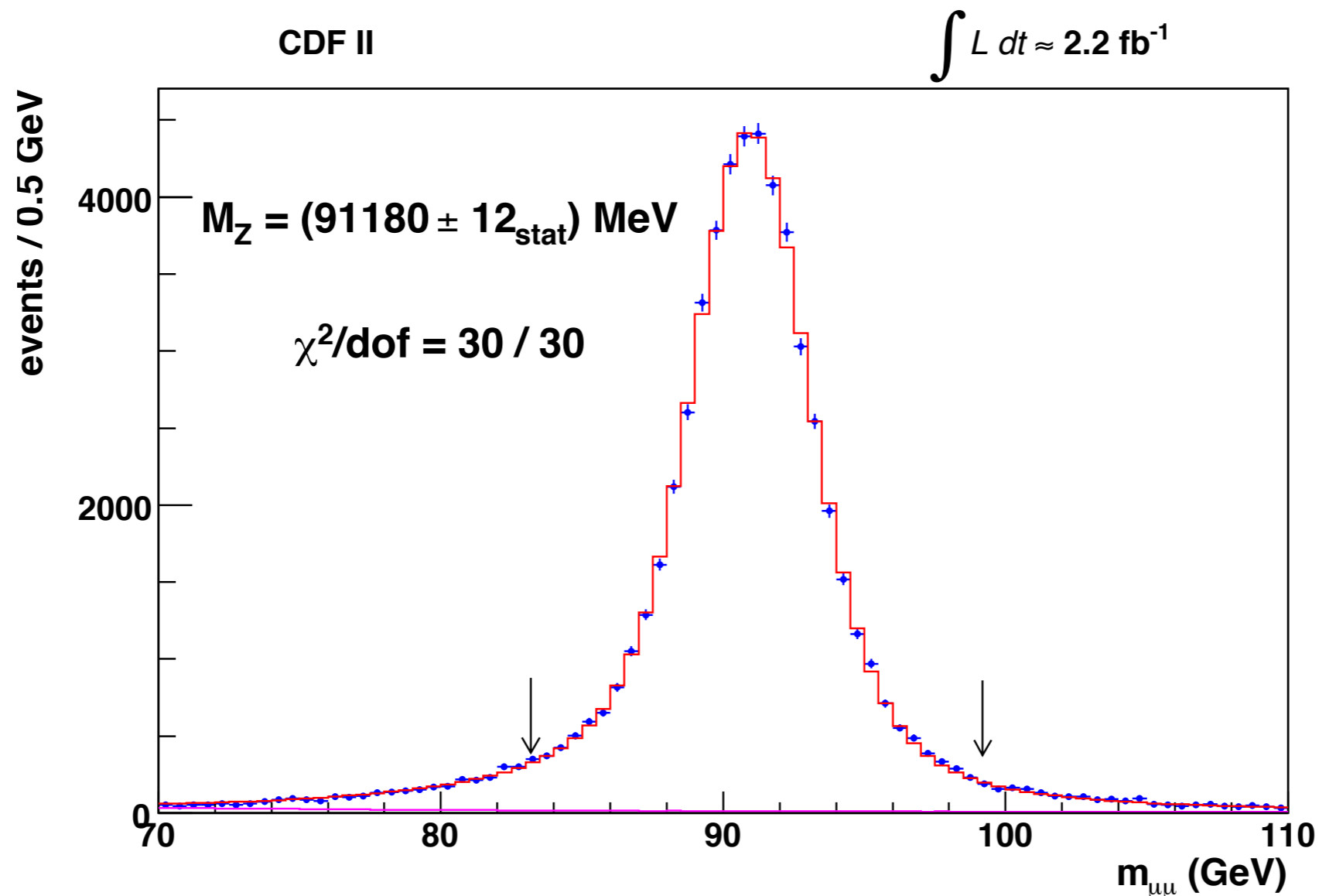
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$\Delta M_W \sim 6 \text{ MeV}$

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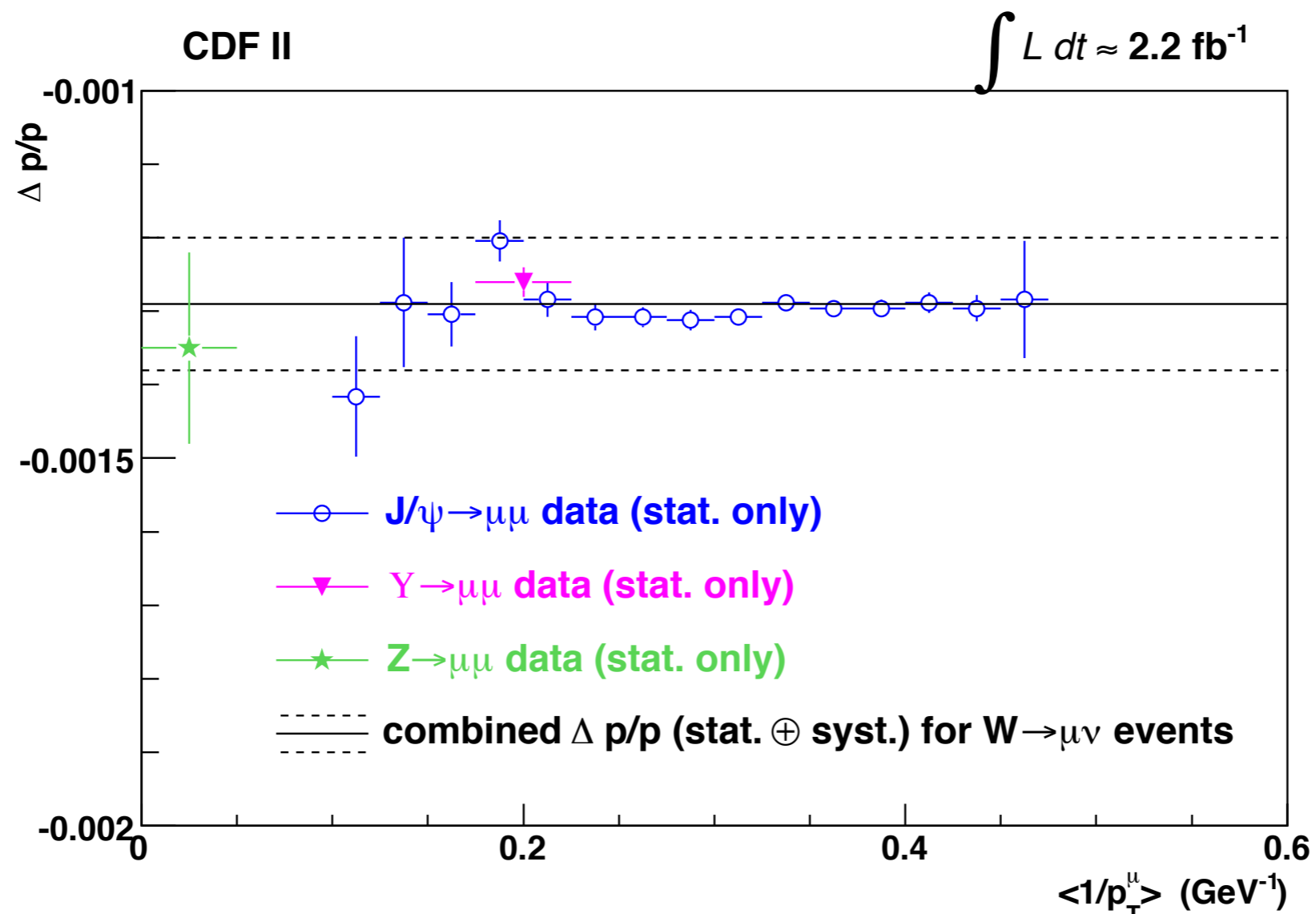
# Muon $Z$ mass measurement

- Perform **independent** measurement of  $Z$  mass using tuned momentum scale
  - Fit central value kept blind during scale calibration
  - $M_Z = 91180 \pm 12_{\text{stat}} \pm 9_{\text{p-scale}} \pm 5_{\text{QED}} \pm 2_{\text{alignment}} = \mathbf{91180 \pm 16 \text{ MeV}}$
  - Excellent agreement with world average ( $91188 \pm 2 \text{ MeV}$ )



# Final momentum scale

- Add Z data as final calibration point for momentum scale
  - $\Delta p/p_{\text{final}} = (-1.29 \pm 0.07_{\text{stat}} \pm 0.05_{\text{QED}} \pm 0.02_{\text{align}}) \times 10^{-3}$
  - Apply scale to  $W$  muons and  $E/p$  calibration
  - Systematic uncertainty  $\Delta M_W = 7 \text{ MeV}$

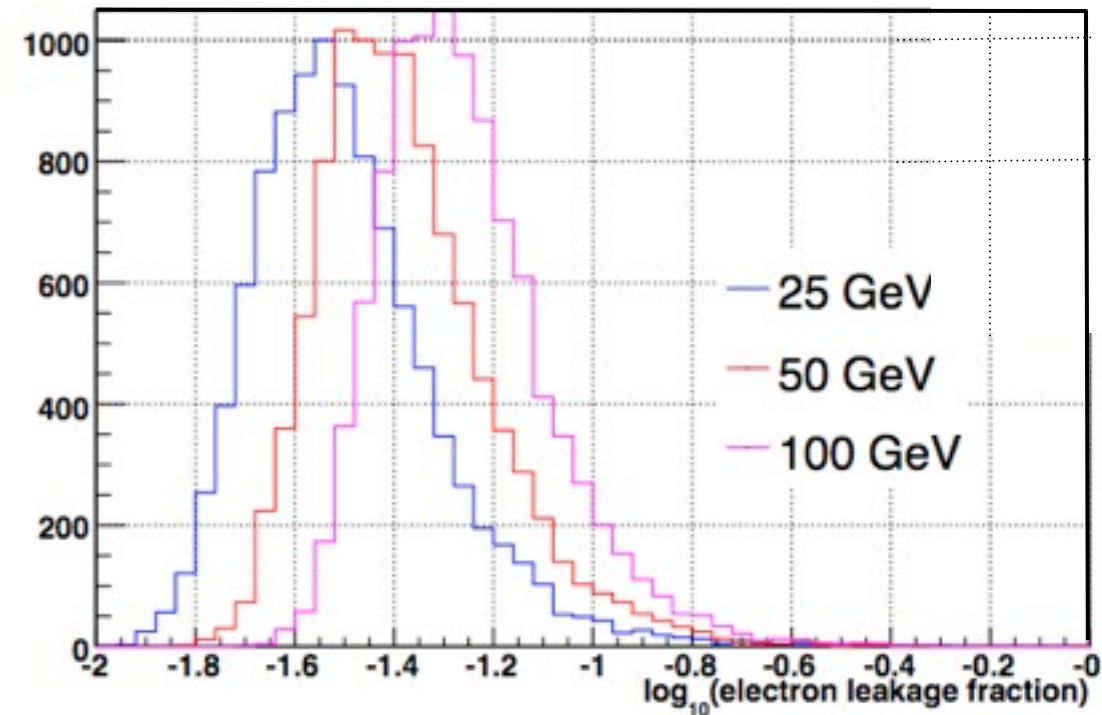


EM calorimeter scale



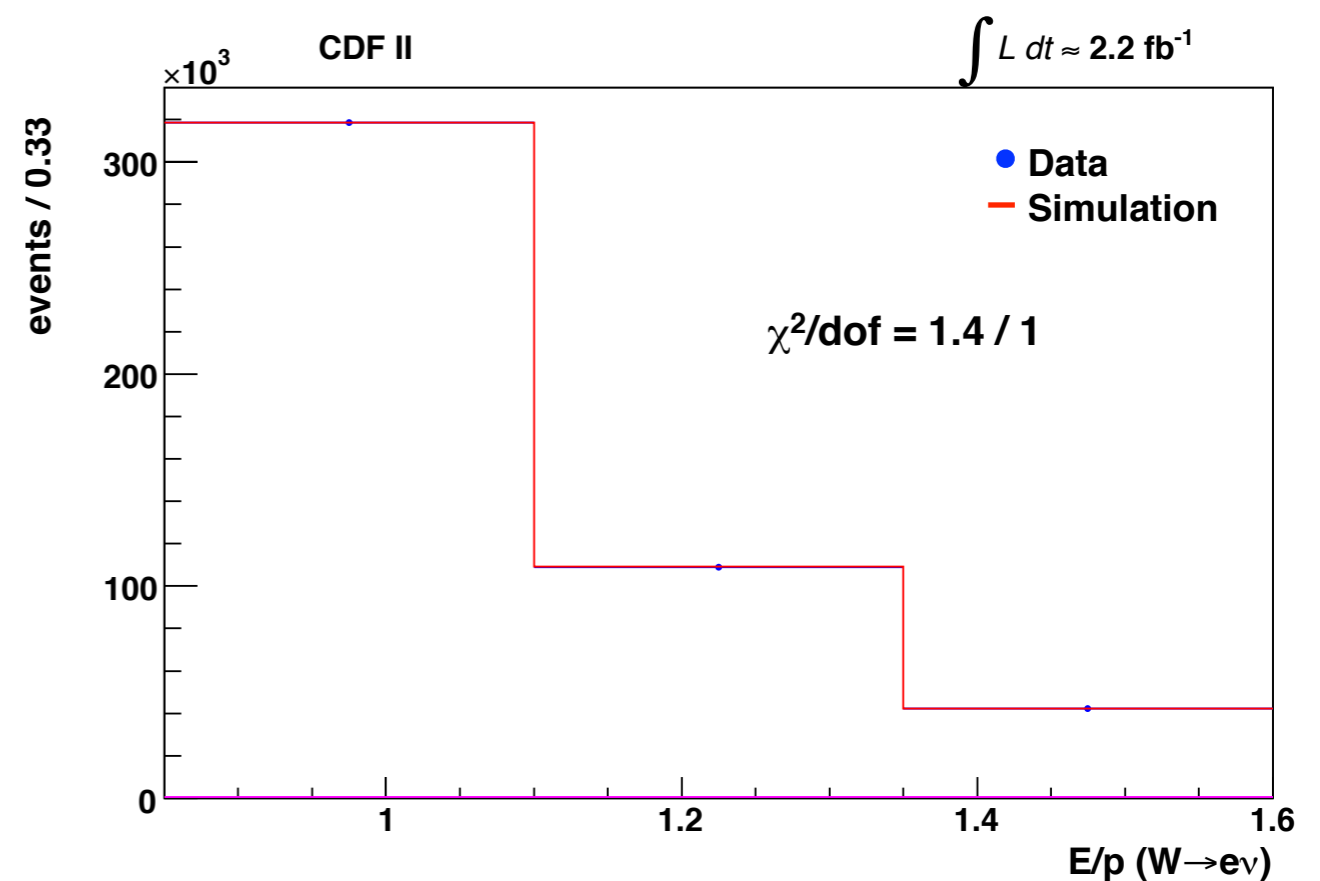
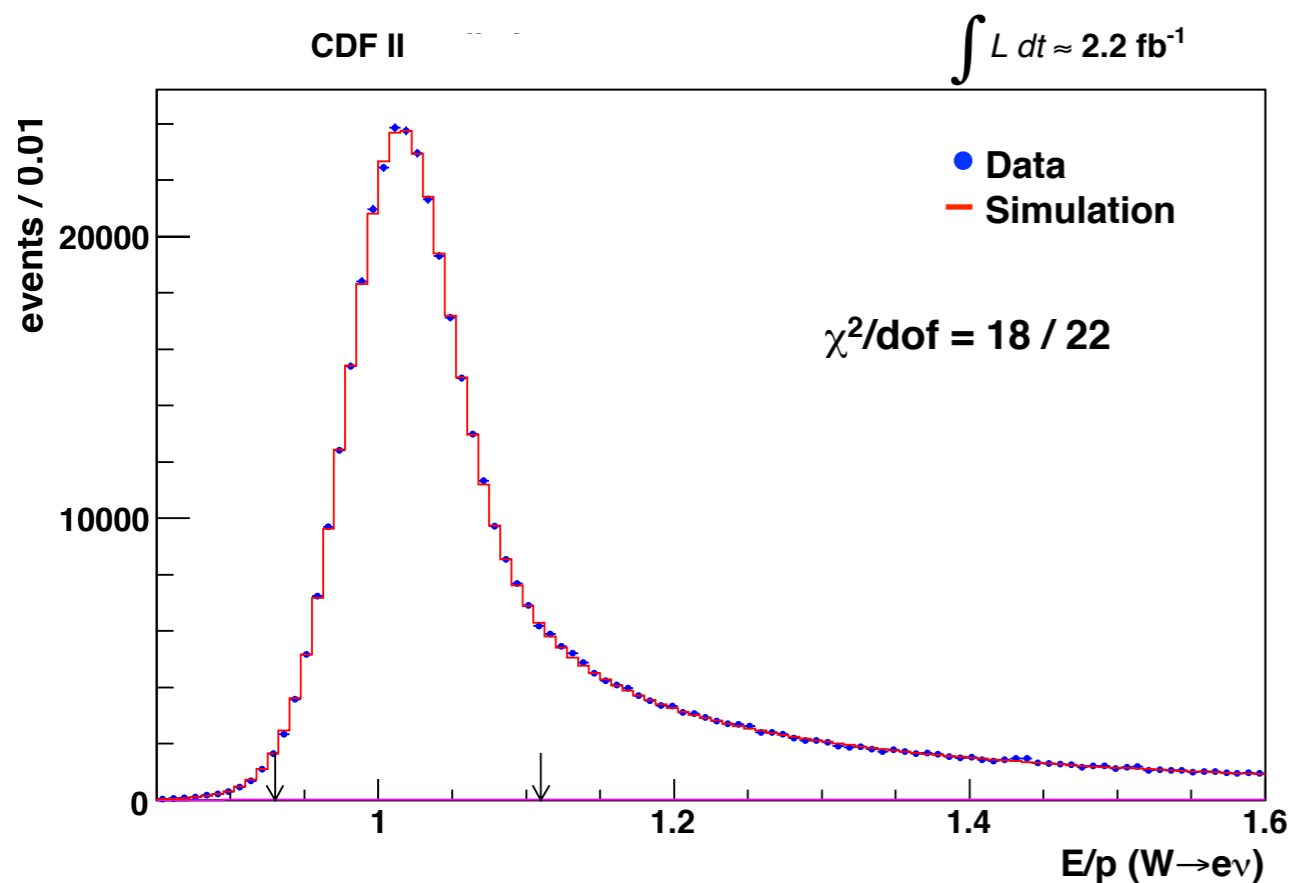
# Simulation for electrons and photons

- EM energy loss studied using detailed GEANT4-based simulation
  - Leakage into hadronic calorimeter
  - Absorption into coil
  - Dependence on incident angle and  $E_T$
- Improved model of Landau-Pomeranchuk-Migdal (LPM) suppression of bremsstrahlung
  - Sophisticated material map for tracker region of detector



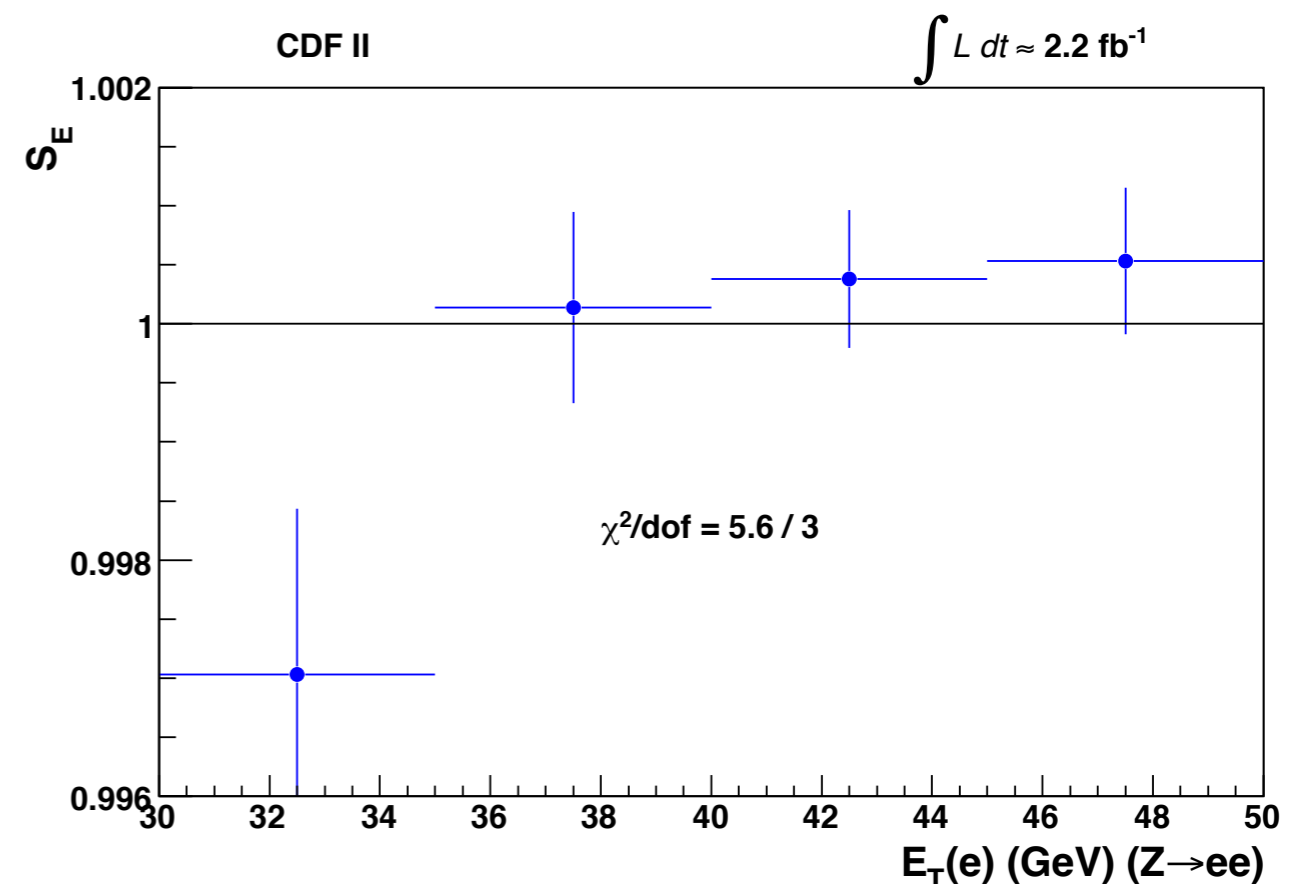
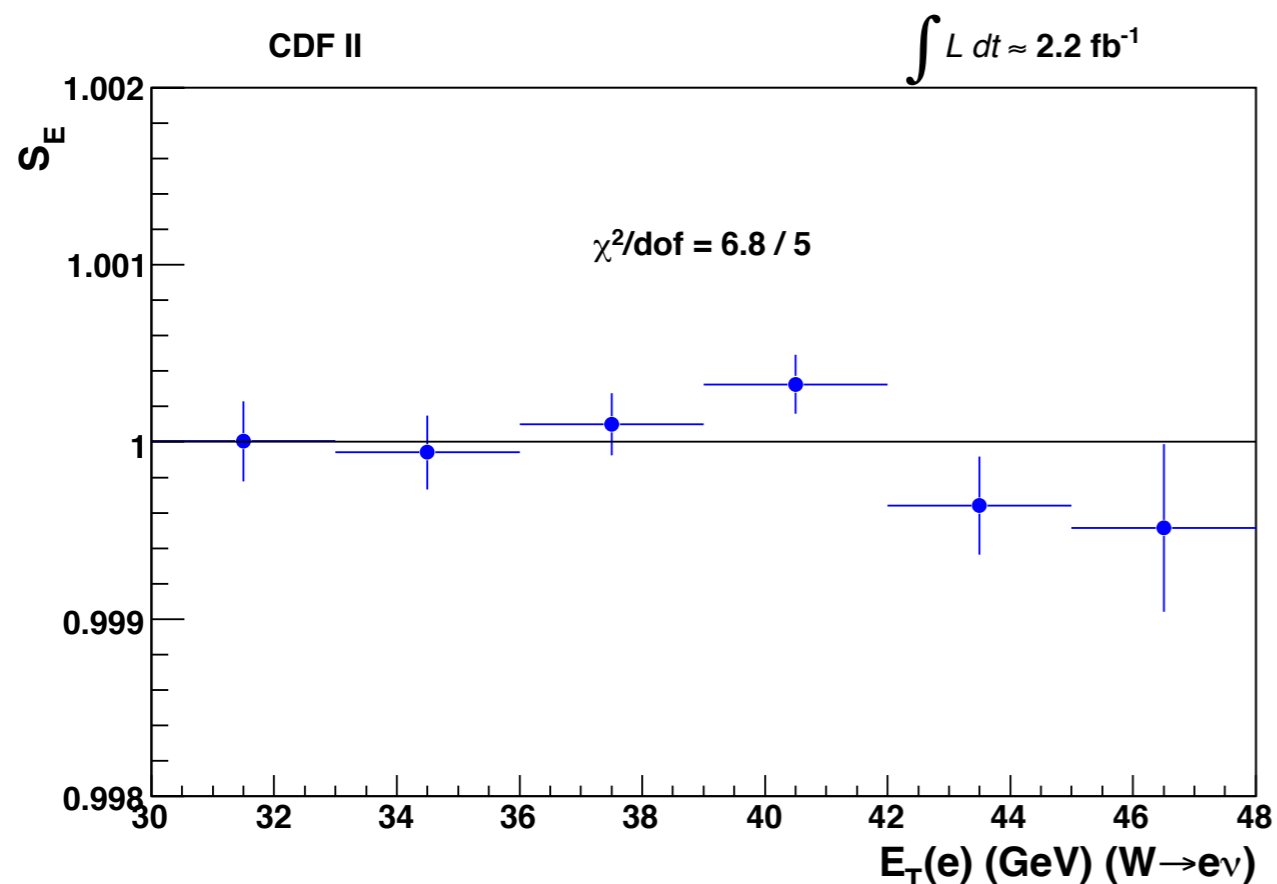
# Energy scale calibration

