

Cascading in the Early Universe

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UC-Davis, Spring 2007

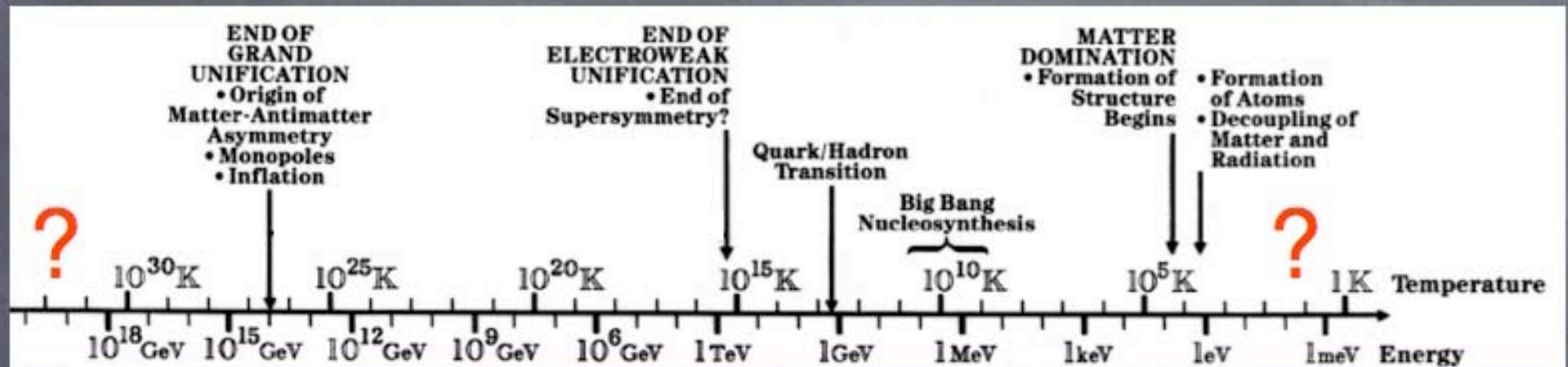
Acknowledgments

- Cambridge:
Kate Marvel, Malcolm Perry
- Columbia:
Brian Greene, Simon Jude, Janna Levin, Amanda Weltman
- Michigan:
Fred Adams, Sera Cremonini, Katie Freese, Chris Gauthier, Gordon Kane, Jim Liu
- Toronto / CITA:
Lev Kofman

Overview

- Brief Review of Inflation Model Building
- Inflation in String theory -- and a problem...
- Moduli Trapping
- Transitions through the landscape
- Coarse graining and a multi-fluid approach to inflation
- Cosmological Perturbations
- Conclusions

Phase Transitions and Cosmology



Phase Transitions can result in many experimental signatures:

- Gravity Waves
 - 1st order: Bubble collisions, Turbulence
 - 2nd order: Inhomogeneous inflaton decay
- Density fluctuations
- Relic Abundances (e.g. neutrino background)
- Defect Formation (e.g. Cosmic strings, Domain walls)

Vacuum Manifolds and Gauge Theories

- Gauge Theories can have rich vacuum structure
(e.g. Theta vacuum)
- Non-perturbative behavior
(e.g. Gaugino condensation, solitons, instantons)
- String theory Landscape
Strings, Branes, lots of fluxes

Old Inflation

Guth and Weinberg, 1981

$SU(5)$ GUT (well motivated by fundamental theory)

Could potentially solve:

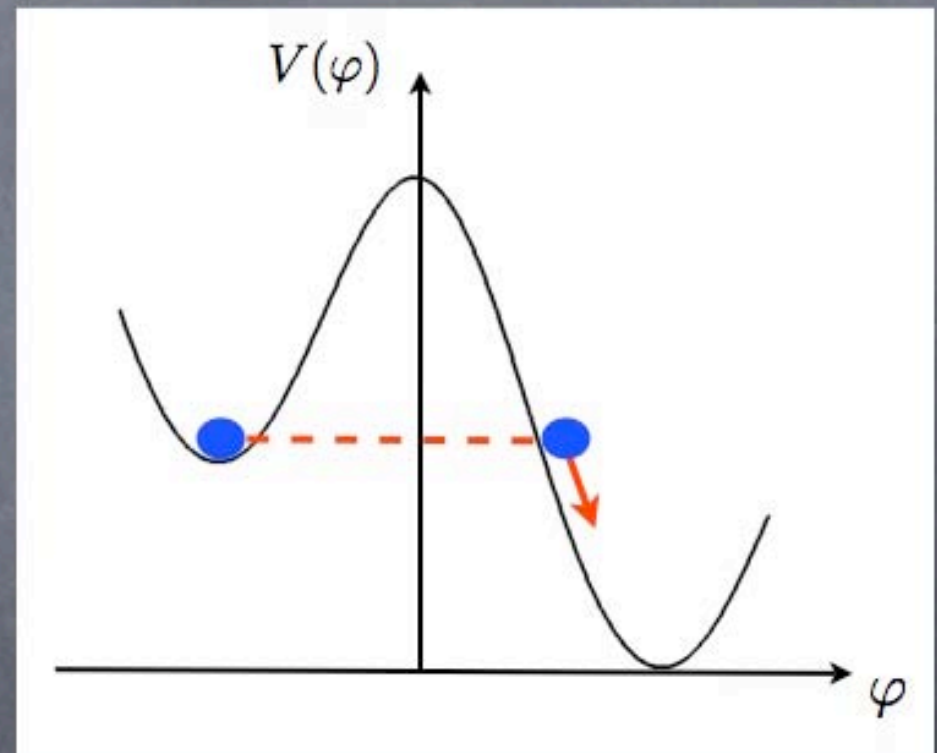
- *Monopole problem*
- Horizon problem,
- Flatness problem,
- Entropy problem

AND (accident)

gives explanation for origin of

Scale Invariant Spectrum of density perturbations (LSS)

(maybe some gravity waves too)