- Calibrate EM calorimeter response using  $W$  and  $Z$   $E/p$  distributions
  - Fit to peak to obtain scale (central value of 1 by construction)
    - $\Delta S_E = (9_{\text{stat}} \pm 5_{\text{non-linearity}} \pm 5_{\text{mat}} \pm 9_{\text{p-scale}}) \times 10^{-5}$
  - Fit to tail to tune amount of radiative material
    - Apply scale factor to material model  $S_{X0} = 1.026 \pm 0.003_{\text{stat}} \pm 0.002_{\text{bkg}}$
- Systematic uncertainty  $\Delta M_W = 13 \text{ MeV}$



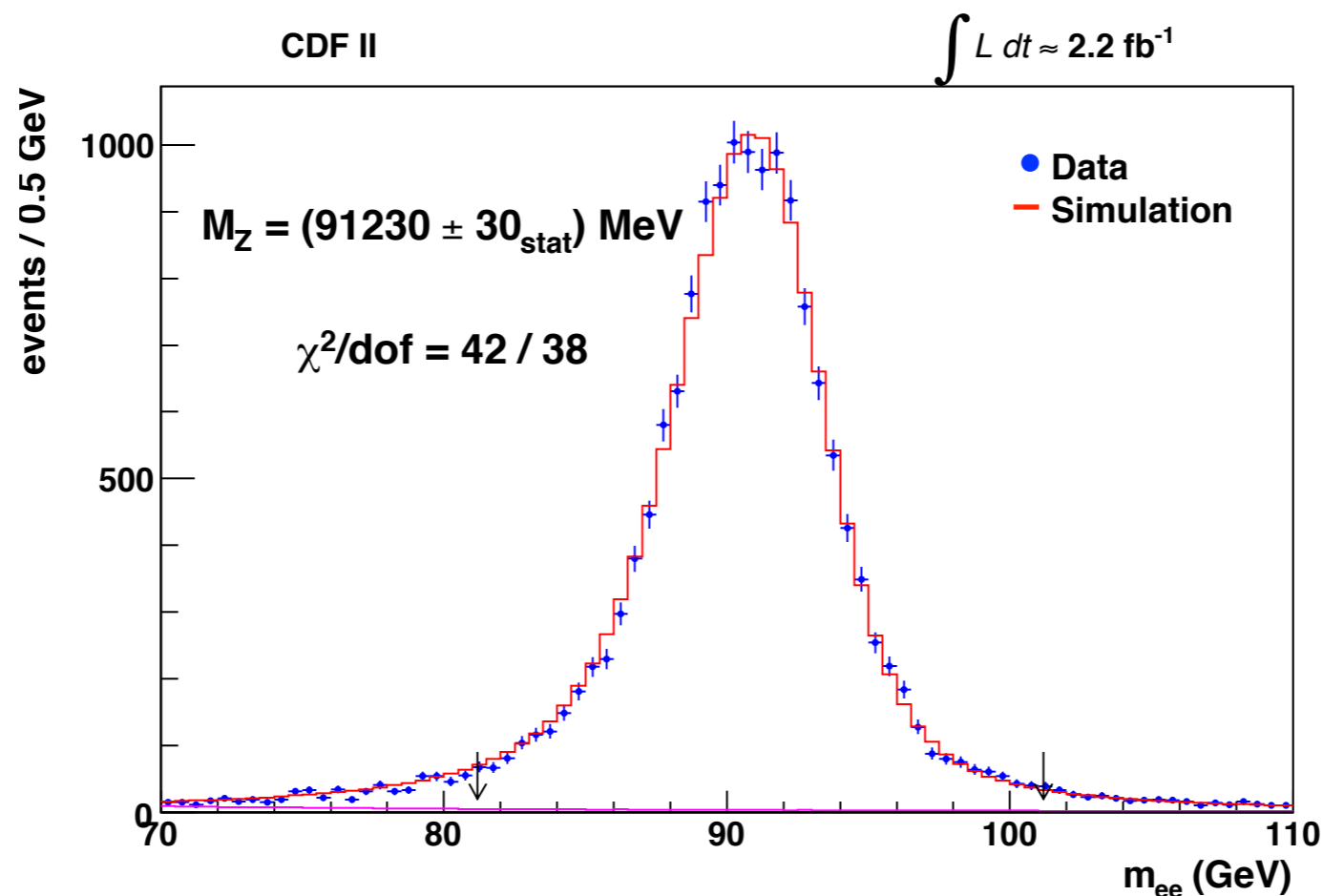
# EM scale non-linearity

- Fit  $E/p$  in bins of electron  $E_T$ 
  - Parameterize non-linearity as  $S_E = 1 + \beta \log(E_T/39 \text{ GeV})$
- Tune using  $W$  and  $Z$  data and obtain  $\beta = (5.2 \pm 0.7_{\text{stat}}) \times 10^{-3}$ 
  - $\Delta M_W = 4 \text{ MeV}$
- Obtain flat response in  $E_T$  after tuning



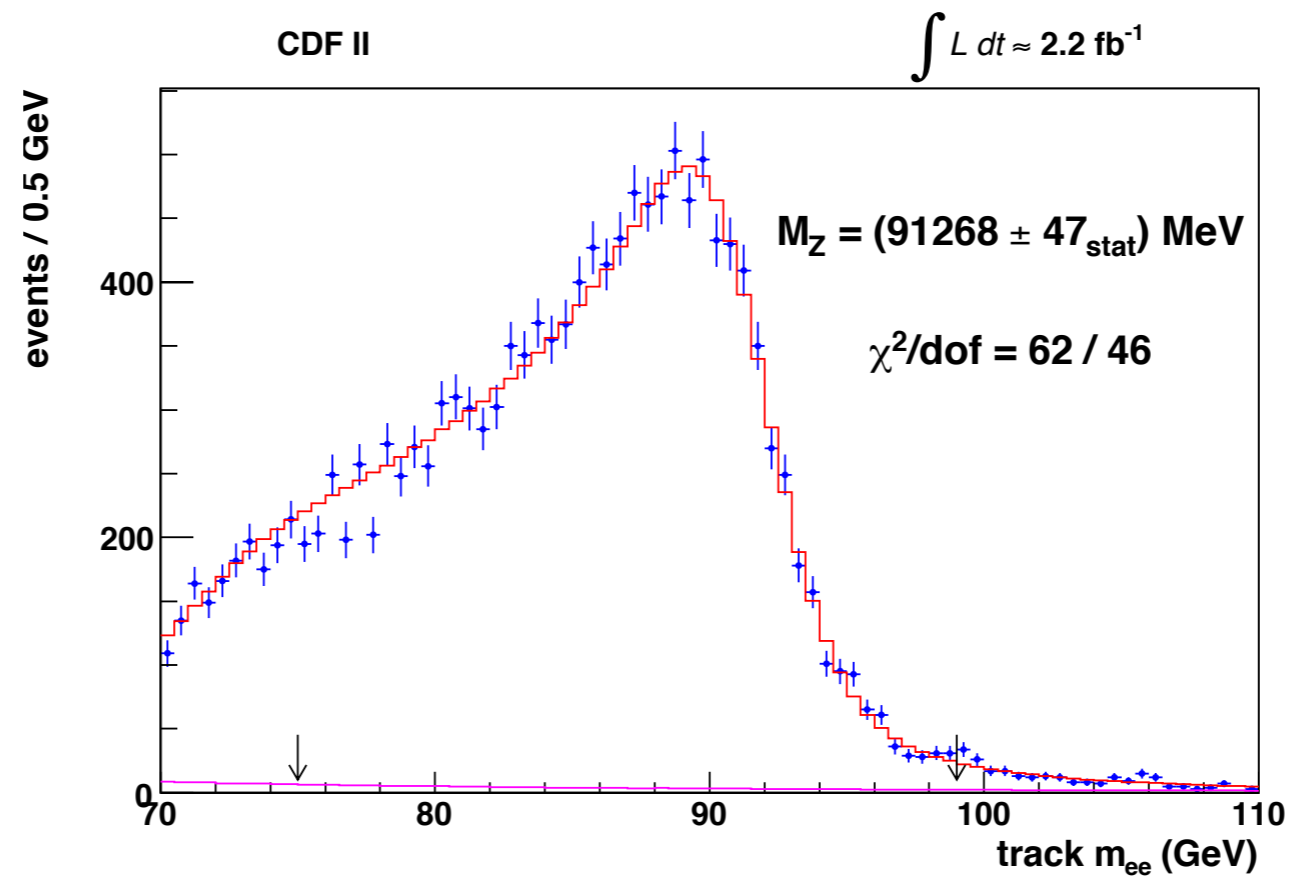
# Electron $Z$ mass and final EM energy scale

- Perform **independent** measurement of  $Z$  mass using calibrated EM scale
  - $M_Z = 91230 \pm 30_{\text{stat}} \pm 10_{E/p} \pm 8_{p\text{-scale}} \pm 5_{\text{QED}} \pm 2_{\text{alignment}} = \mathbf{91230 \pm 33 \text{ MeV}}$
  - Excellent agreement with world average  $M_Z = 91188 \pm 2 \text{ MeV}$
- Combine  $E/p$  calibration with  $M_Z$  to obtain final EM calibration
  - Systematic uncertainty  $\Delta M_W = \mathbf{10 \text{ MeV}}$



# Z mass with electron tracks

- Measurement made with only track momenta of Z electrons
- Validates material model and application of momentum scale to high- $p_T$  electron tracks



# Lepton resolution

---

- Muons
  - Track resolution determined by uncertainty on beamspot size ( $35 \pm 1 \mu\text{m}$ ) and track hit resolution ( $150 \pm 1 \mu\text{m}$ )
  - Tuned using widths of Z and Y peaks

- Electrons

- EM calorimeter resolution defined by sampling term and constant term

$$\sigma = 12.6\% \sqrt{E_T / \text{GeV}} \oplus \kappa$$

- Constant term tuned using E/p distribution  $\kappa = (0.58 \pm 0.05)\%$
    - Apply secondary constant term for radiative electrons ( $E/p > 1.1$ )
      - $\kappa_\gamma = (7.4 \pm 1.8)\%$
- Resolution terms total  $\Delta M_W = 4 \text{ MeV}$

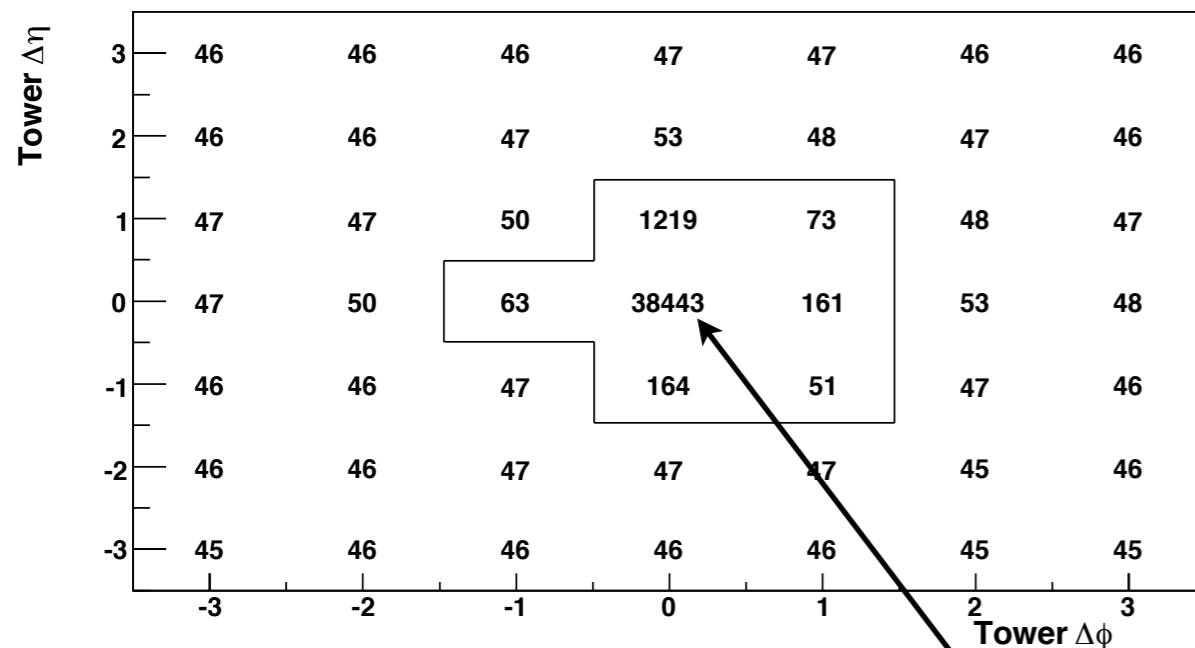
Hadronic recoil

# Hadronic recoil: lepton removal

- Hadronic recoil  $\mathbf{u}$  is vector sum of all calorimeter towers minus towers containing lepton energy
- Some underlying event energy removed with “lepton towers”
  - Estimate using rotated lepton removal windows
  - Systematic uncertainty  $\Delta M_W = 2 \text{ MeV}$

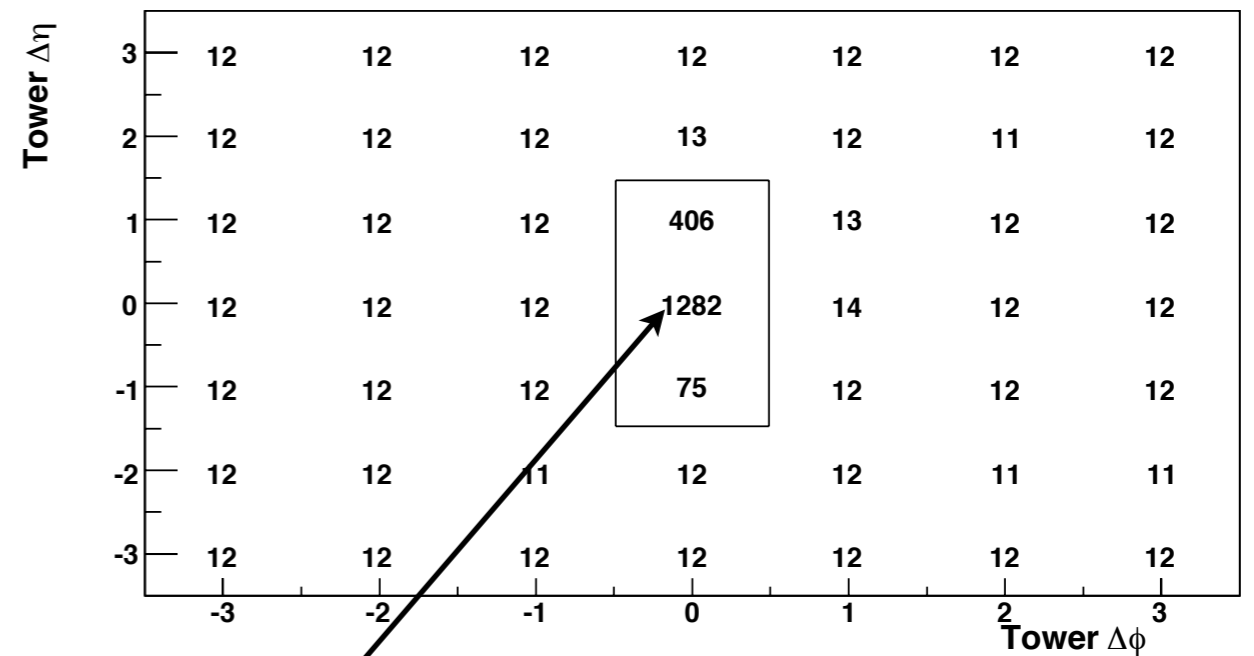
## Electron channel W data:

Mean EM calorimeter deposition (MeV)



## Muon channel W data:

Mean hadronic calorimeter deposition (MeV)



□ Default towers removed

Central lepton tower



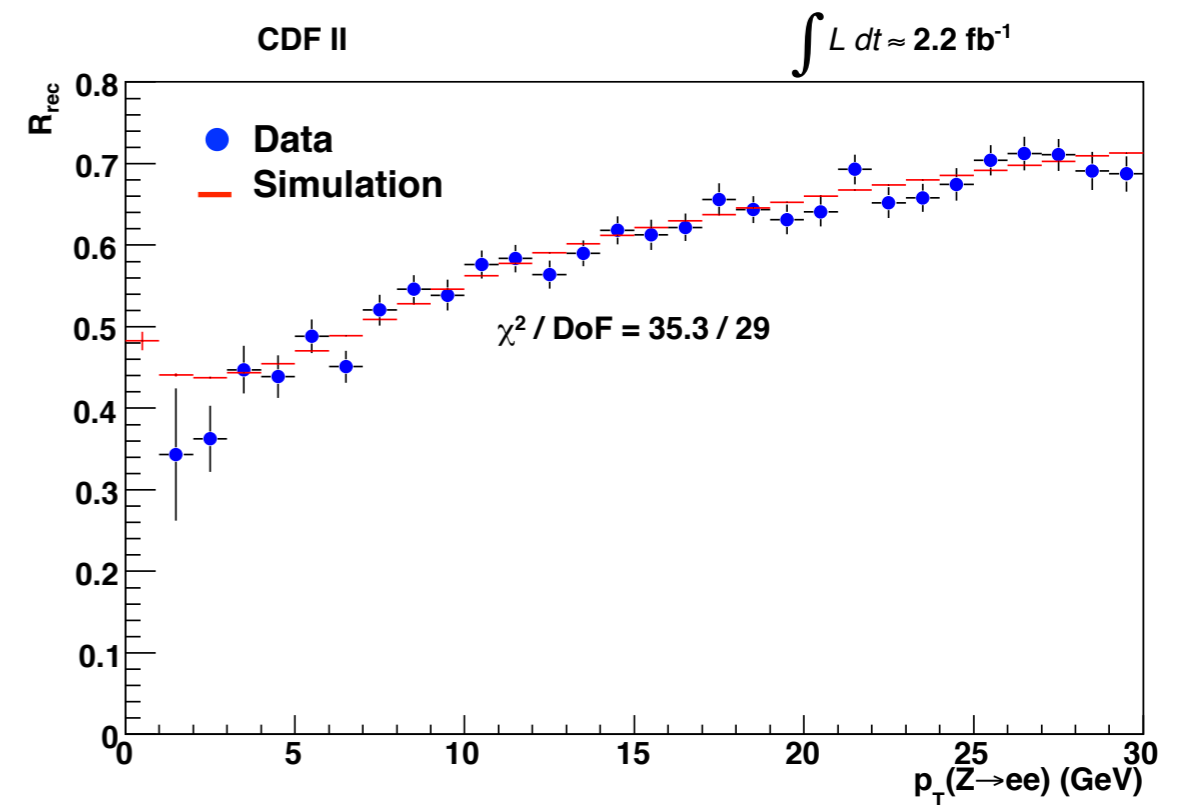
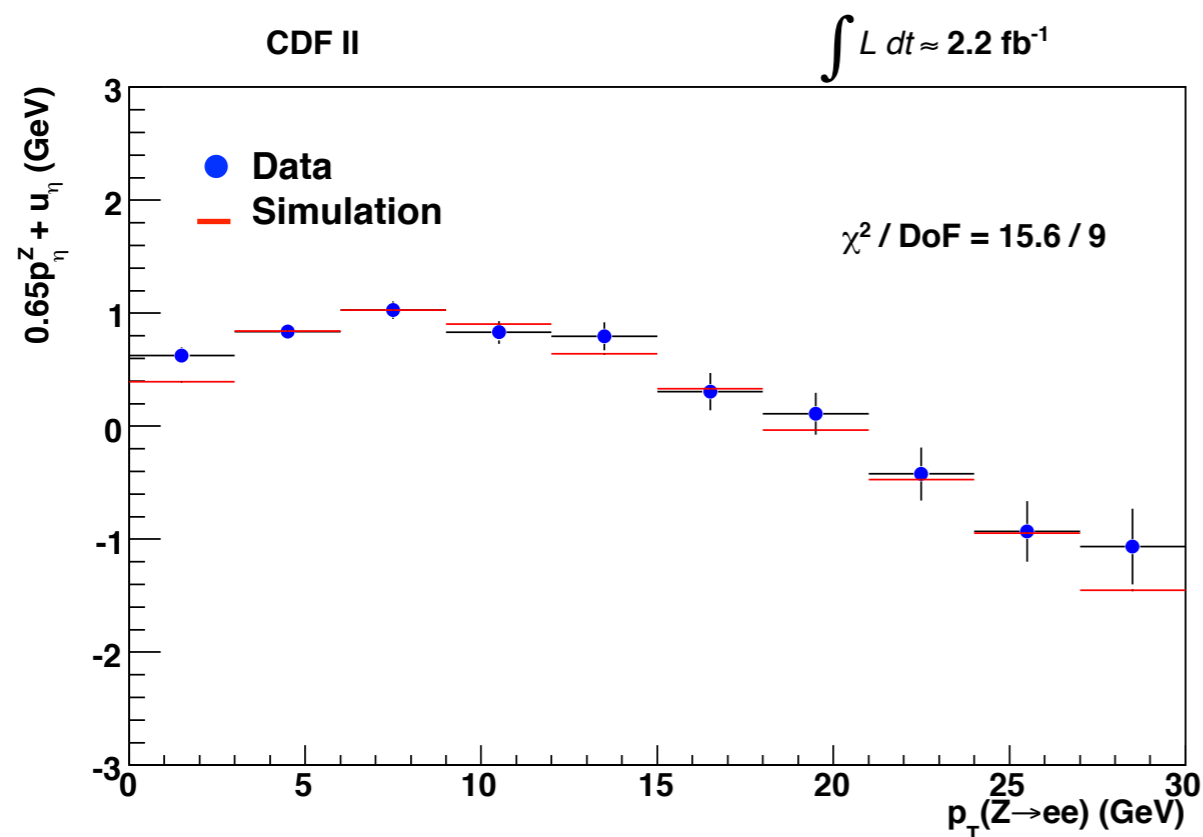
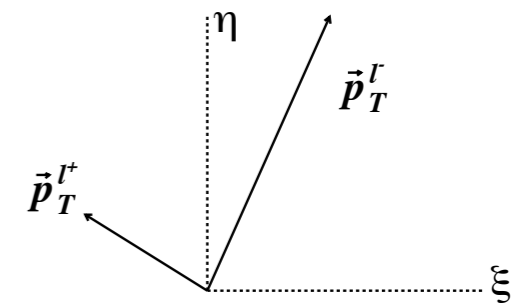
# Recoil model

---

- Parametrize recoil model and tune using data
- Two components
  1. Soft “spectator interaction” component
    - Randomly oriented ( $\sim 2$  additional interactions per event)
    - Model using minimum-bias data
  2. Hard “jet” component
    - Boson  $p_T$  dependent response and resolution
    - Tune by balancing boson  $p_T$  and recoil

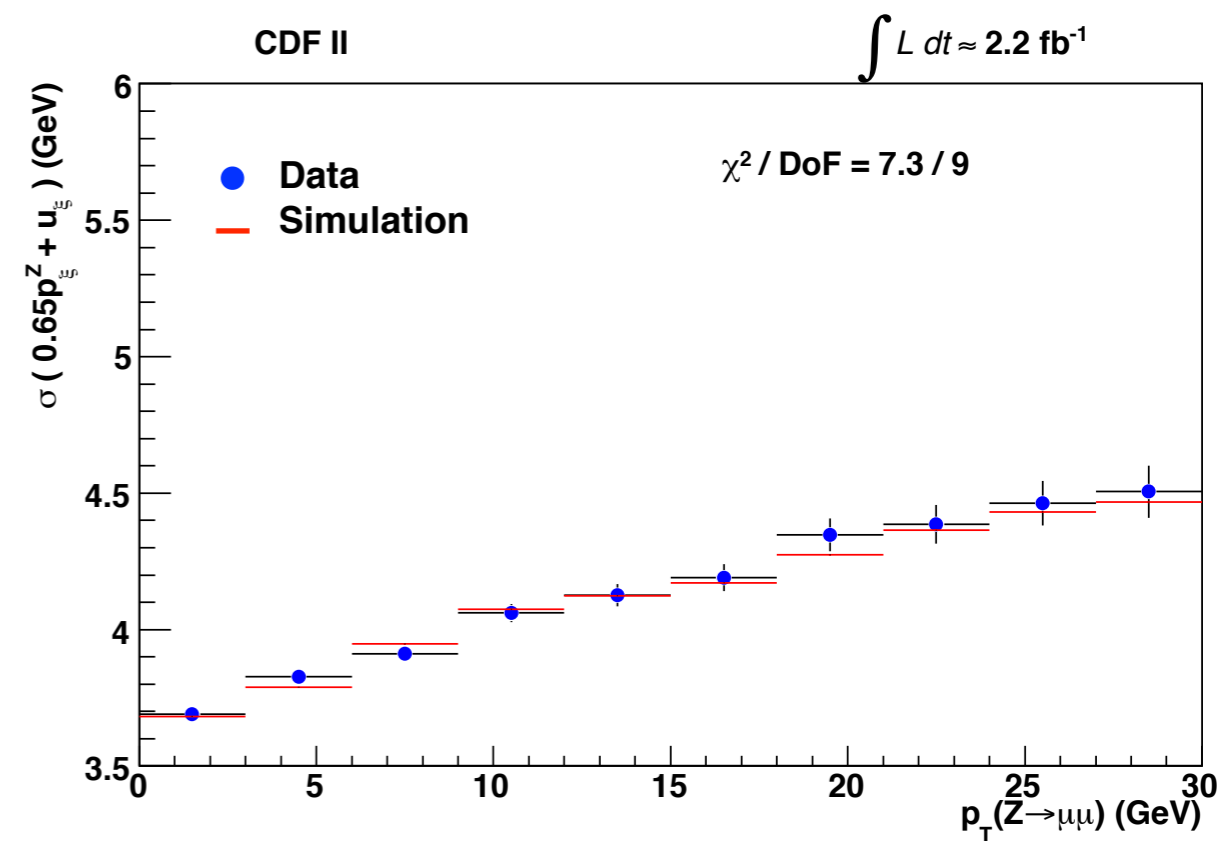
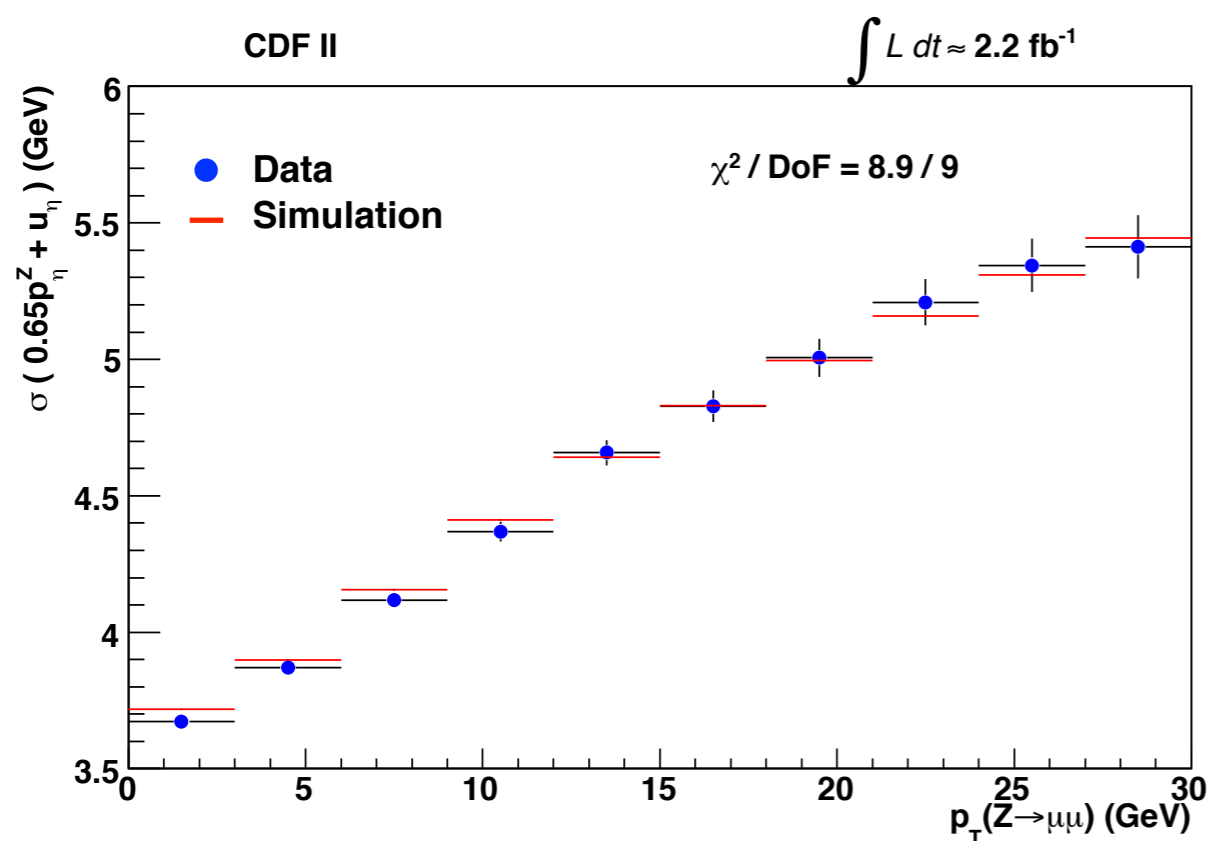
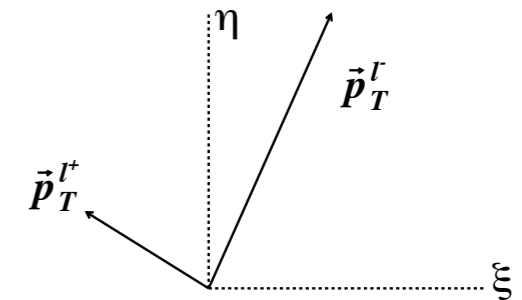
# Calibrating recoil response

- Recoil scale  $R = U_{meas} / U_{true}$ 
  - Calibrate by balancing  $Z p_T$  against  $p_T + u$  along eta axis  $\Delta M_W = 4 \text{ MeV}$



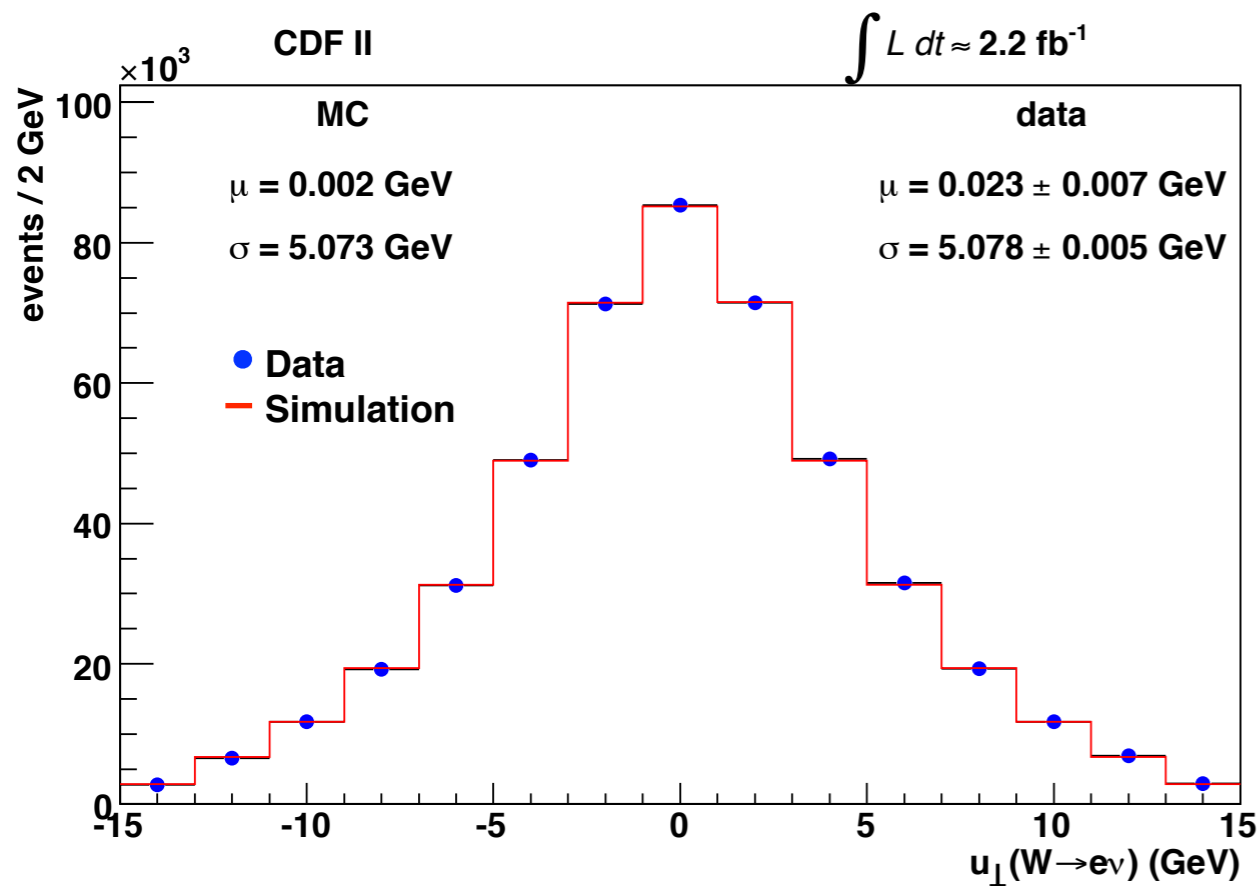
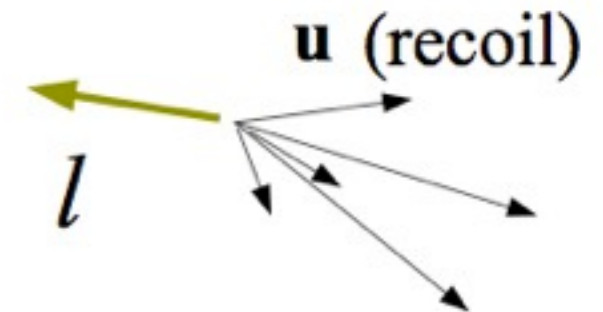
# Calibrating recoil resolution

- Recoil resolution
  - Calibrate balancing  $Z$   $p_T$  against  $\text{rms}(p_T+u)$  along both axes  $\Delta M_W = 4 \text{ MeV}$

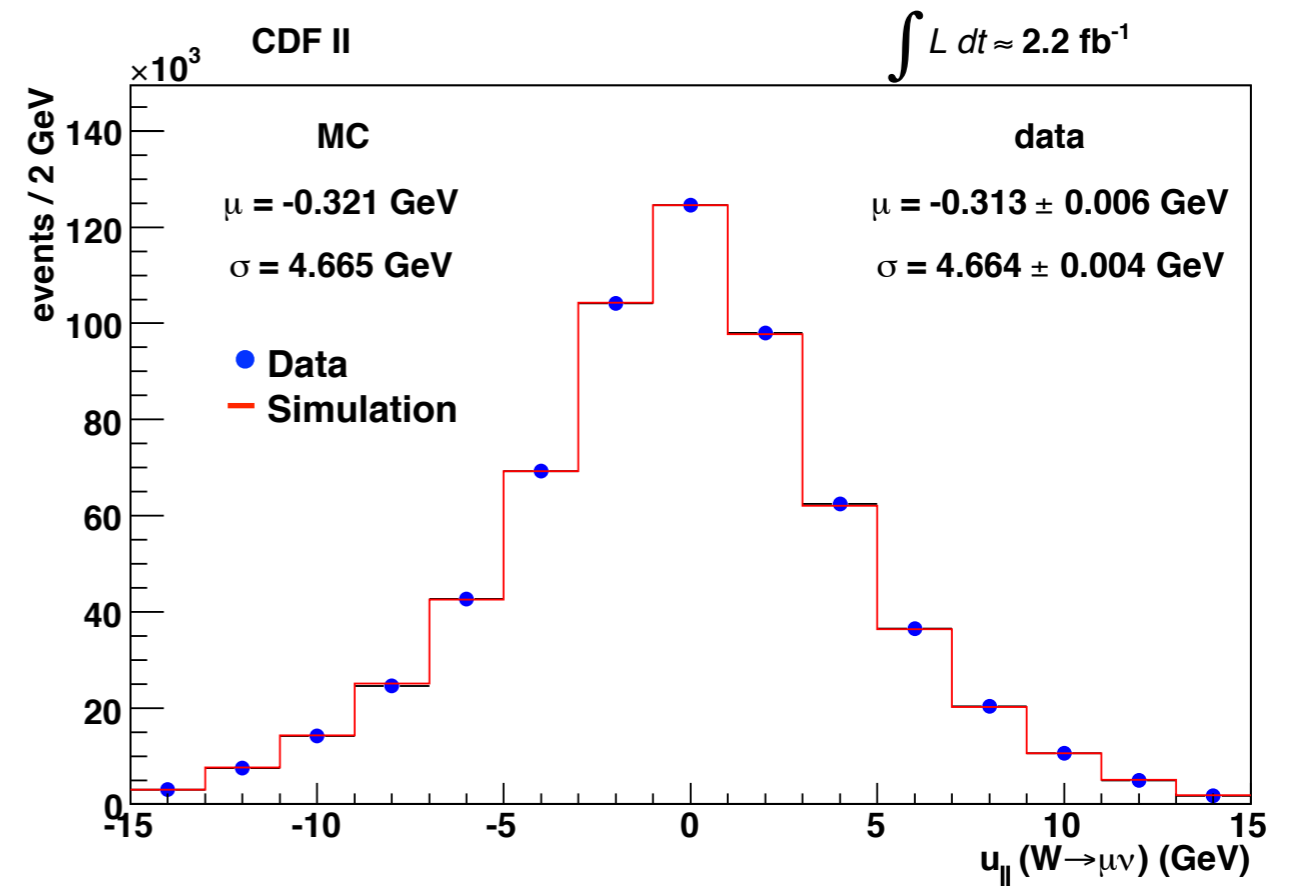


# Recoil validation

- Test recoil model with W events
  - Compare measured recoil in data to model tuned with Z



Recoil projection perpendicular to lepton (electrons)



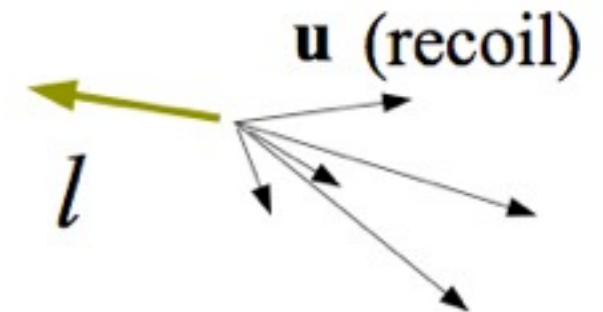
Recoil projection in direction of lepton (muons)

for  $u \ll p_T^l$  :

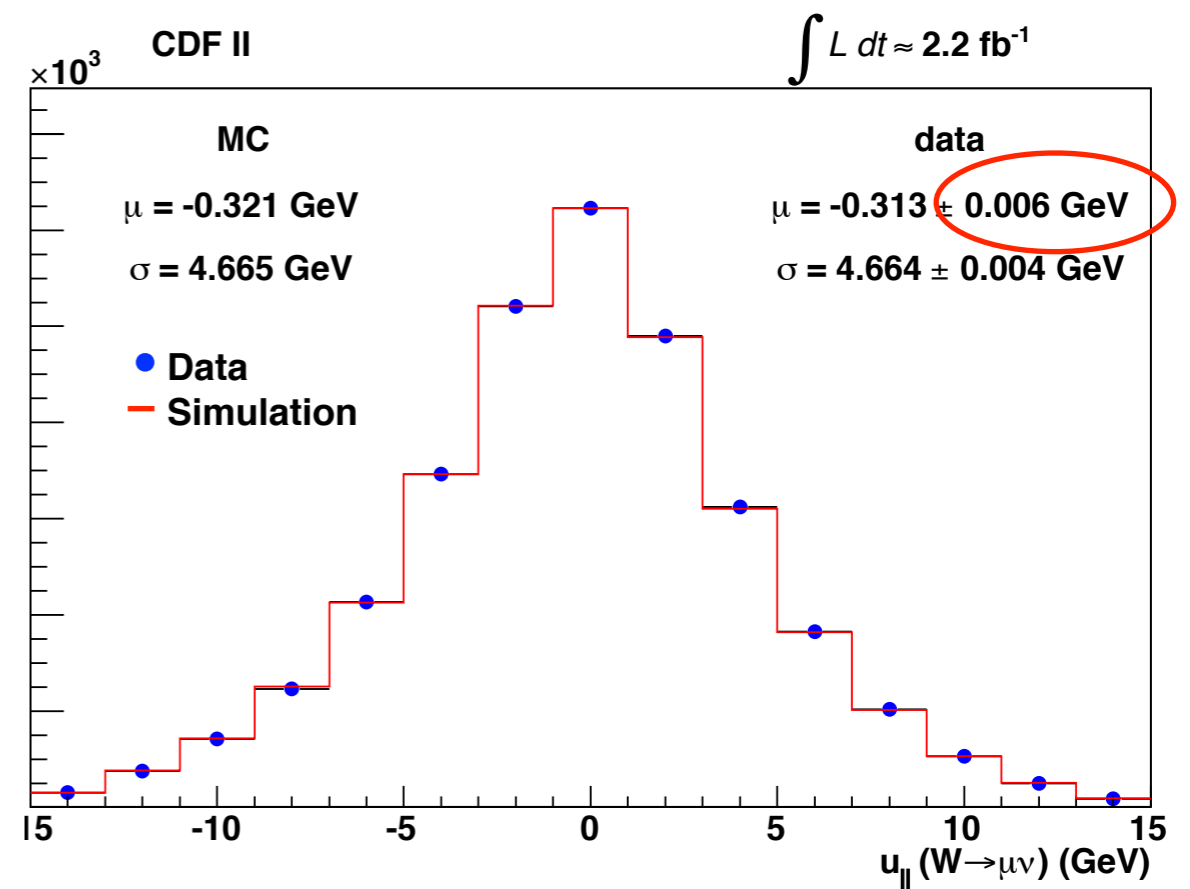
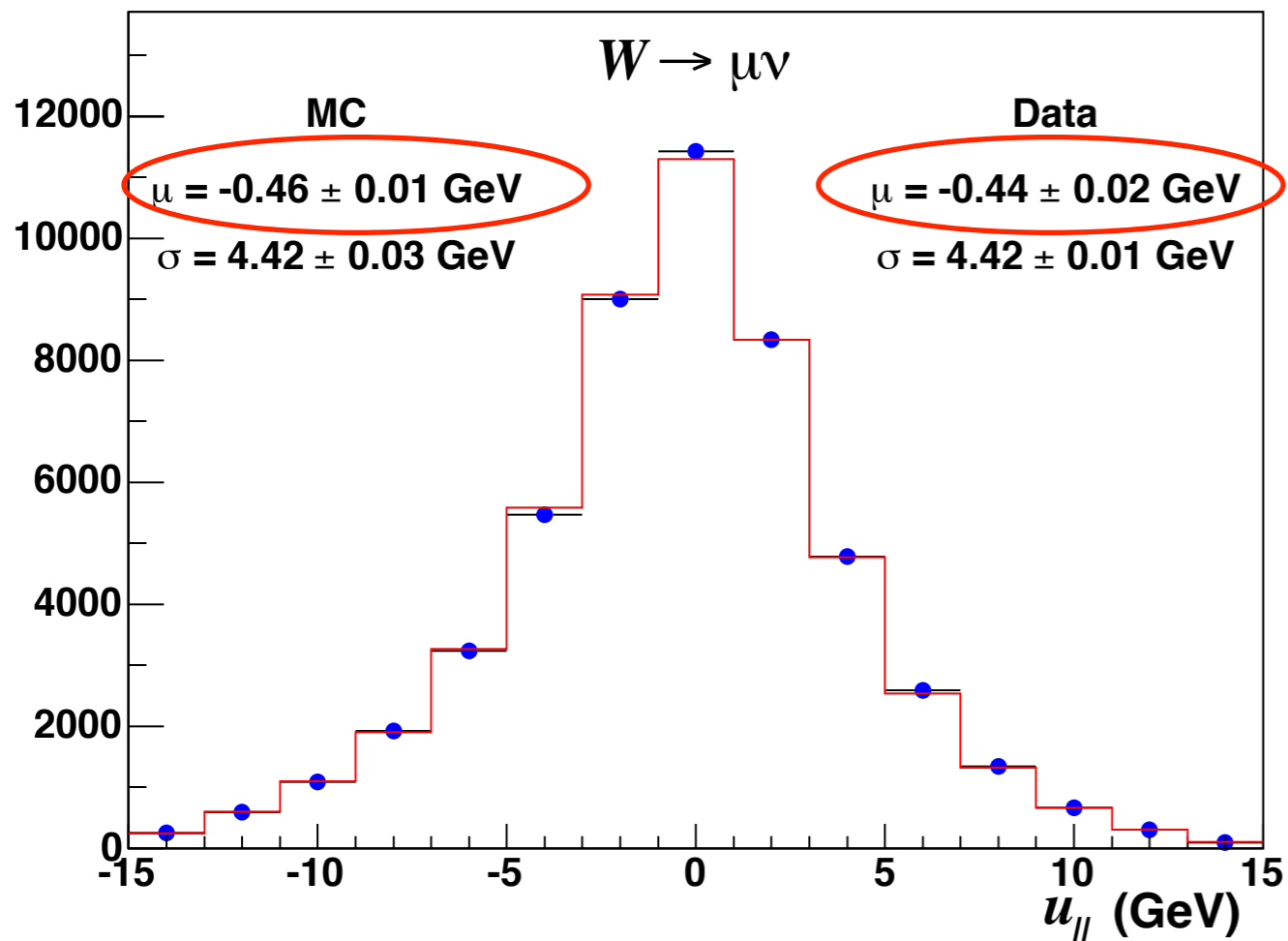
$$m_T \approx 2p_T^l + u_{\parallel}, \quad p_T^{\nu} \approx 2p_T^l + 2u_{\parallel}$$

# Recoil validation

- Test recoil model with W events
  - Compare measured recoil in data to model tuned with Z



$200 \text{ pb}^{-1}$  [PRD77:112001,2008]



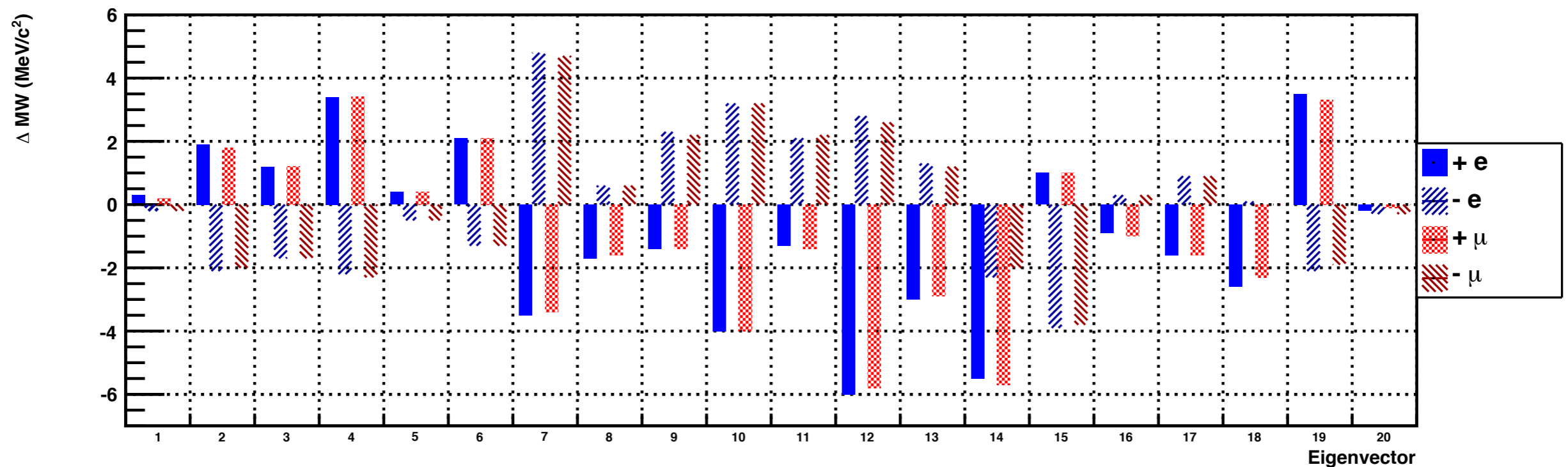
Recoil projection in direction of lepton (muons)

for  $u \ll p_T^l$ :

$$m_T \approx 2p_T^l + u_{||}, \quad p_T^v \approx 2p_T^l + 2u_{||}$$

# Parton distribution functions

- Utilize CTEQ6.6 PDF as default
- Evaluate 90% CL uncertainty eigenvectors for MSTW2008 and CTEQ6.6 (consistent)
- Use 68% CL MSTW2008 to determine systematic  $\Delta M_W = 10 \text{ MeV}$



# Backgrounds

- Electroweak backgrounds ( $Z \rightarrow ll$ ,  $W \rightarrow \tau\nu$ )
  - Model using standard CDF detector simulated MC
  - Tune recoil model and lepton response
- QCD backgrounds (hadronic jets, meson decay-in-flight)
  - Model using control regions in data
- Except  $Z \rightarrow \mu\mu$  (lost forward muon), backgrounds are small
- Include all estimated background shapes in final templates

Background	Fraction of W data (%)	$m_\tau$	$\Delta m_W$ (MeV)					
			$p_T^l$	$p_T^{\nu}$	$p_T^l$	$p_T^{\nu}$	$p_T^l$	$p_T^{\nu}$
$Z \rightarrow ll$	$7.35 \pm 0.09$	$0.139 \pm 0.014$	2	1	4	2	5	1
$W \rightarrow \tau\nu$	$0.880 \pm 0.004$	$0.93 \pm 0.01$	0	1	0	1	0	1
QCD	$0.035 \pm 0.025$	$0.39 \pm 0.14$	1	4	1	2	1	4
Decay-in-flight	$0.24 \pm 0.02$		1		3		1	
Cosmic Rays	$0.02 \pm 0.02$		1		1		1	
<i>Total</i>			3	4	5	3	6	4

muons
electrons

# Results

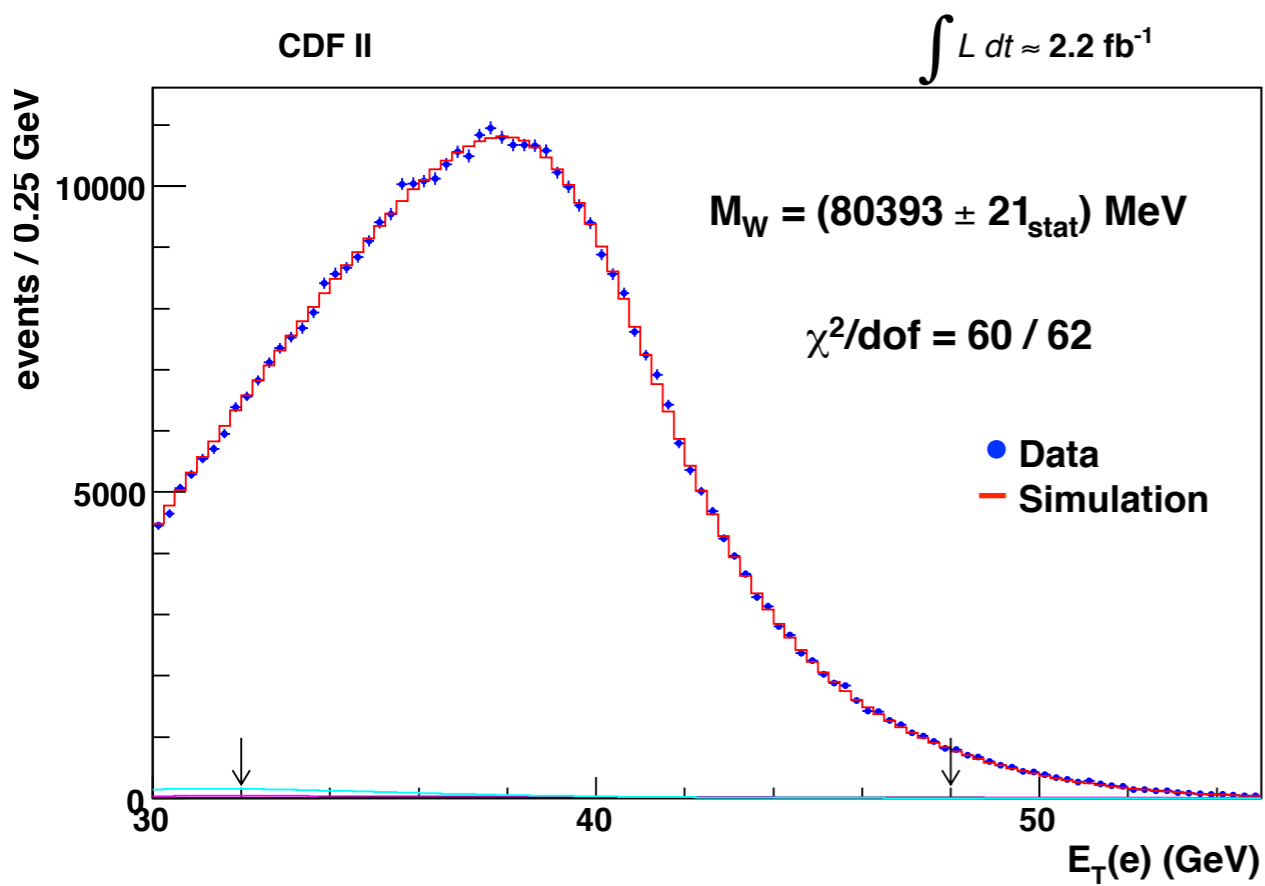


# A word on blinding

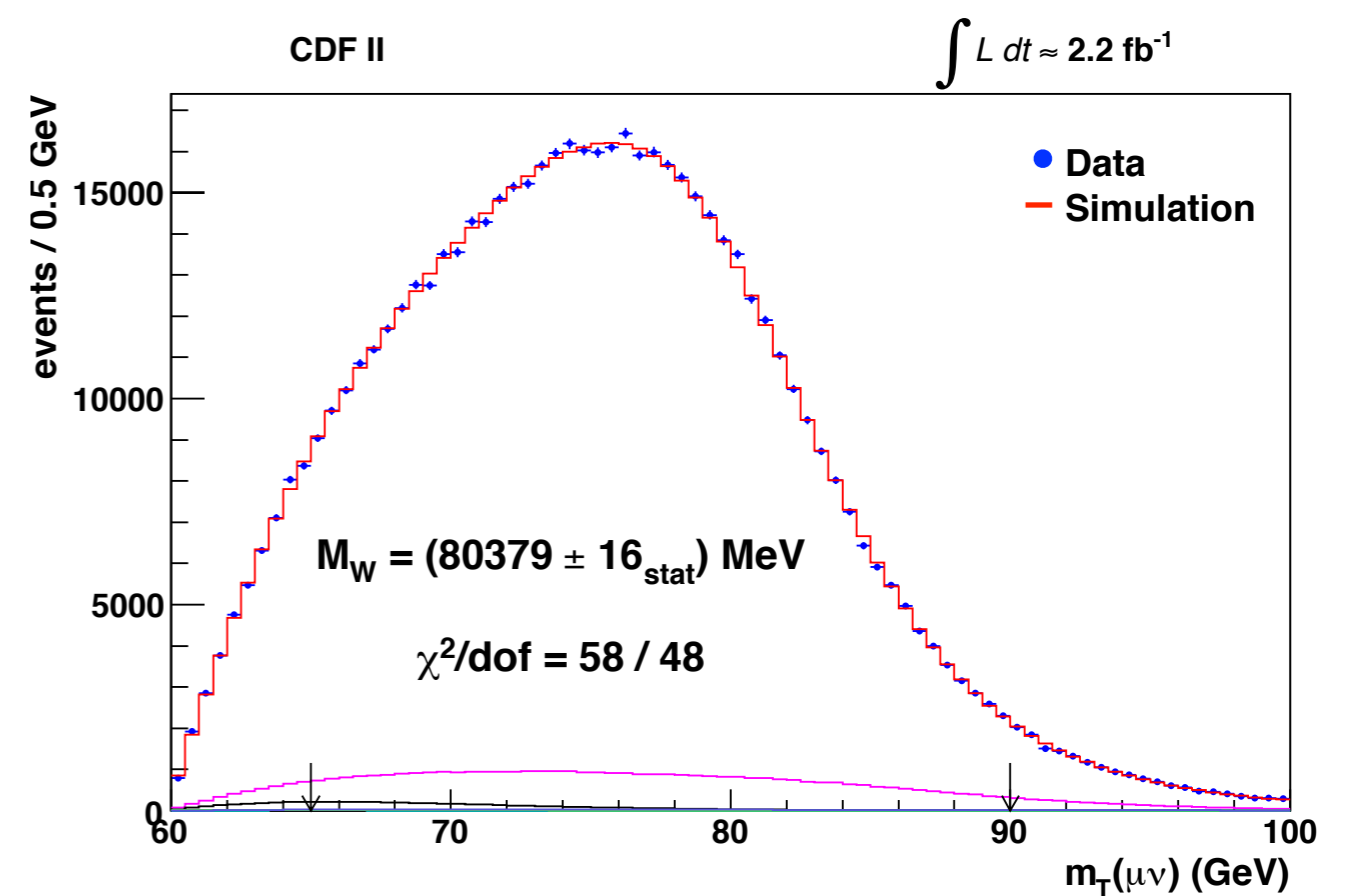
---

- During development of analysis, all fits **blinded** with random offset from  $[-75,75]$  MeV
  - Common offset applied to all six mass fits
    - Allows for comparison and cross-check
  - During calibration of energy scales, separate offset applied to Z mass fits
- Blinding offset removed only after analysis frozen
  - No changes made since removal

# Example mass fits



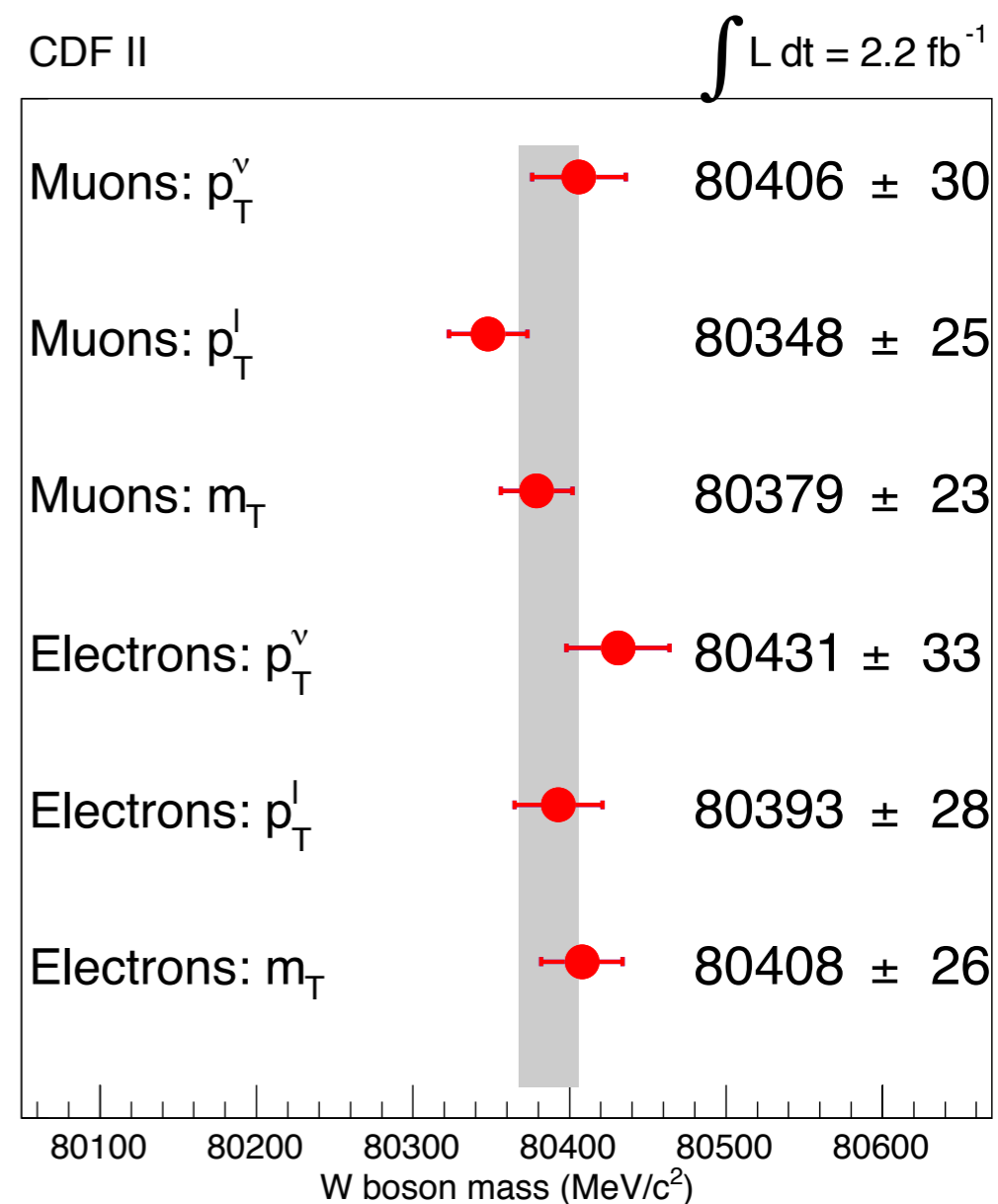
$p_T^l$ : electrons



$m_T$ : muons

# All fits

Fit	Fit result (MeV)	$\chi^2/\text{dof}$
$W \rightarrow e\nu$ ( $m_T$ )	$80408 \pm 19_{\text{stat}} \pm 18_{\text{syst}}$	52/48
$W \rightarrow e\nu$ ( $p_T^l$ )	$80393 \pm 21_{\text{stat}} \pm 19_{\text{syst}}$	60/62
$W \rightarrow e\nu$ ( $p_T^\nu$ )	$80431 \pm 25_{\text{stat}} \pm 22_{\text{syst}}$	71/62
$W \rightarrow \mu\nu$ ( $m_T$ )	$80379 \pm 16_{\text{stat}} \pm 16_{\text{syst}}$	58/48
$W \rightarrow \mu\nu$ ( $p_T^l$ )	$80348 \pm 18_{\text{stat}} \pm 18_{\text{syst}}$	54/62
$W \rightarrow \mu\nu$ ( $p_T^\nu$ )	$80406 \pm 22_{\text{stat}} \pm 20_{\text{syst}}$	79/62



# Combined results

---

Combine using *BLUE*  
L. Lyons, D. Gibaut, and P. Clifford,  
NIM A **270**, 110 (1988).

# Combined results

---

- All electron fits combined

$$M_W = 80406 \pm 25 \text{ MeV}, \chi^2/\text{dof} = 1.4/2 (49\%)$$

Combine using *BLUE*  
L. Lyons, D. Gibaut, and P. Clifford,  
NIM A **270**, 110 (1988).

# Combined results

---

- All electron fits combined

$$M_W = 80406 \pm 25 \text{ MeV}, \chi^2/\text{dof} = 1.4/2 (49\%)$$

- All muon fits combined

$$M_W = 80374 \pm 22 \text{ MeV}, \chi^2/\text{dof} = 4/2 (12\%)$$

Combine using *BLUE*  
L. Lyons, D. Gibaut, and P. Clifford,  
NIM A **270**, 110 (1988).

# Combined results

---

- All electron fits combined

$$M_W = 80406 \pm 25 \text{ MeV}, \chi^2/\text{dof} = 1.4/2 (49\%)$$

- All muon fits combined

$$M_W = 80374 \pm 22 \text{ MeV}, \chi^2/\text{dof} = 4/2 (12\%)$$

- All fits combined

$$M_W = 80387 \pm 19 \text{ MeV}, \chi^2/\text{dof} = 6.6/5 (25\%)$$

Combine using *BLUE*  
L. Lyons, D. Gibaut, and P. Clifford,  
NIM A **270**, 110 (1988).

# Combined uncertainties

---

<b>Source</b>	<b>Uncertainty 2.2 fb<sup>-1</sup> (MeV)</b>
Lepton energy scale	7
Lepton energy resolution	2
Recoil energy scale	4
Recoil energy resolution	4
Lepton removal	2
Backgrounds	3
p <sub>T</sub> (W) model	5
PDFs	10
QED radiation	4
<i>Total systematics</i>	<i>15</i>
W statistics	12
<b>Total</b>	<b>19</b>

$$M_W = 80387 \pm 12_{\text{stat}} \pm 15_{\text{syst}} \text{ MeV}/c^2$$



# Combined uncertainties

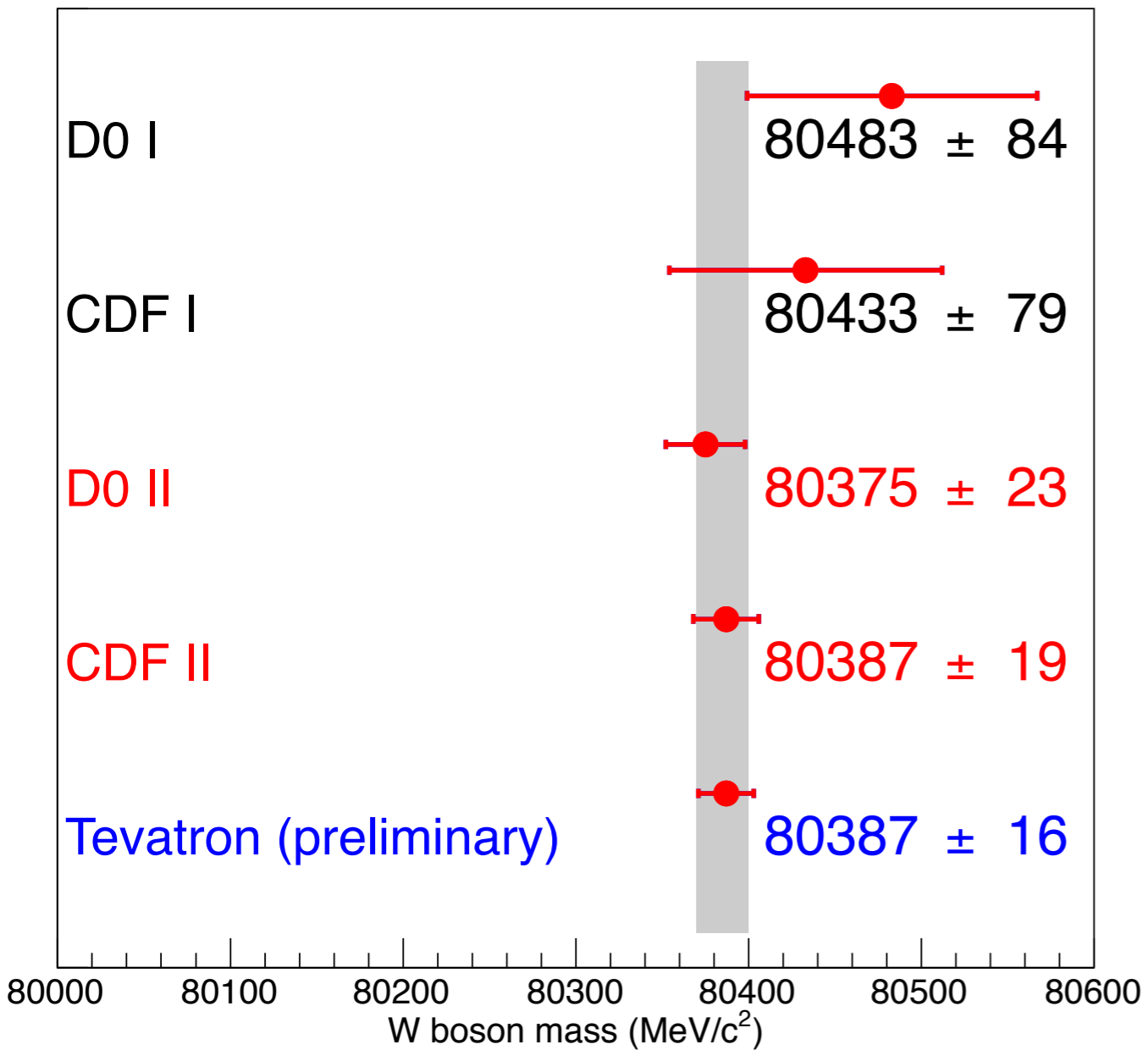
Source	Uncertainty 2.2 fb <sup>-1</sup> (MeV)	Uncertainty 0.2 fb <sup>-1</sup> (MeV)
Lepton energy scale	7	23
Lepton energy resolution	2	4
Recoil energy scale	4	8
Recoil energy resolution	4	10
Lepton removal	2	6
Backgrounds	3	6
p <sub>T</sub> (W) model	5	4
PDFs	10	11
QED radiation	4	10
<i>Total systematics</i>	<i>15</i>	<i>34</i>
W statistics	12	34
<b>Total</b>	<b>19</b>	<b>48</b>

Statistics limited by  
control data

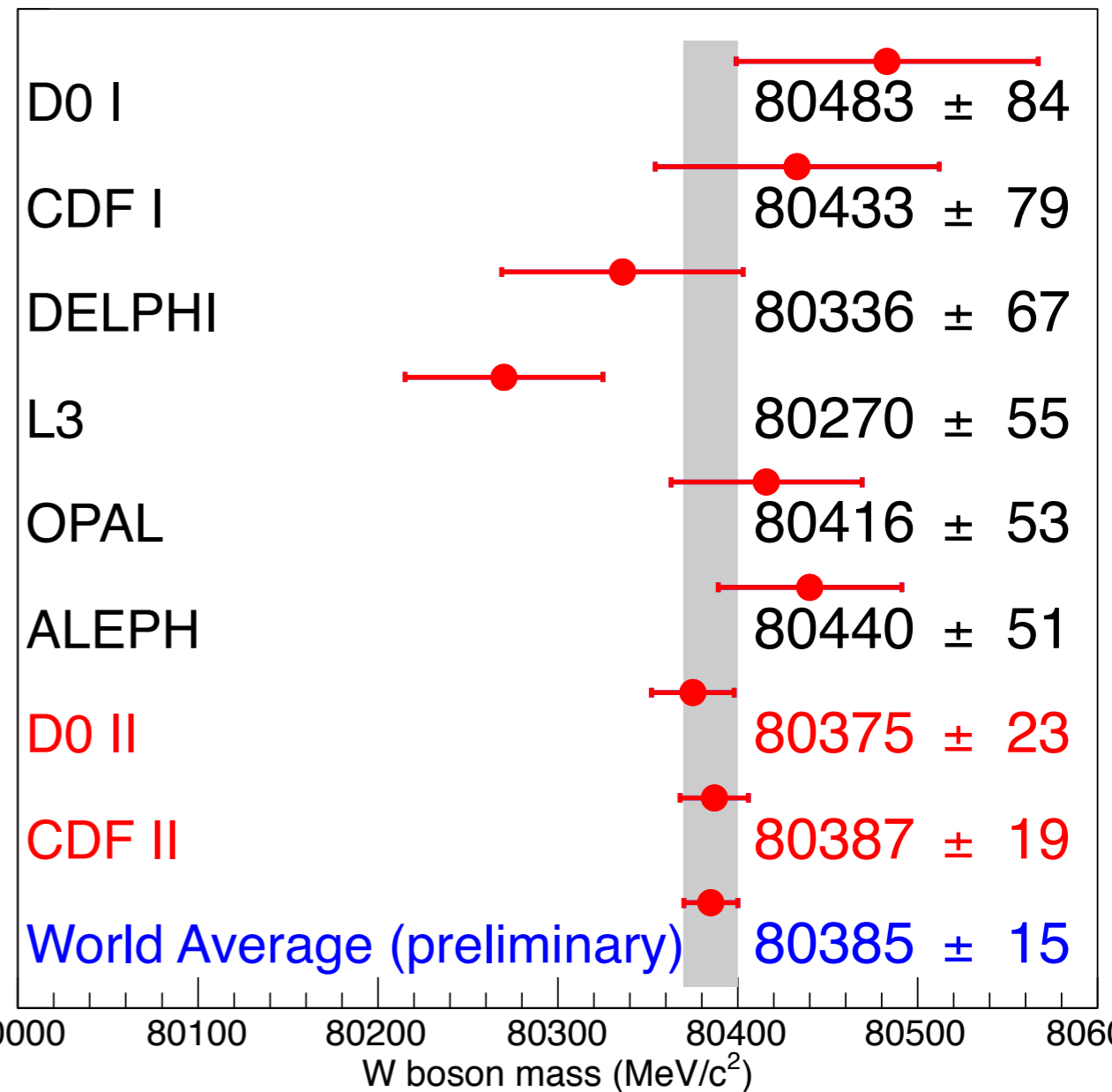
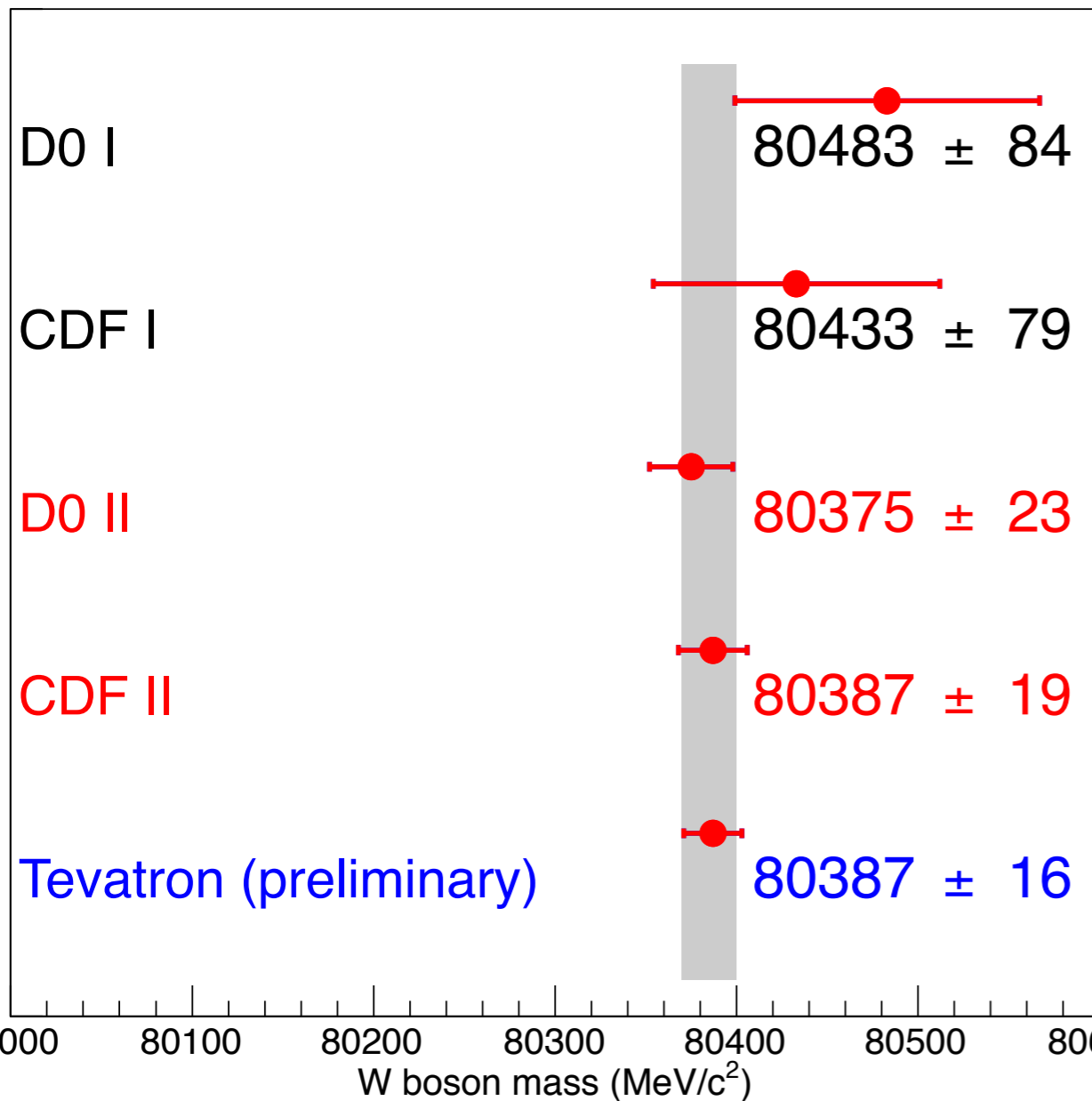
Theory based  
(external inputs)

$$M_W = 80387 \pm 12_{\text{stat}} \pm 15_{\text{syst}} \text{ MeV}/c^2$$

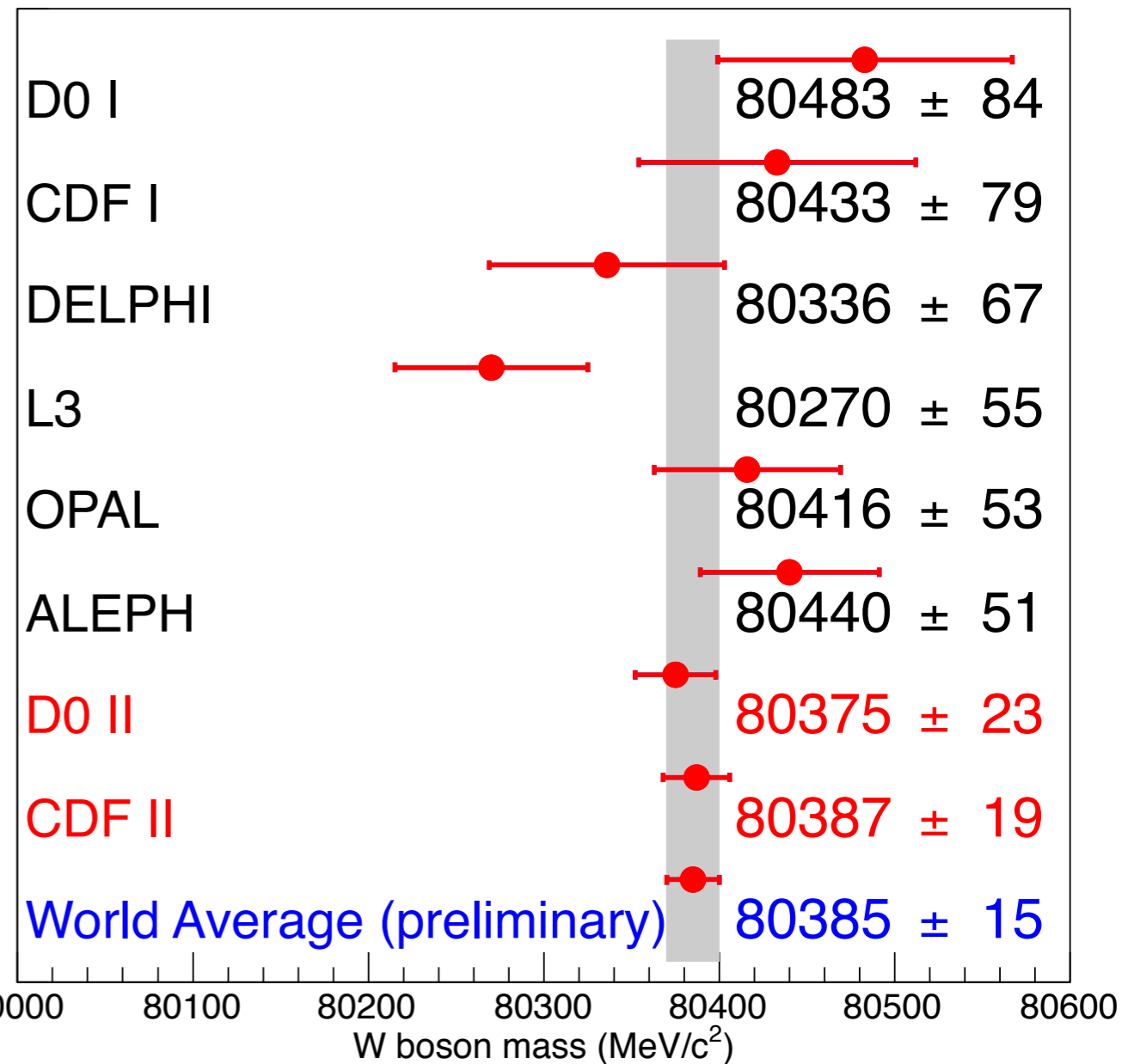
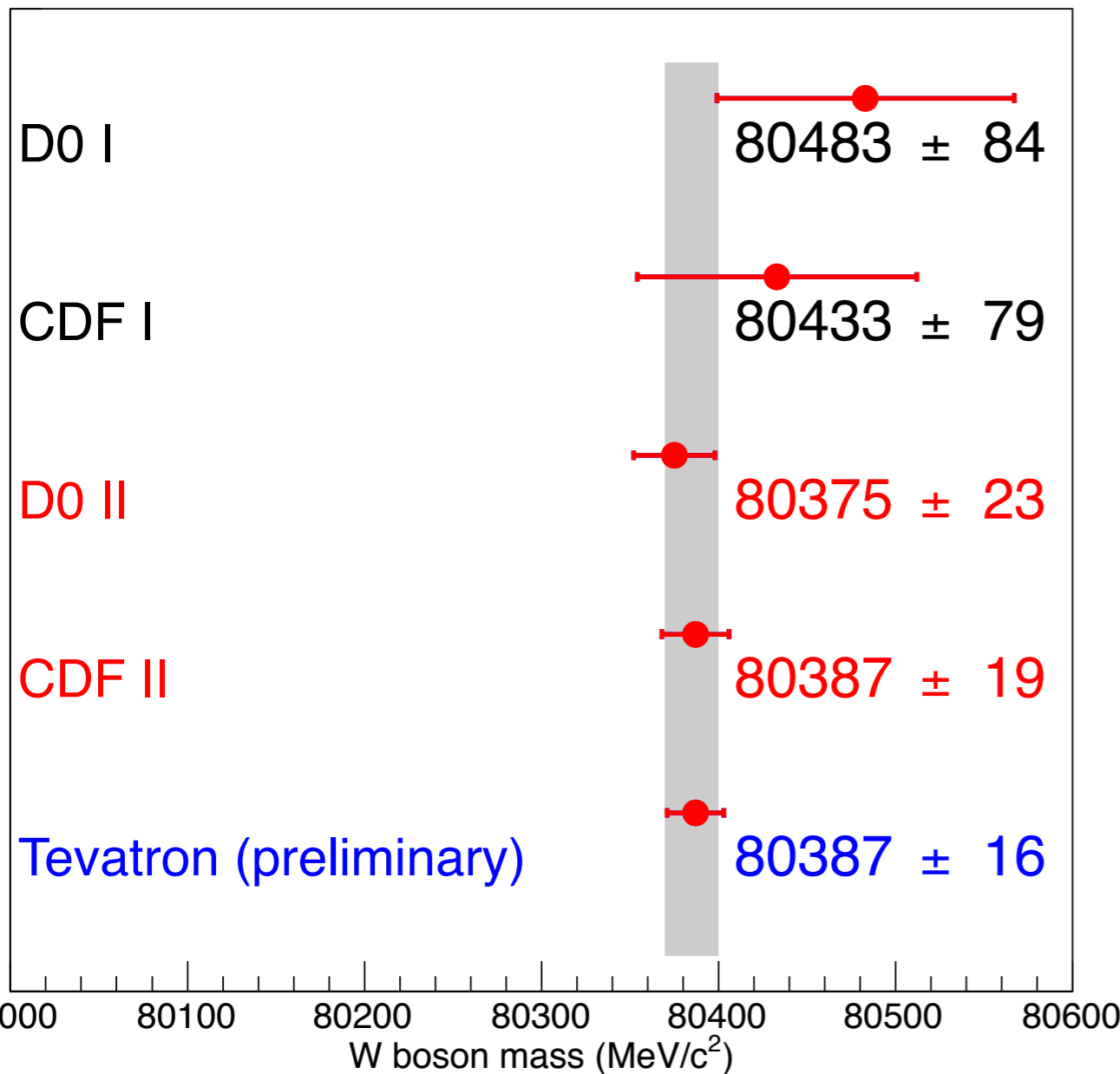
# Tevatron and world combinations



# Tevatron and world combinations



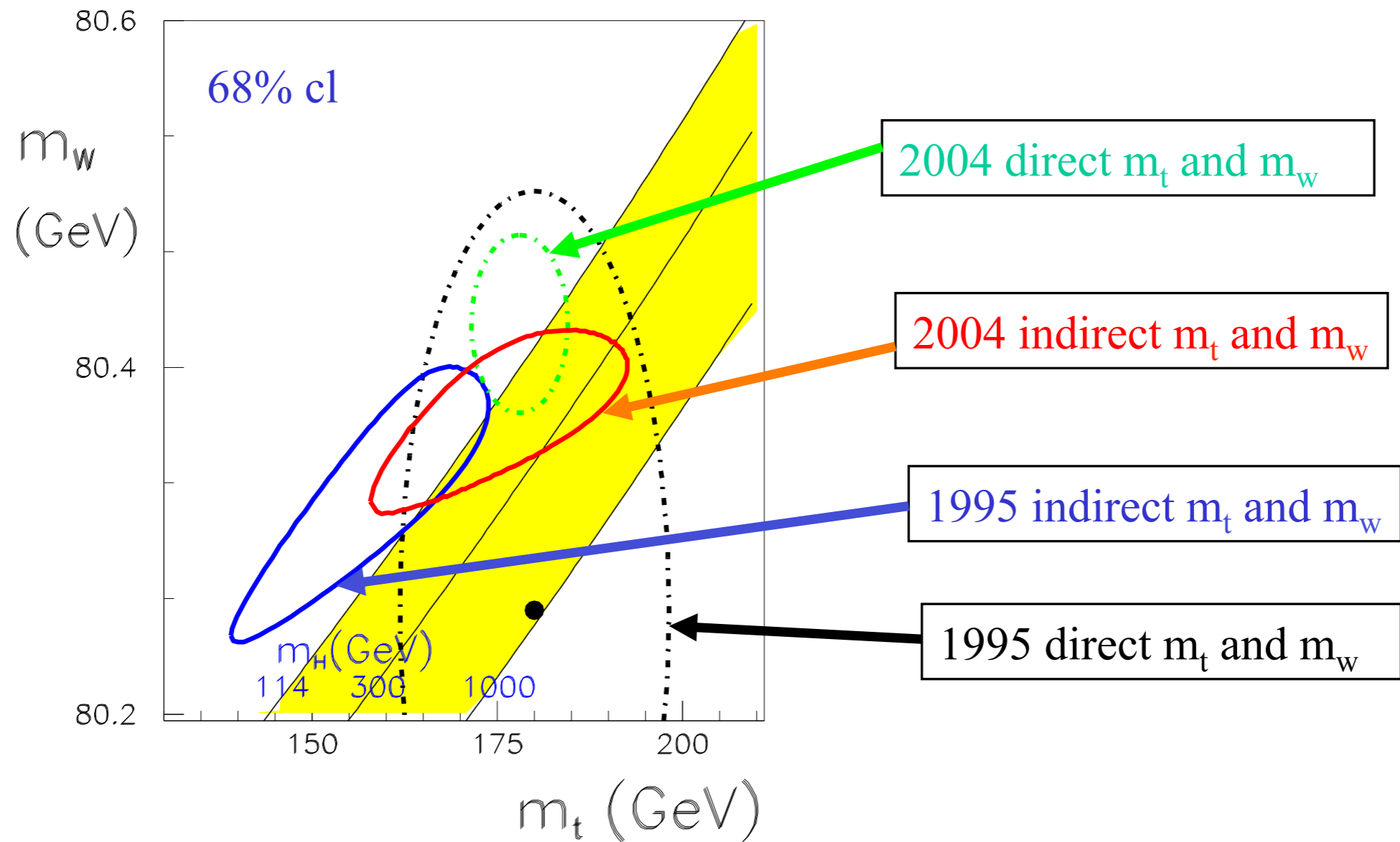
# Tevatron and world combinations



*nb:* 2009 world average  
 $M_W = 80399 \pm 23$  MeV

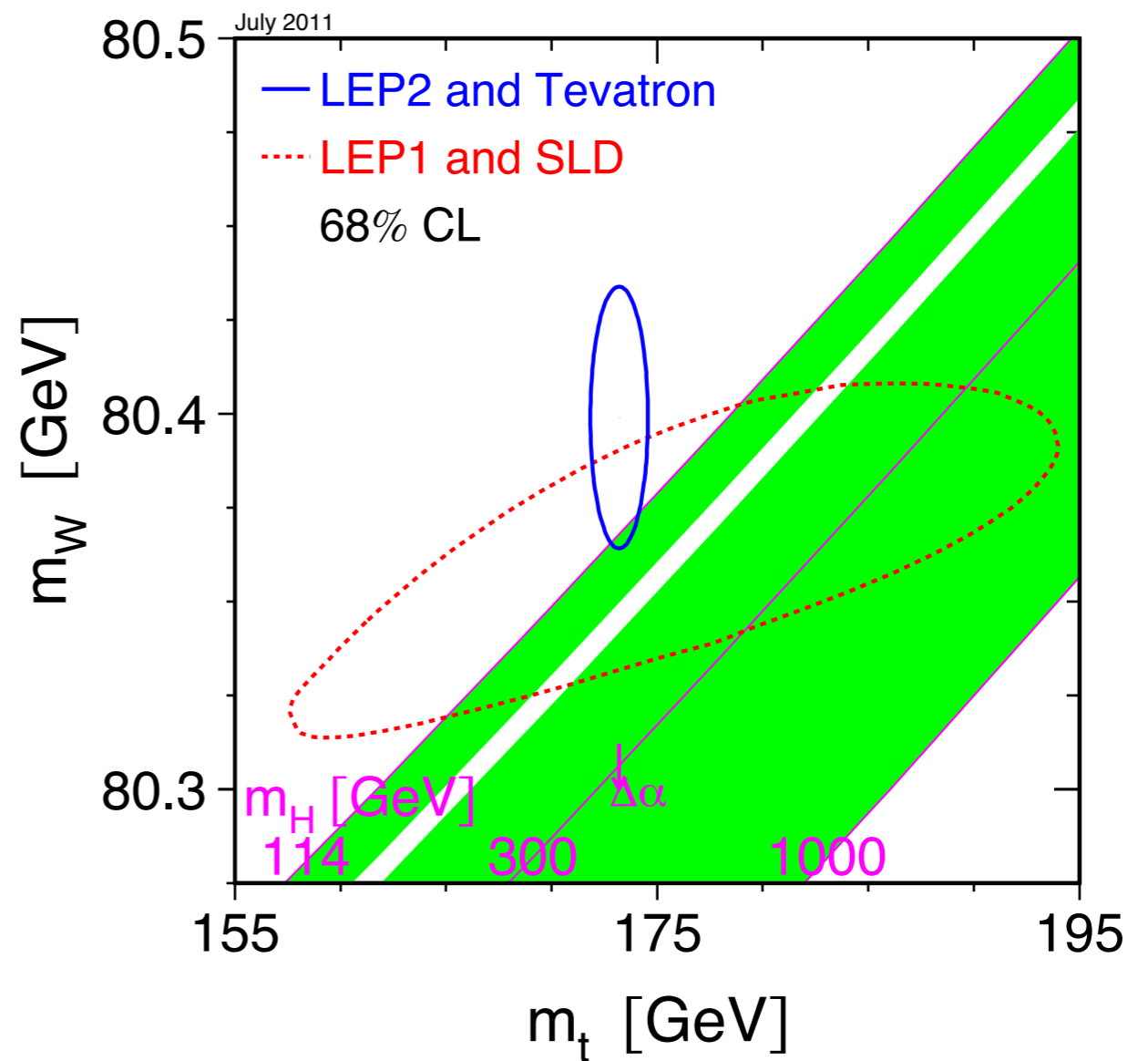
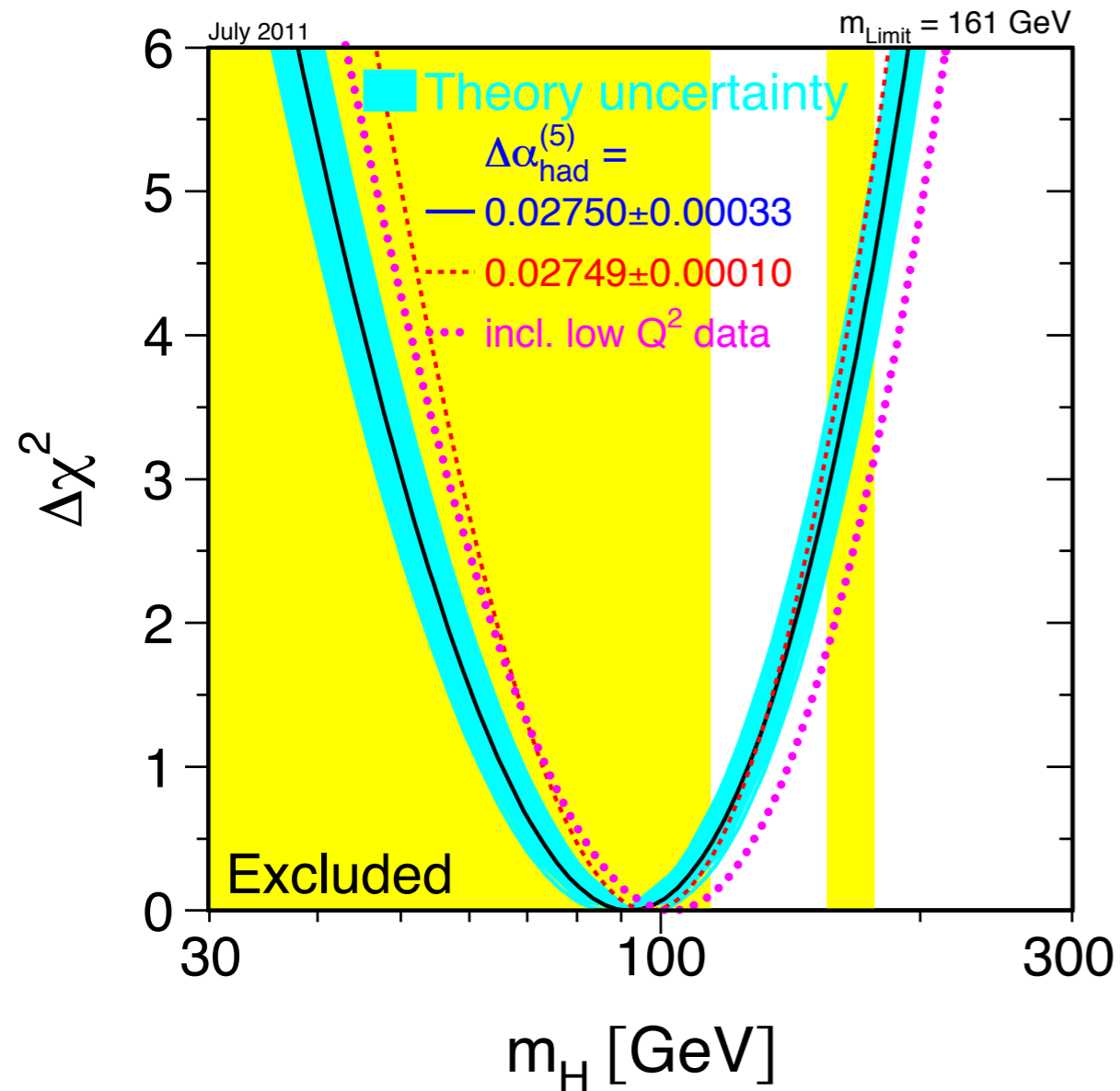
*New CDF measurement significantly exceeds precision of all previous measurements of  $M_W$  combined!*

# Sidetrack down memory lane



**P. Renton, ICHEP 2004**

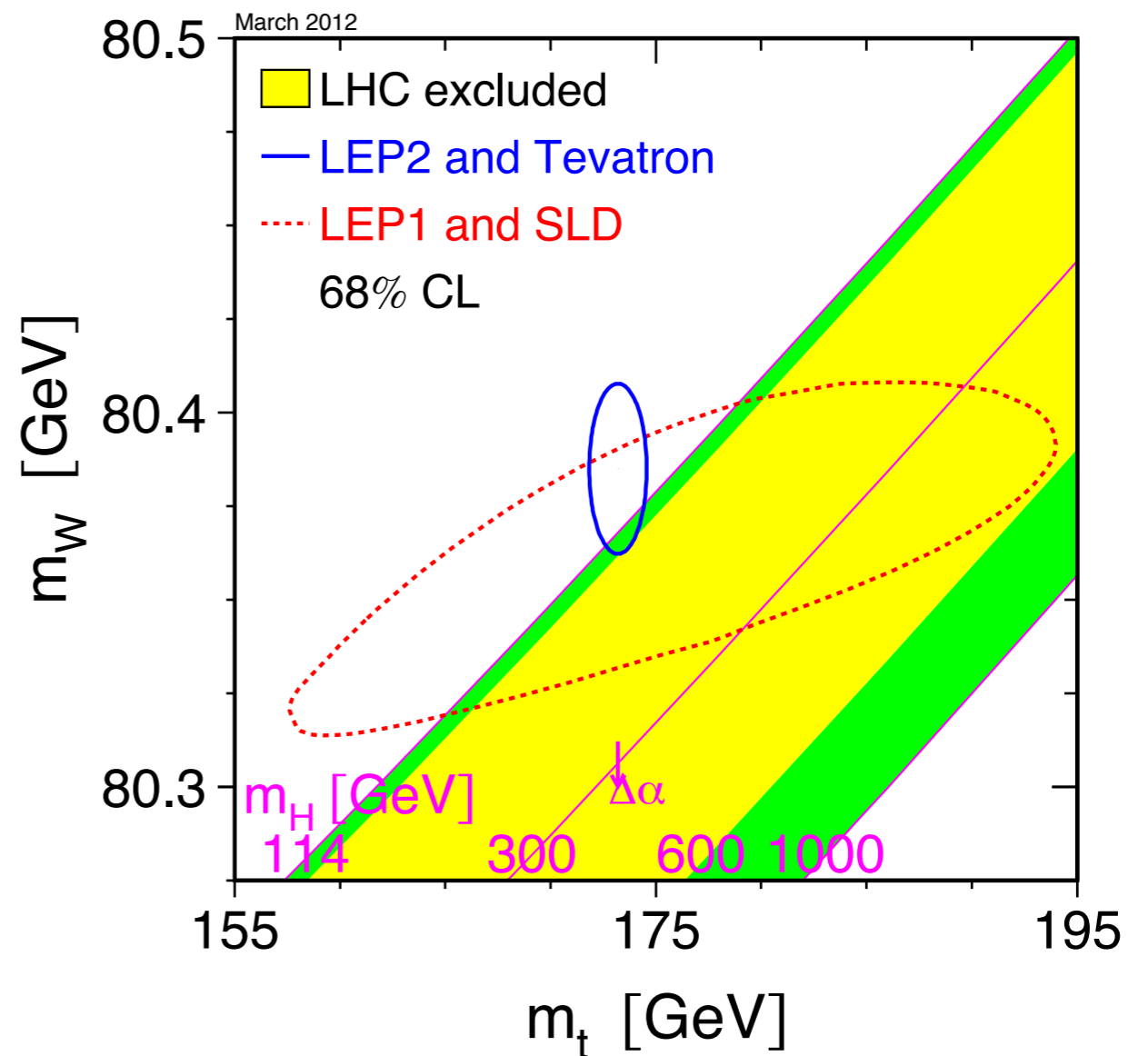
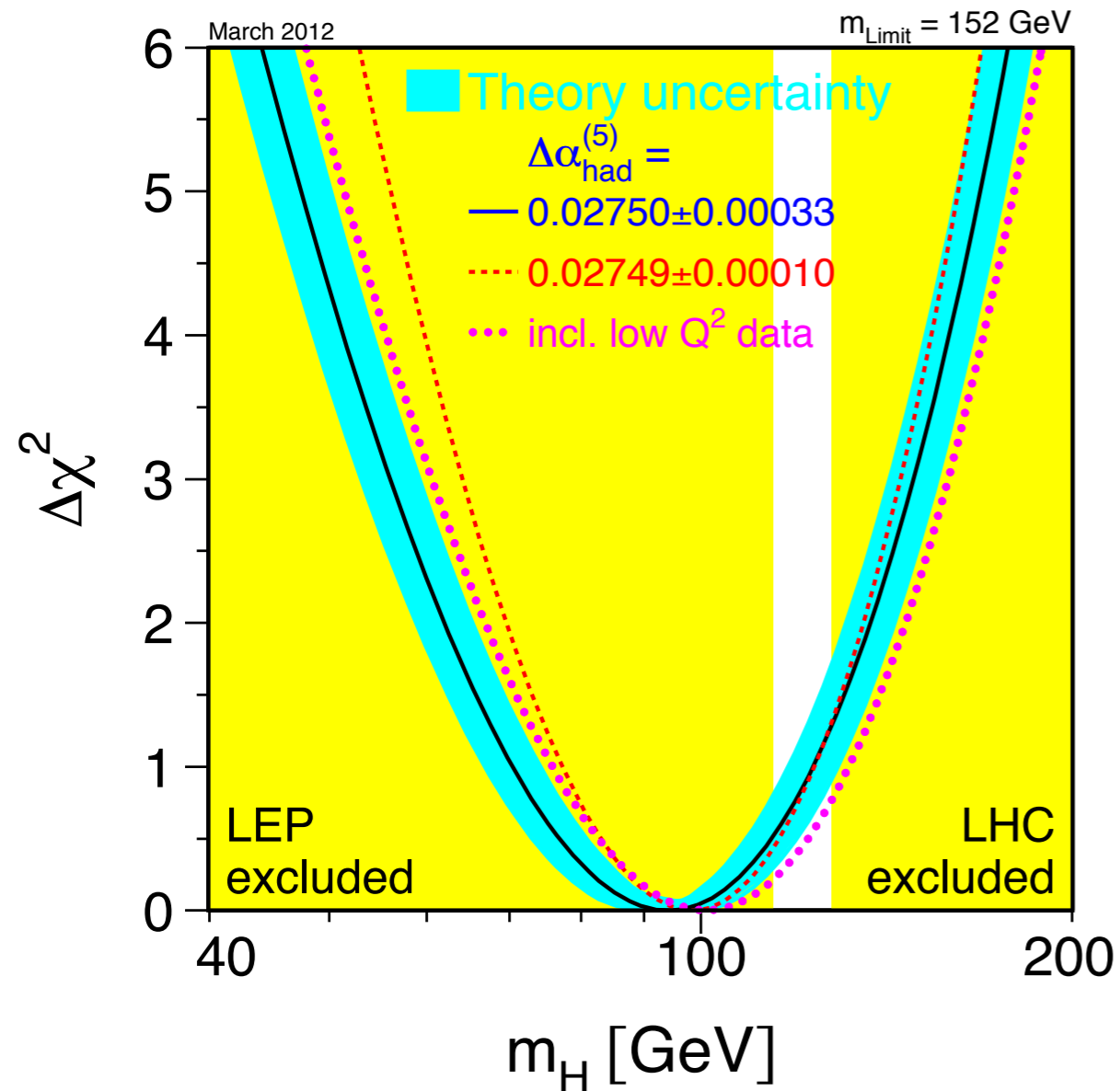
# Standard model fit



As of July 2011:  
 $m_{\text{H}} = 92^{+34}_{-26} \text{ GeV}$   
 $m_{\text{H}} < 161 \text{ GeV @95\% CL}$

Fits and plots from **LEPEWWG**

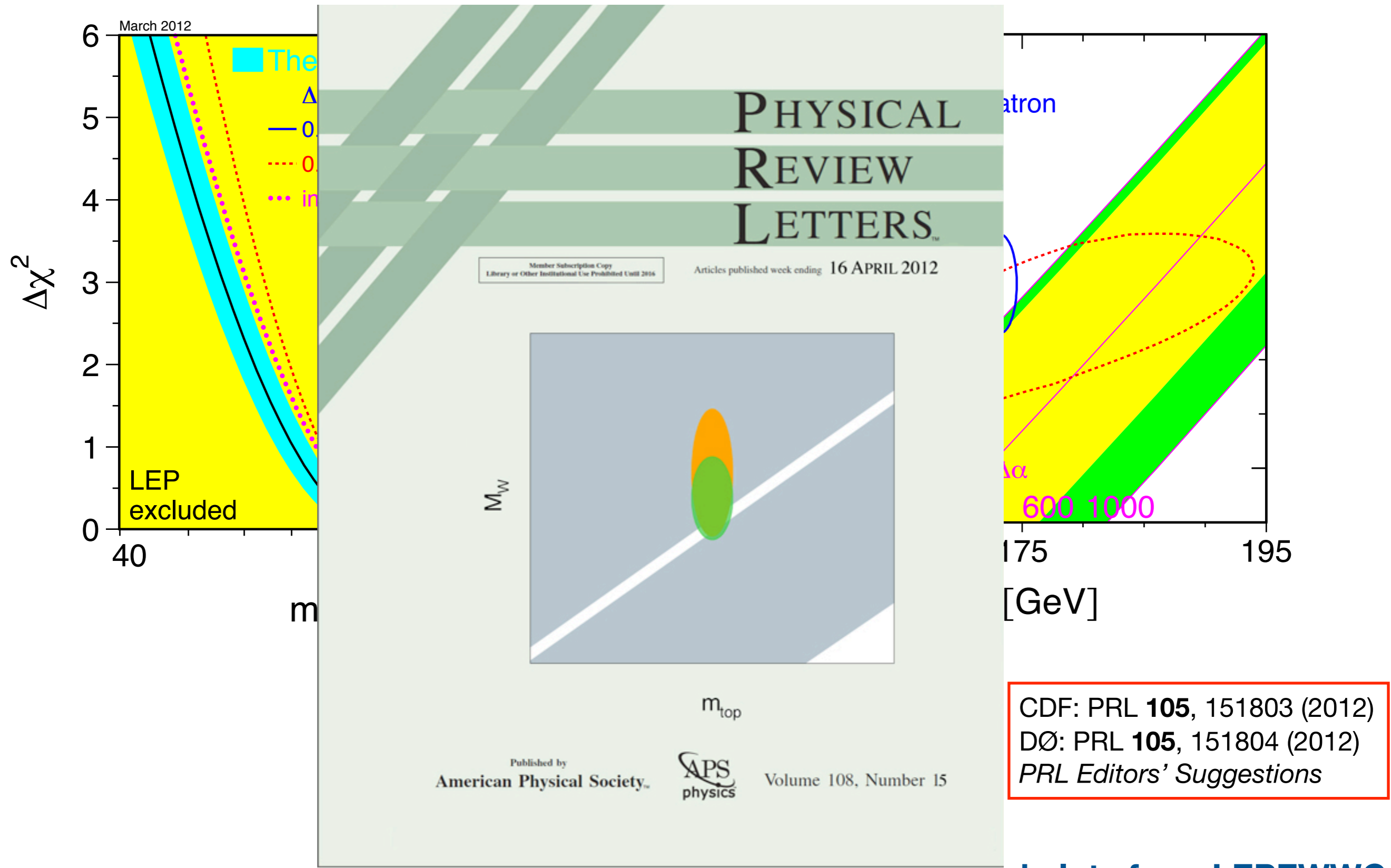
# Standard model fit



As of March 2012:  
 $m_H = 94^{+29}_{-24} \text{ GeV}$   
 $m_H < 152 \text{ GeV @95\% CL}$

Fits and plots from **LEPEWWG**

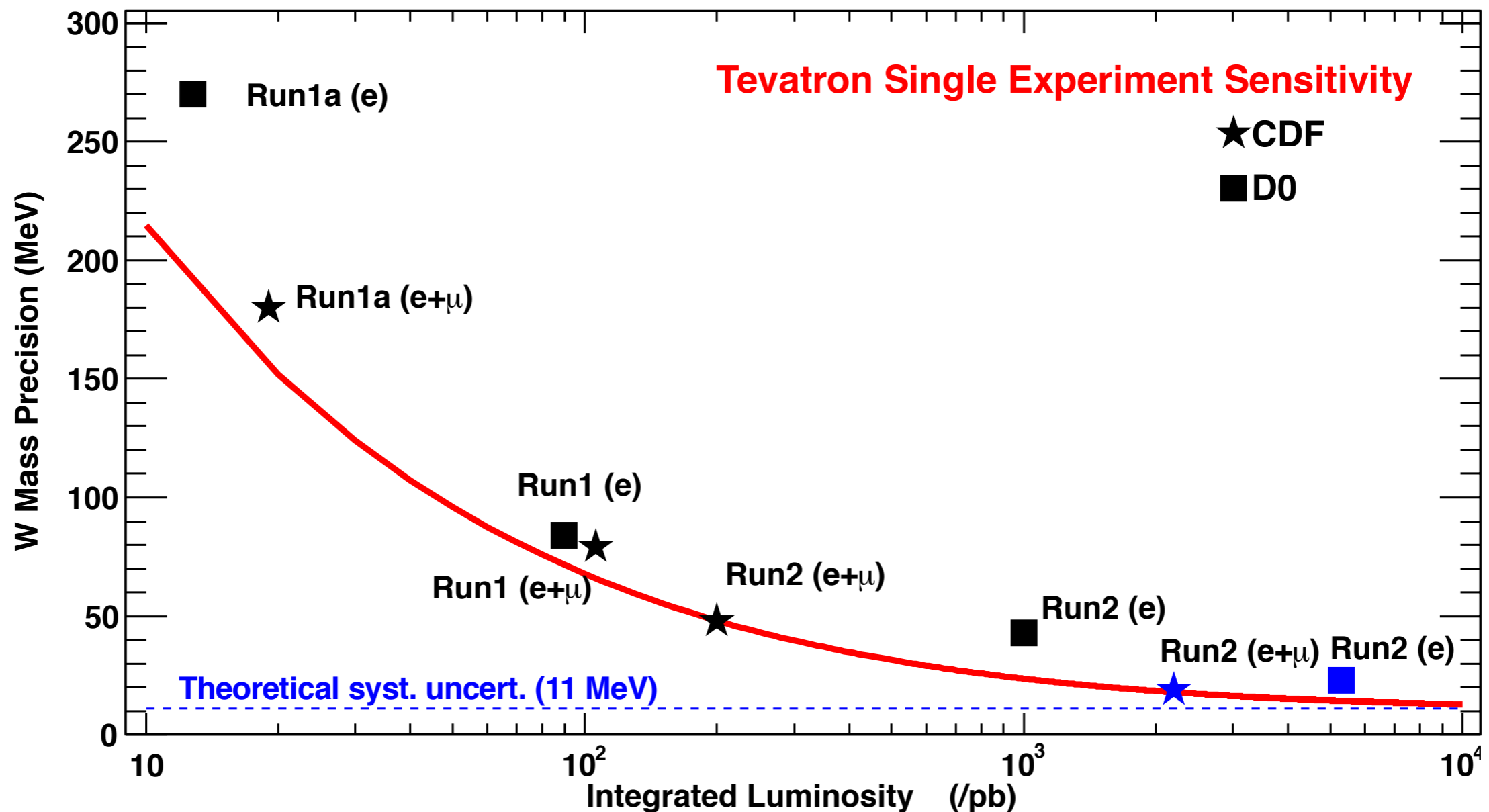
# Standard model fit



Fits and plots from **LEPEWWG**



# Uncertainty projections



- Projection assumes PDF+QED errors (11 MeV) fixed
  - Become limiting uncertainty for measurements with full Tevatron dataset

# Conclusion

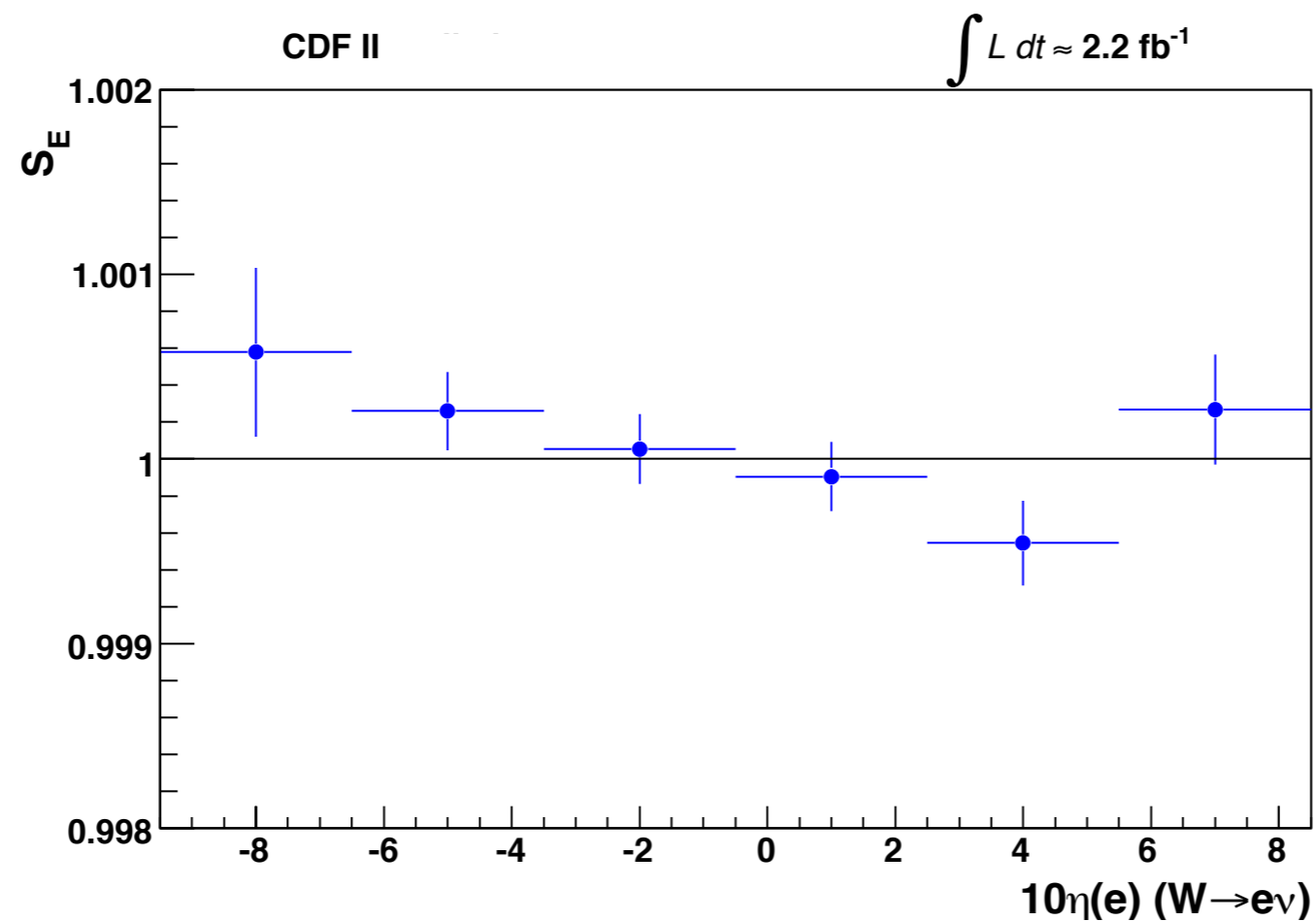
---

- CDF has performed the most precise measurement of the  $W$  boson mass
  - $M_W = 80387 \pm 19 \text{ MeV}$  [*Phys. Rev. Lett.* **105**, 158103]
  - More precise than all previous measurements combined
  - Improves world average uncertainty from 23 MeV to 16 MeV
- New combinations (including DØ [*Phys. Rev. Lett.* **105**, 158104])
  - **Tevatron:**  $M_W = 80387 \pm 16 \text{ MeV}$  (TeVWWG, preliminary)
  - **World:**  $M_W = 80385 \pm 15 \text{ MeV}$  (TeVWWG, preliminary)
- Results in SM fits of  $M_H < 152 \text{ GeV}$  @ 95% CL
  - Previously  $M_H < 161 \text{ GeV}$  @ 95% CL
  - $M_W$  still is the limiting factor in  $M_H$  prediction
- Full Tevatron dataset ( $\sim 10 \text{ fb}^{-1}$ ) on hand
  - $\Delta M_W < 15 \text{ MeV}$  per experiment achievable

Backup

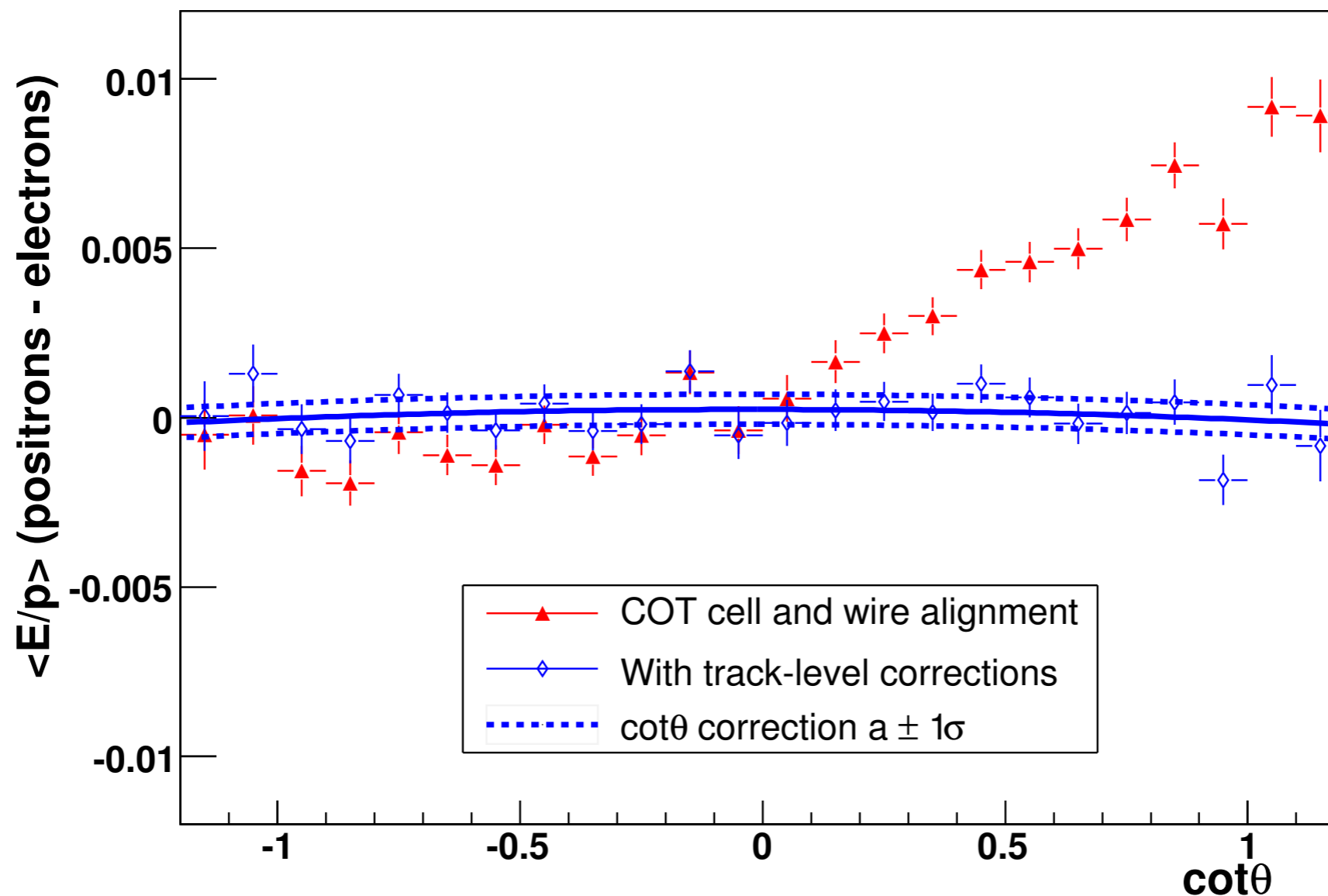
# EM calorimeter spatial uniformity

- Apply tower-by-tower correction to flatten response in eta
  - Response after tuning flat

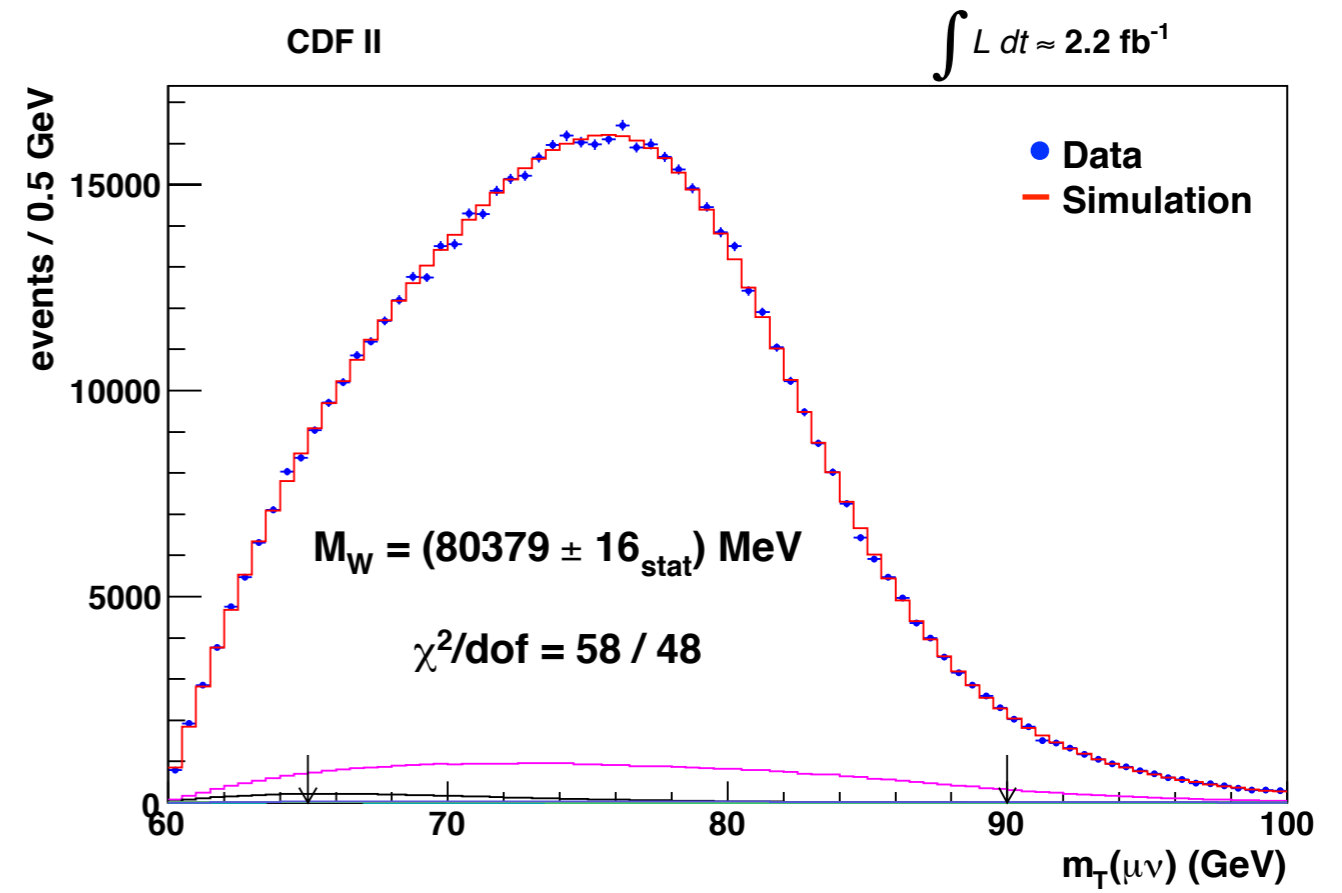
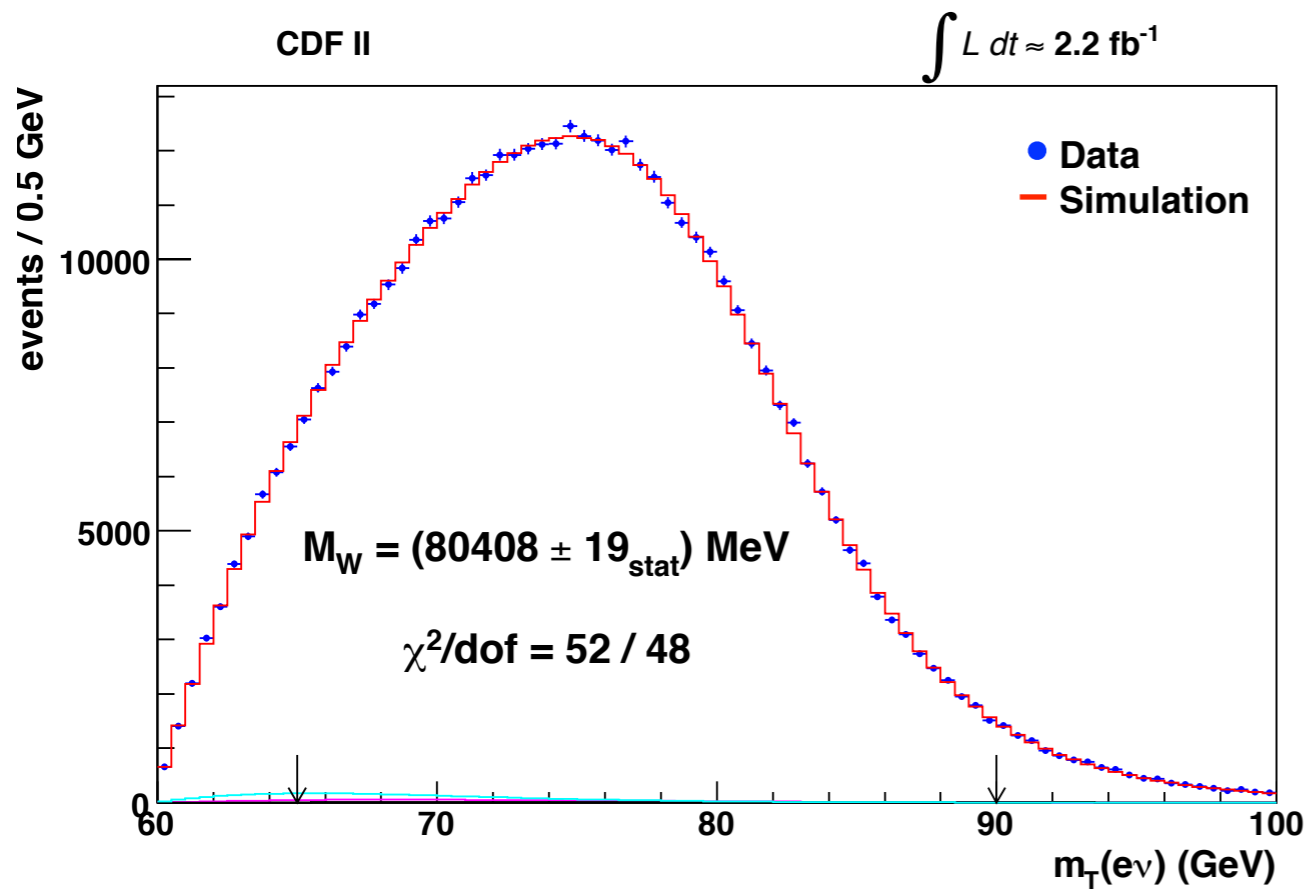


# Residual alignment corrections

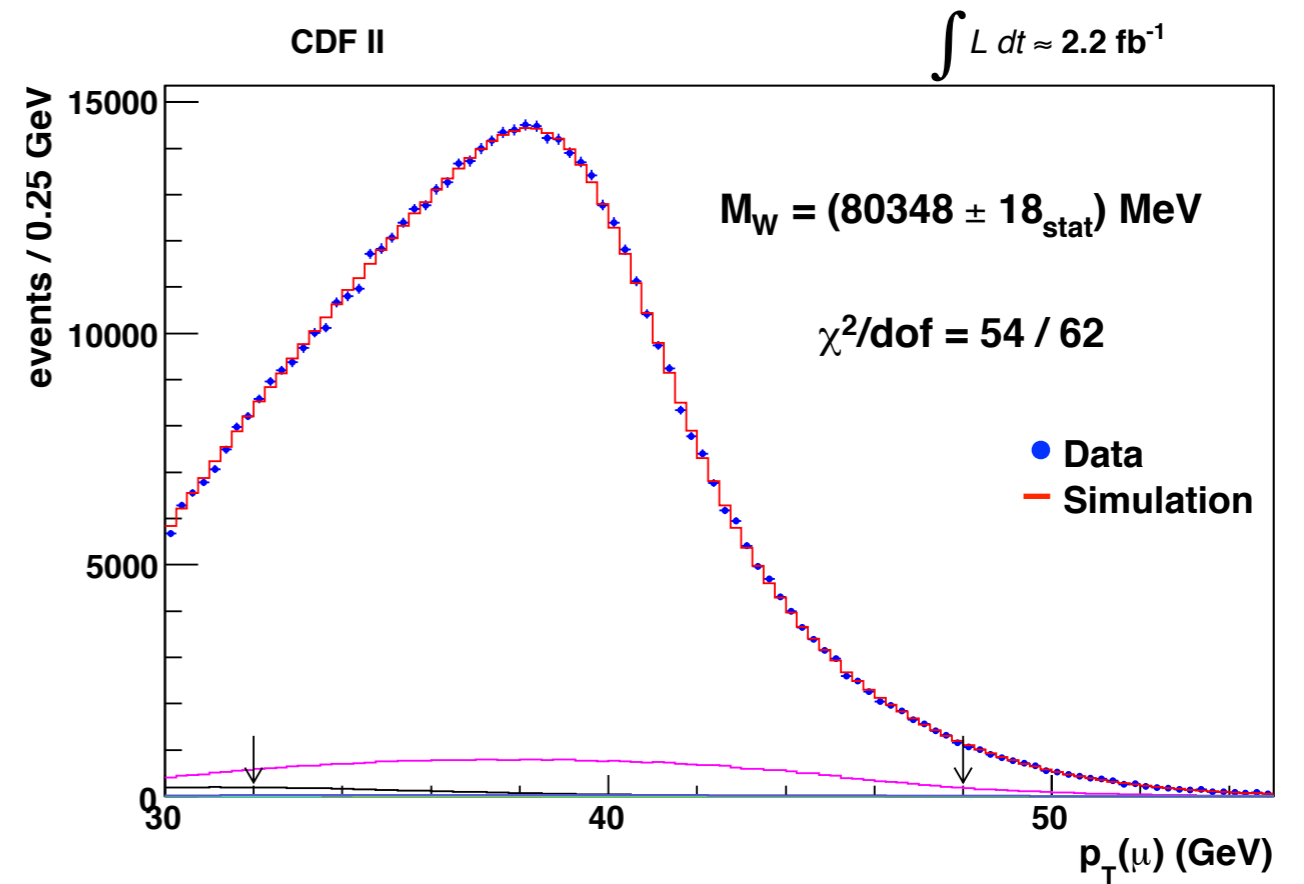
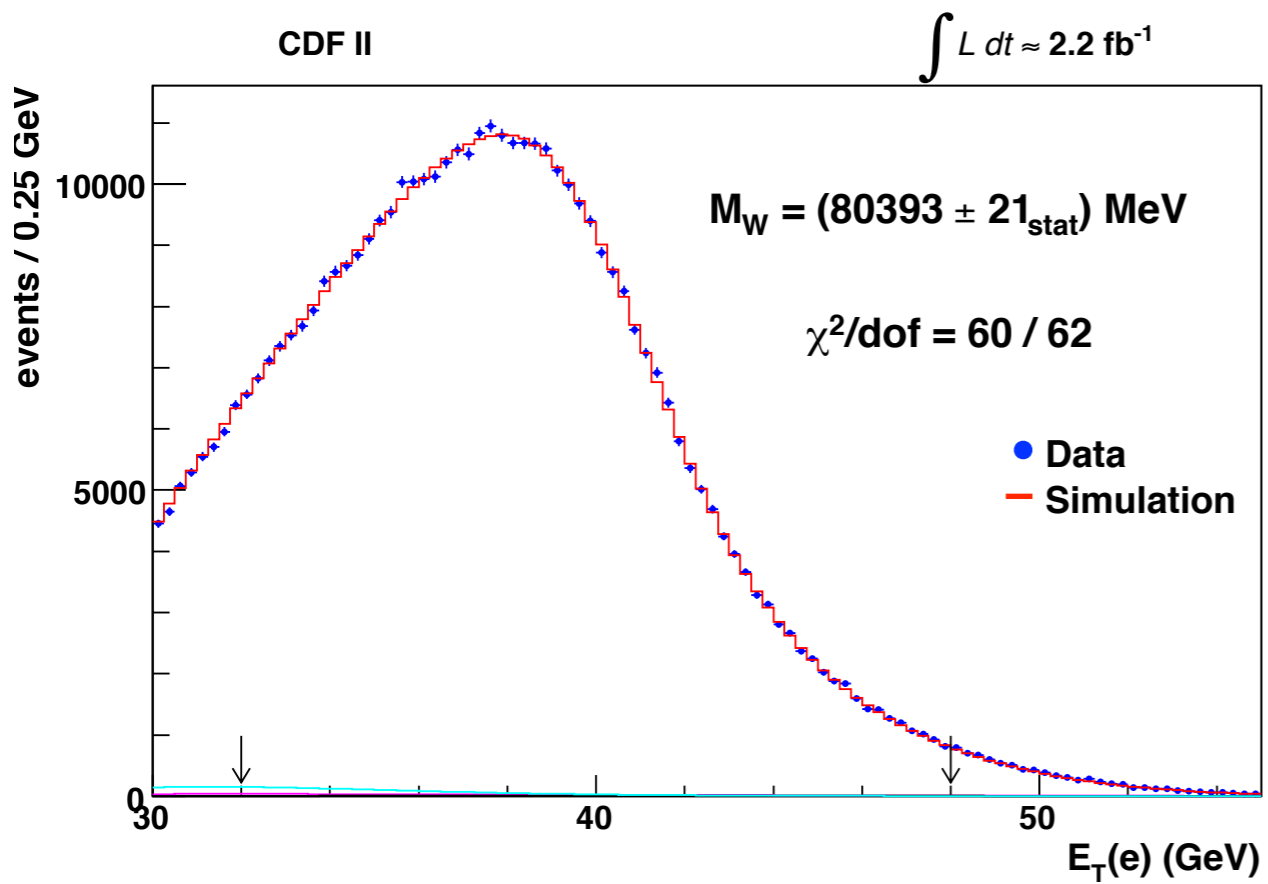
- Some “weakly constrained modes” not corrected by cosmic alignment
- Study these using difference in  $\langle E/p \rangle$  between  $e^+$  and  $e^-$  events
  - Apply correction to alignment based on this difference



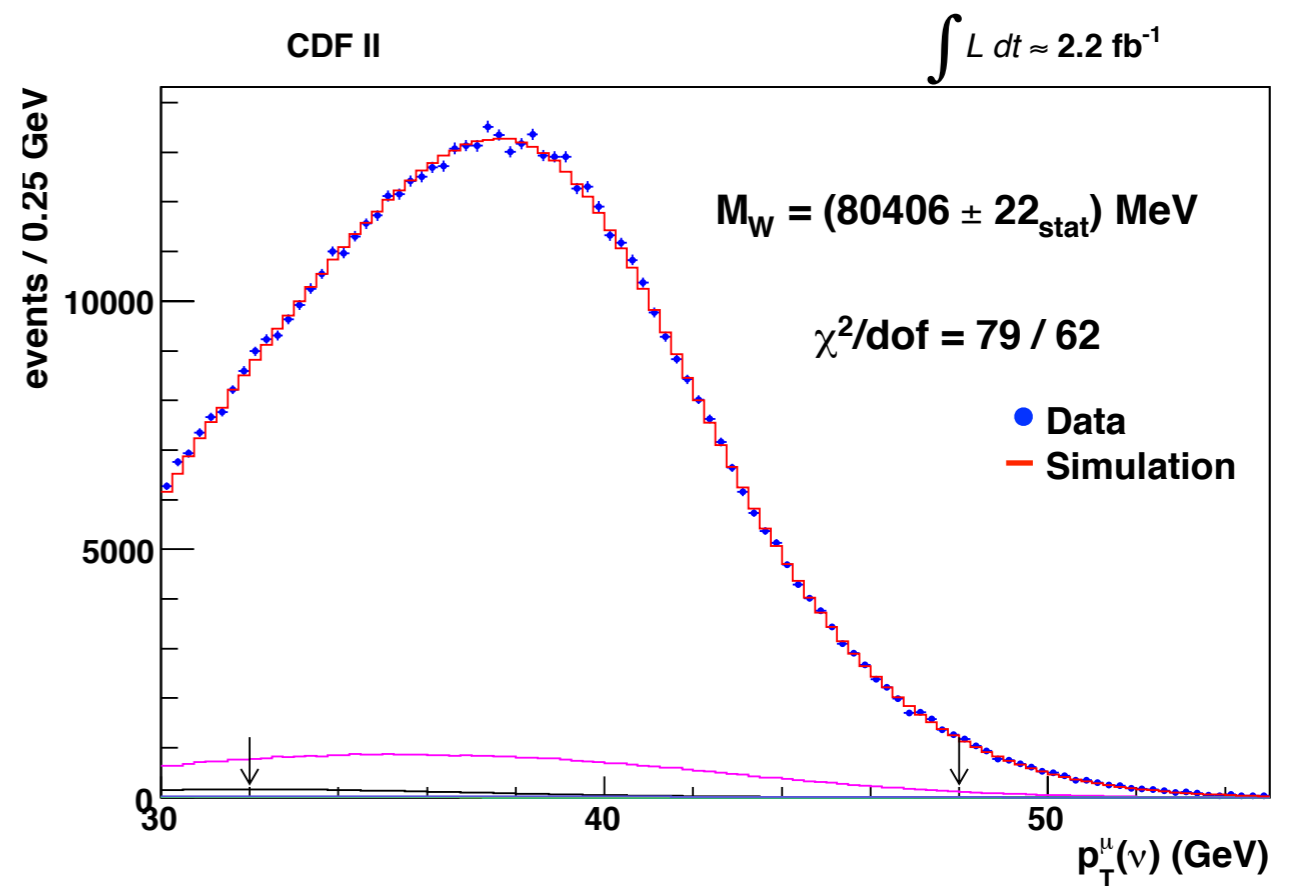
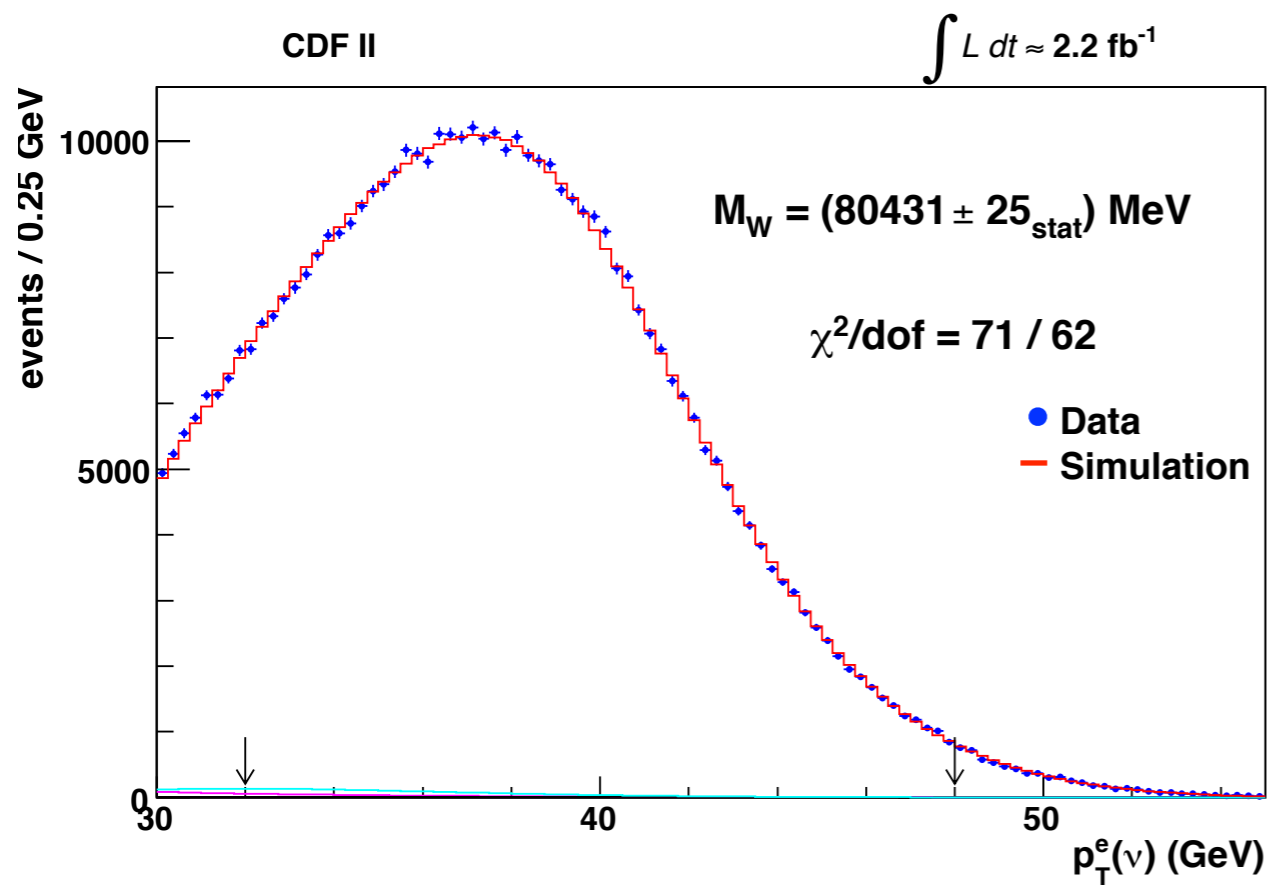
# W mass fits: $m_T$



# W mass fits: lepton $p_T$

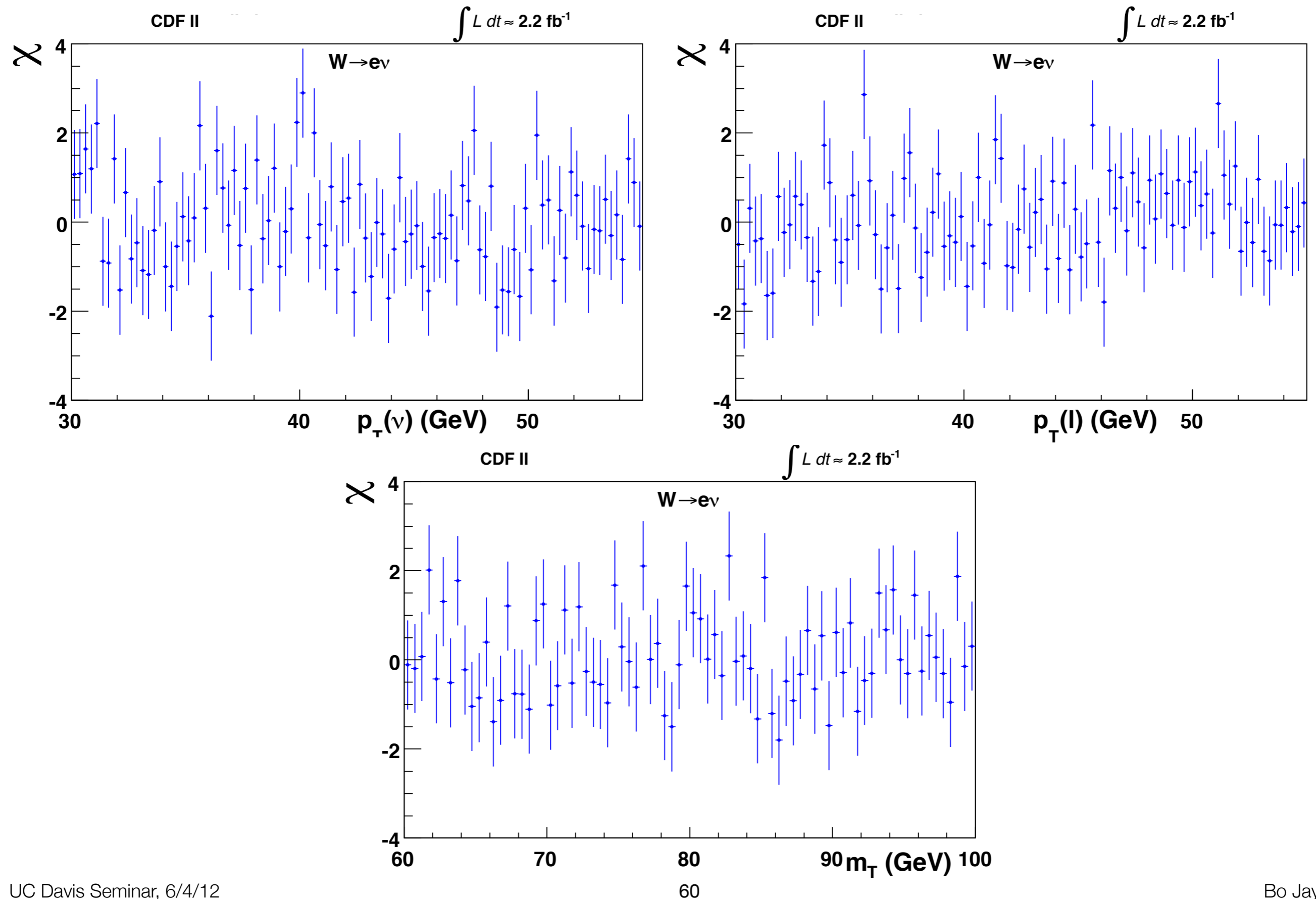


# W mass fits: neutrino $p_T$

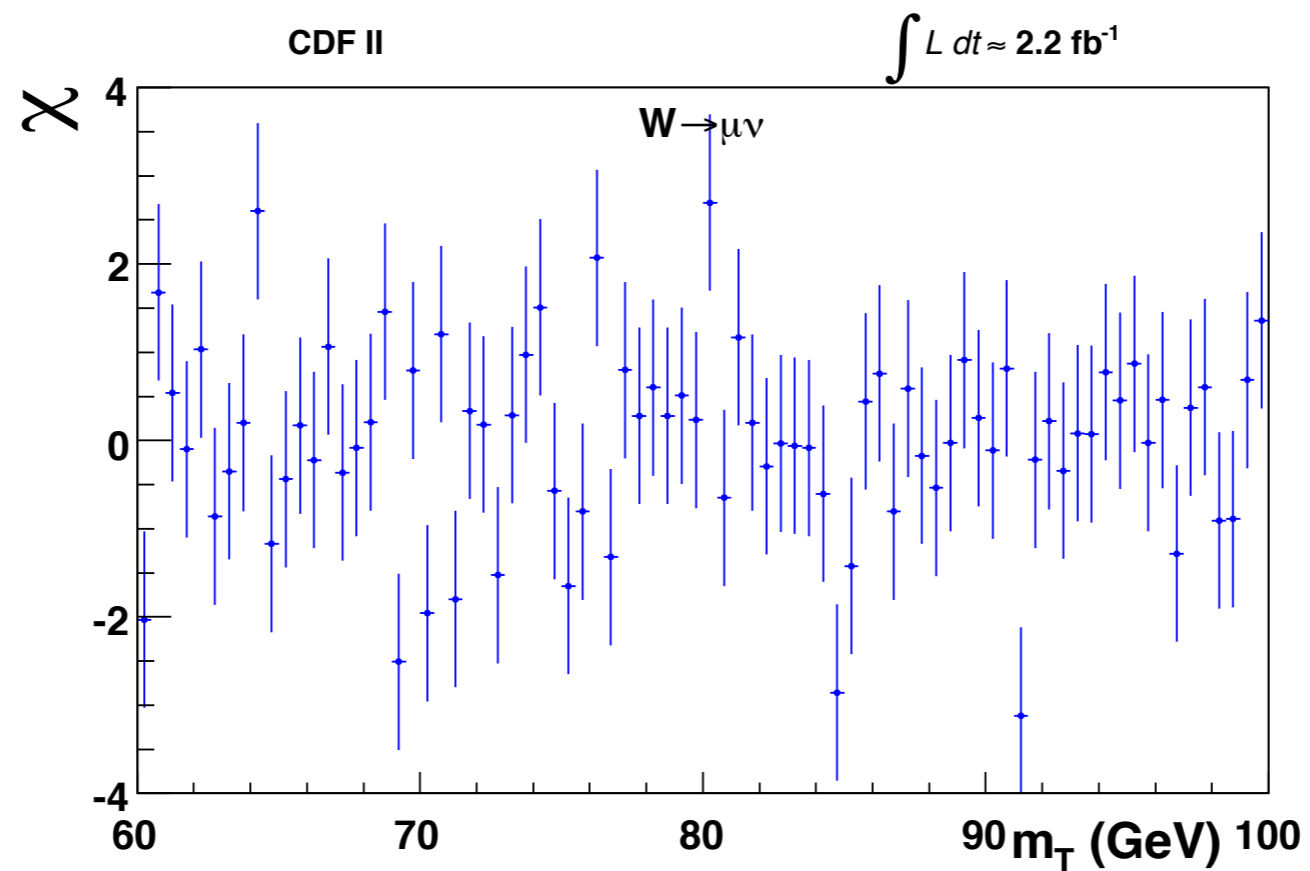
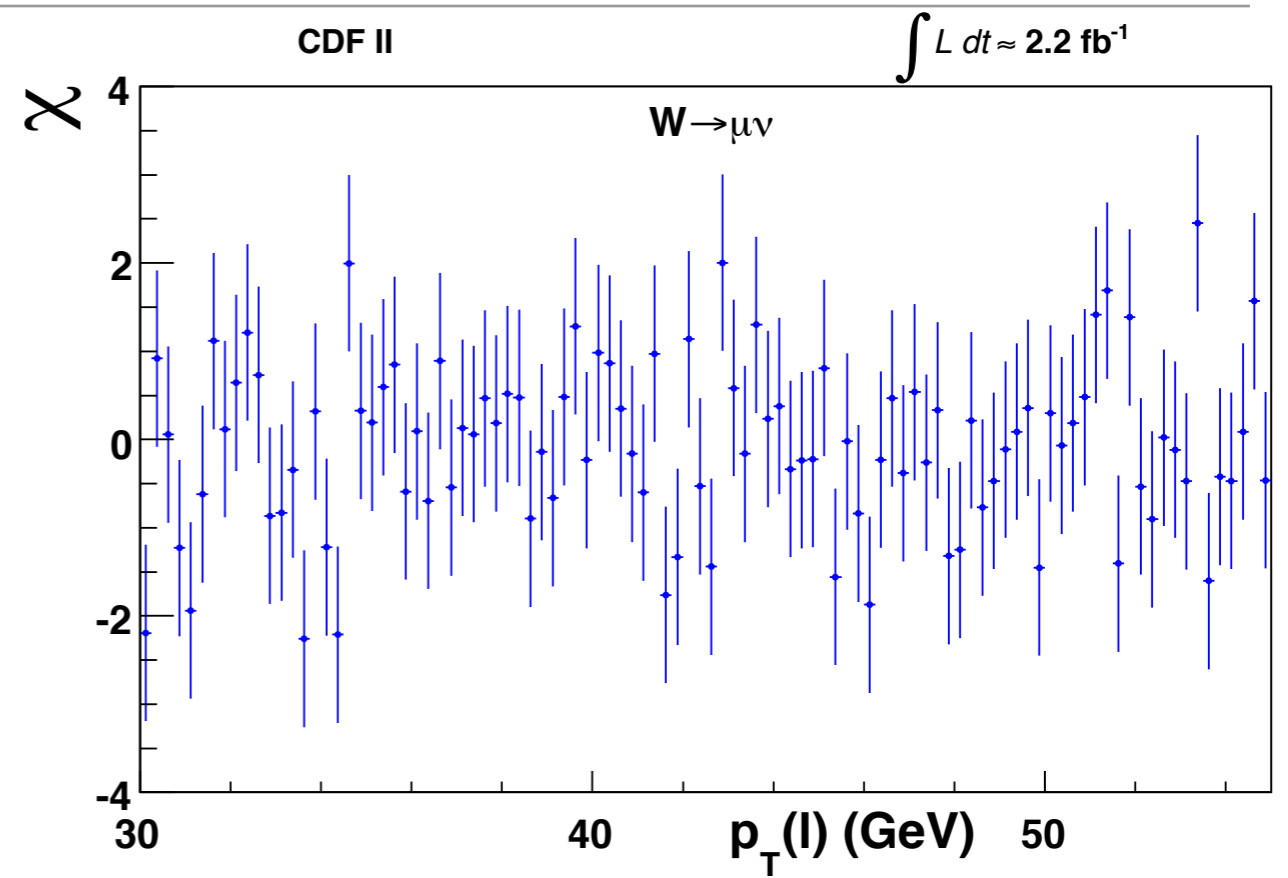
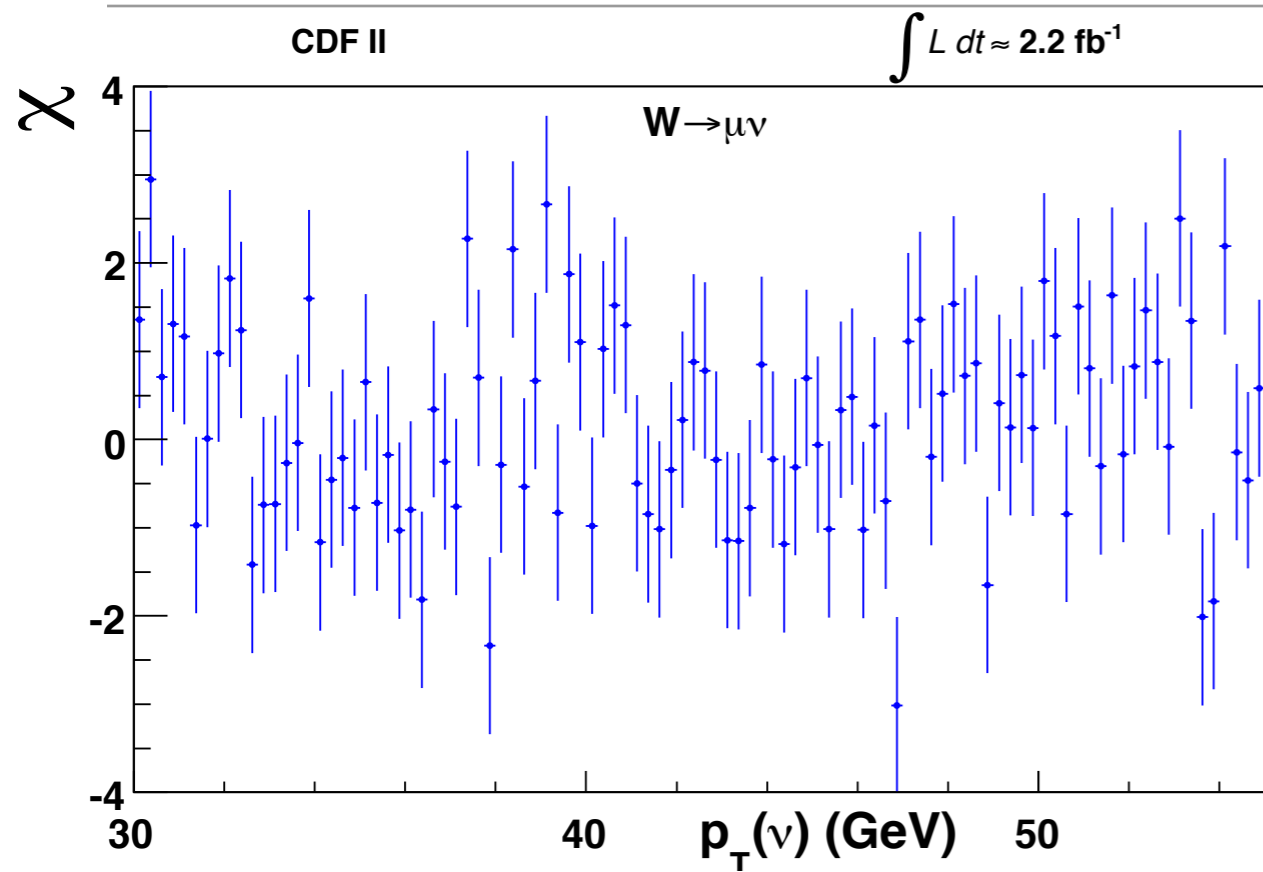




# Electron fit residuals

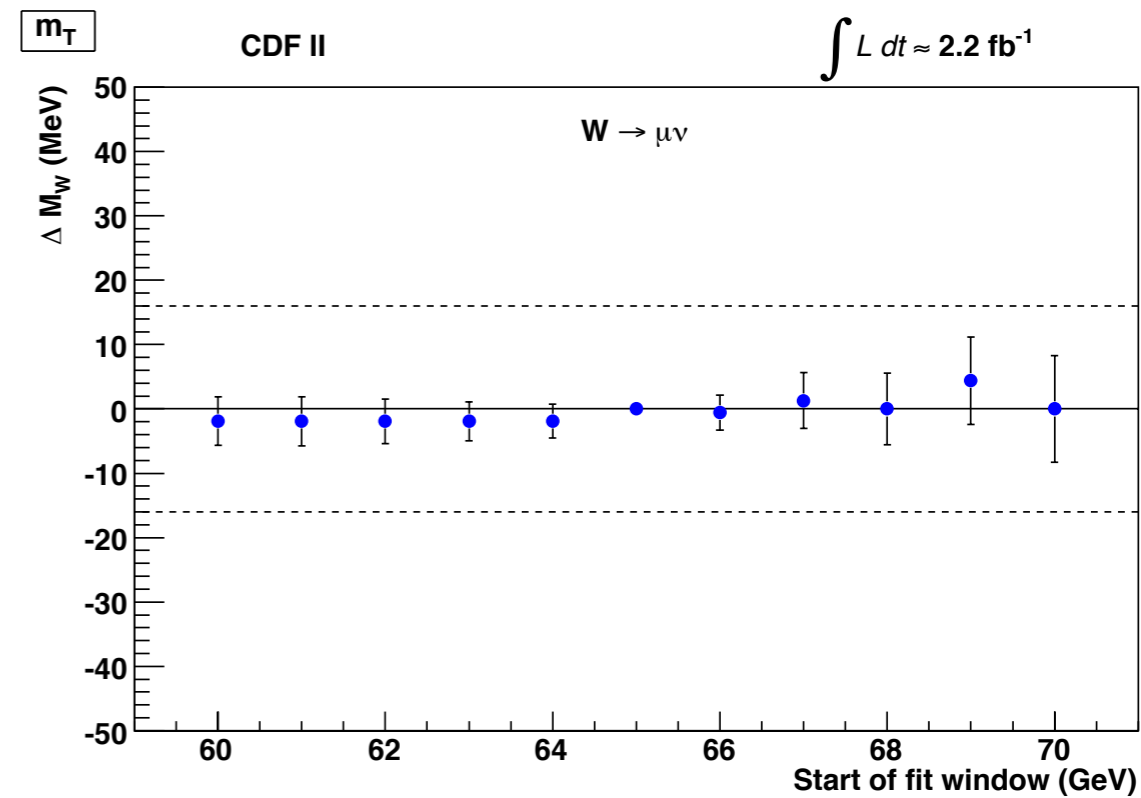
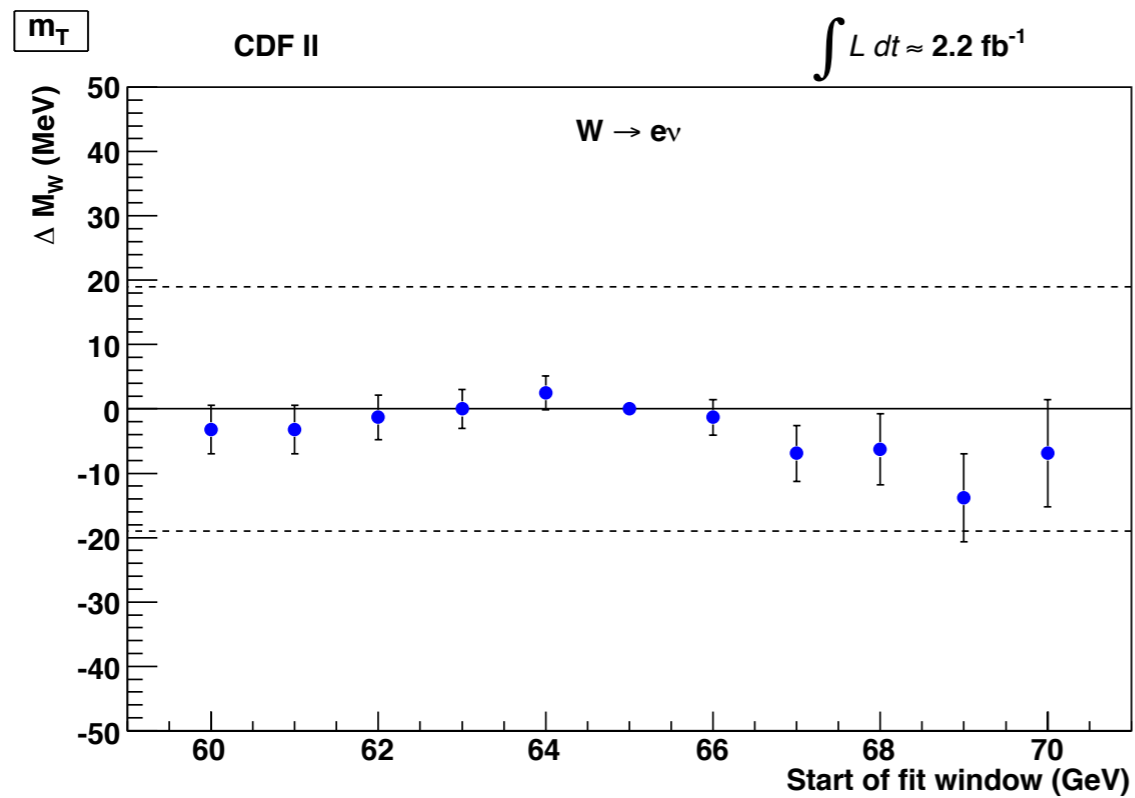


# Muon fit residuals

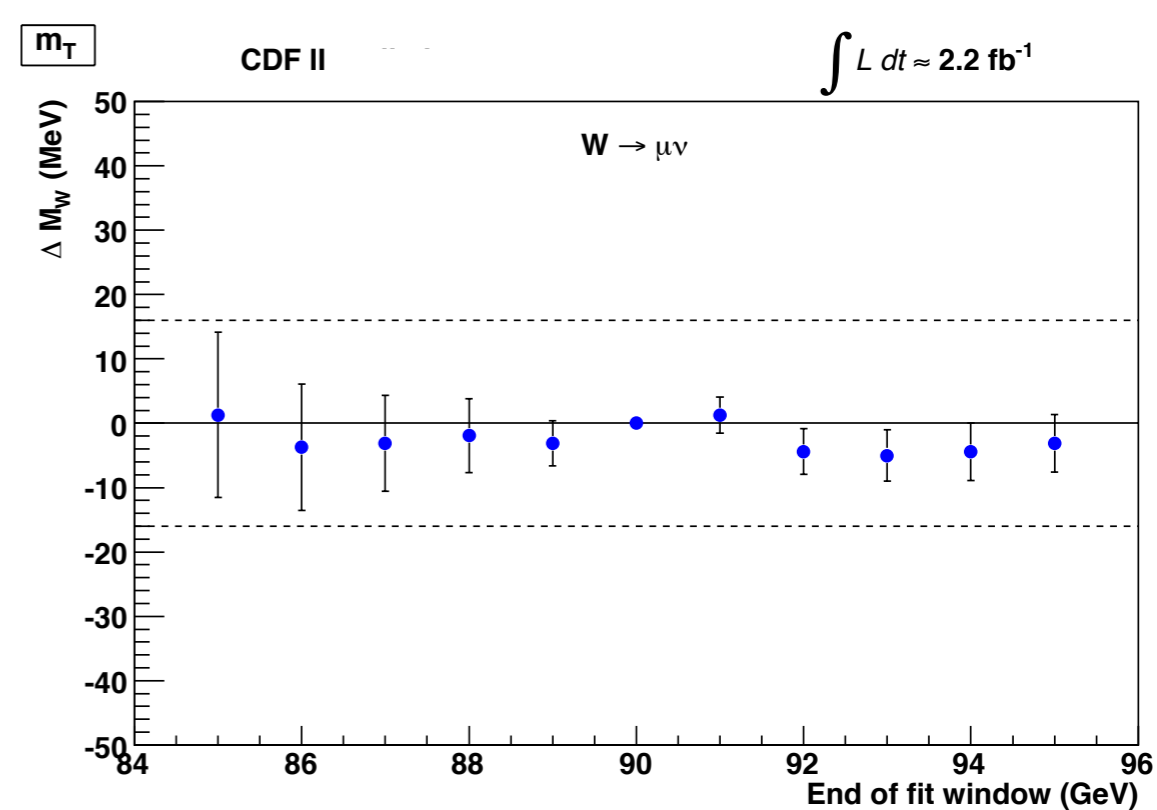
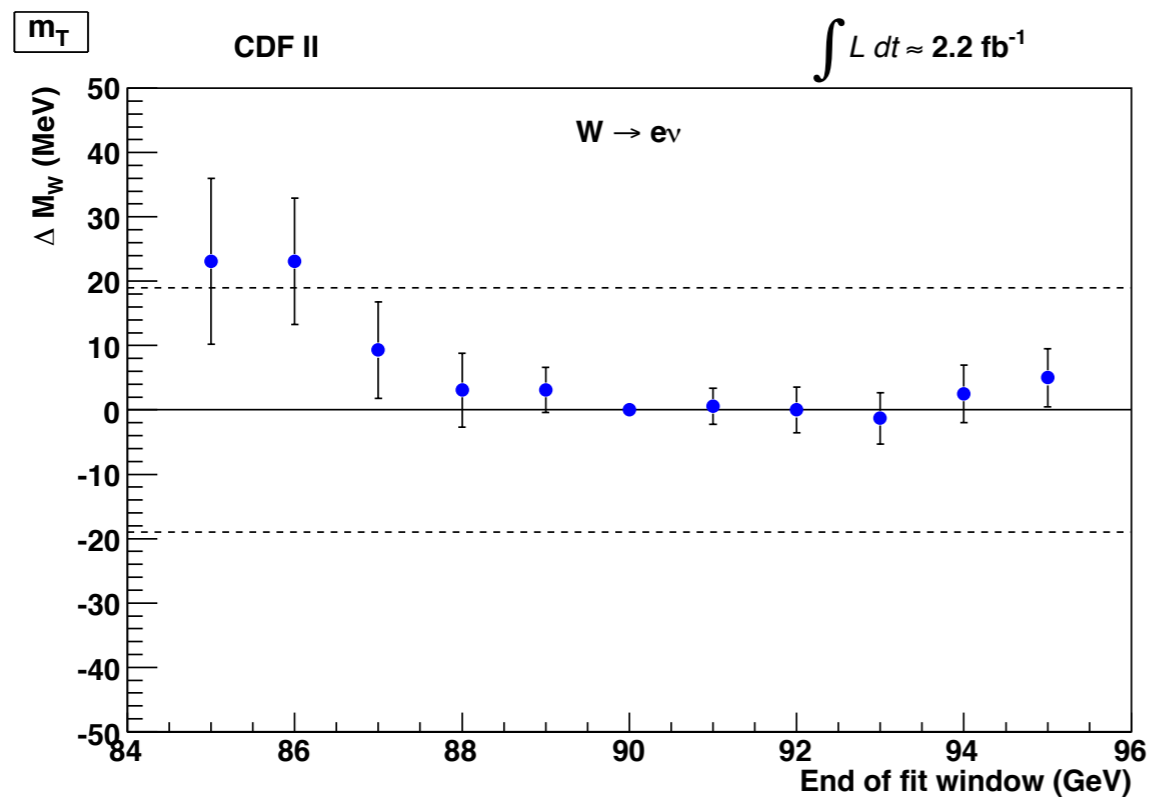


# Fit window variation: $m_T$

lower



upper



# Systematics: $m_T$

---

Systematic (MeV)	Electrons	Muons	Common
Lepton Energy Scale	10	7	5
Lepton Energy Resolution	4	1	0
Recoil Energy Scale	5	5	5
Recoil Energy Resolution	7	7	7
$u_{  }$ Efficiency	0	0	0
Lepton Removal	3	2	2
Backgrounds	4	3	0
$p_T(W)$ Model ( $g_2, g_3, \alpha_s$ )	3	3	3
Parton Distributions	10	10	10
QED Radiation	4	4	4
Total	18	16	15

# Systematics: $p_T^l$

---

Systematic (MeV)	Electrons	Muons	Common
Lepton Energy Scale	10	7	5
Lepton Energy Resolution	4	1	0
Recoil Energy Scale	6	6	6
Recoil Energy Resolution	5	5	5
$u_{  }$ efficiency	2	1	0
Lepton Removal	0	0	0
Backgrounds	3	5	0
$p_T(W)$ model ( $g_2, g_3, \alpha_s$ )	9	9	9
Parton Distributions	9	9	9
QED radiation	4	4	4
Total	19	18	16

# Systematics: $p_T^V$

---

Systematic (MeV)	Electrons	Muons	Common
Lepton Energy Scale	10	7	5
Lepton Energy Resolution	7	1	0
Recoil Energy Scale	2	2	2
Recoil Energy Resolution	11	11	11
$u_{  }$ efficiency	3	2	0
Lepton Removal	6	4	4
Backgrounds	4	6	0
$p_T(W)$ model ( $g_2, g_3, \alpha_s$ )	4	4	4
Parton Distributions	11	11	11
QED radiation	4	4	4
Total	22	20	18

# Some cross-checks

---

*Stat. uncertainty only.  $p_T^l$  fits only.*

Lepton	Fit	Result (MeV)
Electron	$M_{W^+} - M_{W^-}$	$-49 \pm 42$
Electron	$M_W(\phi > 0) - M_W(\phi < 0)$	$-58 \pm 45$
Muon	$M_{W^+} - M_{W^-}$	$71 \pm 69$
Muon	$M_W(\phi > 0) - M_W(\phi < 0)$	$-54 \pm 36$

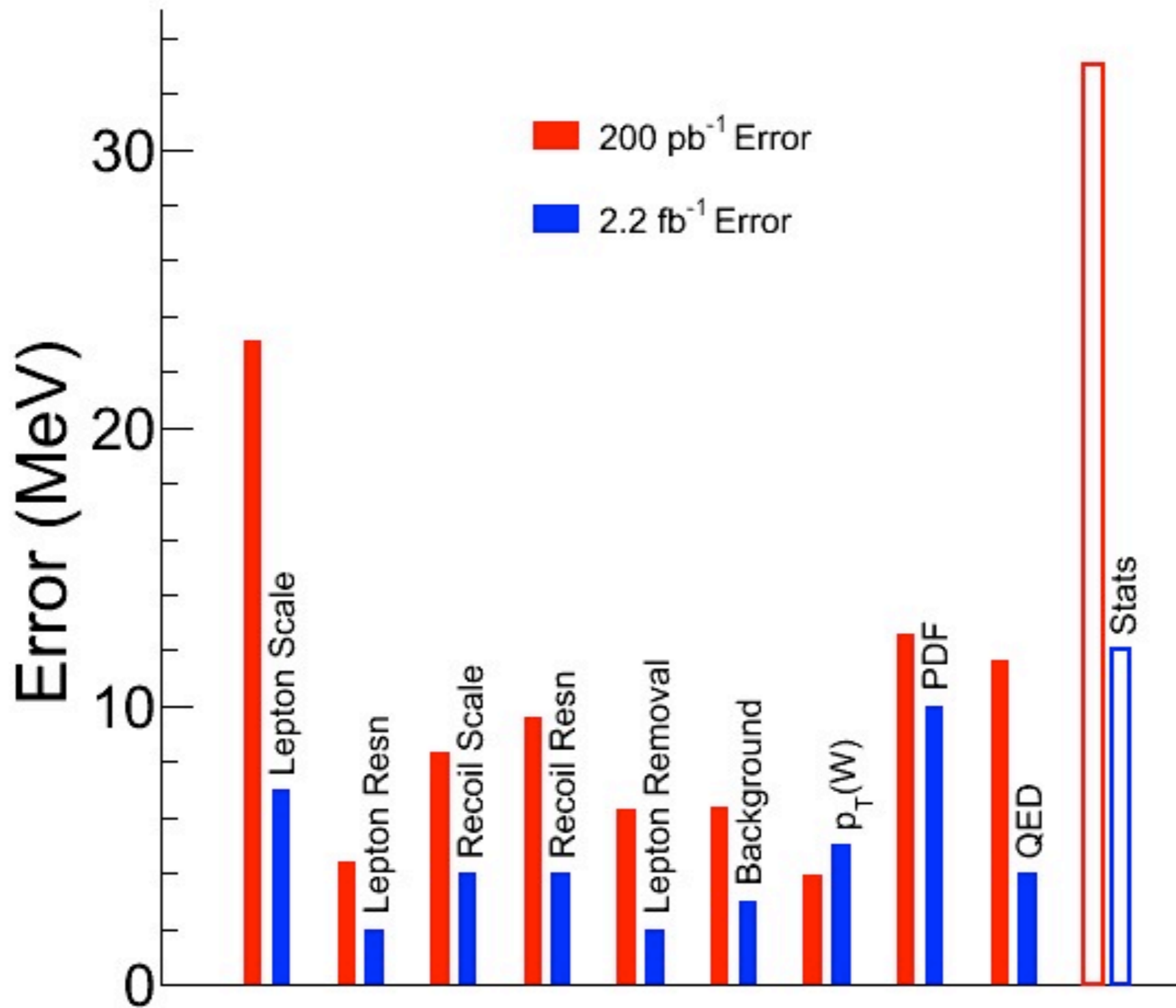
# Mass fit combinations

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- Electron and muon  $m_T$  fits combined  
 $m_W = 80390 \pm 20 \text{ MeV}, \chi^2/\text{dof} = 1.2/1 (28\%)$
- Electron and muon  $p_T$  fits combined  
 $m_W = 80366 \pm 22 \text{ MeV}, \chi^2/\text{dof} = 2.3/1 (13\%)$
- Electron and muon MET fits combined  
 $m_W = 80416 \pm 25 \text{ MeV}, \chi^2/\text{dof} = 0.5/1 (49\%)$
- All electron fits combined  
 $m_W = 80406 \pm 25 \text{ MeV}, \chi^2/\text{dof} = 1.4/2 (49\%)$
- All muon fits combined  
 $m_W = 80374 \pm 22 \text{ MeV}, \chi^2/\text{dof} = 4/2 (12\%)$
- All fits combined  
 $m_W = 80387 \pm 19 \text{ MeV}, \chi^2/\text{dof} = 6.6/5 (25\%)$



# Uncertainty progress



# MSSM allowed region

*Heinemeyer, Hollik, Stockinger, Weiglein, Zeune*

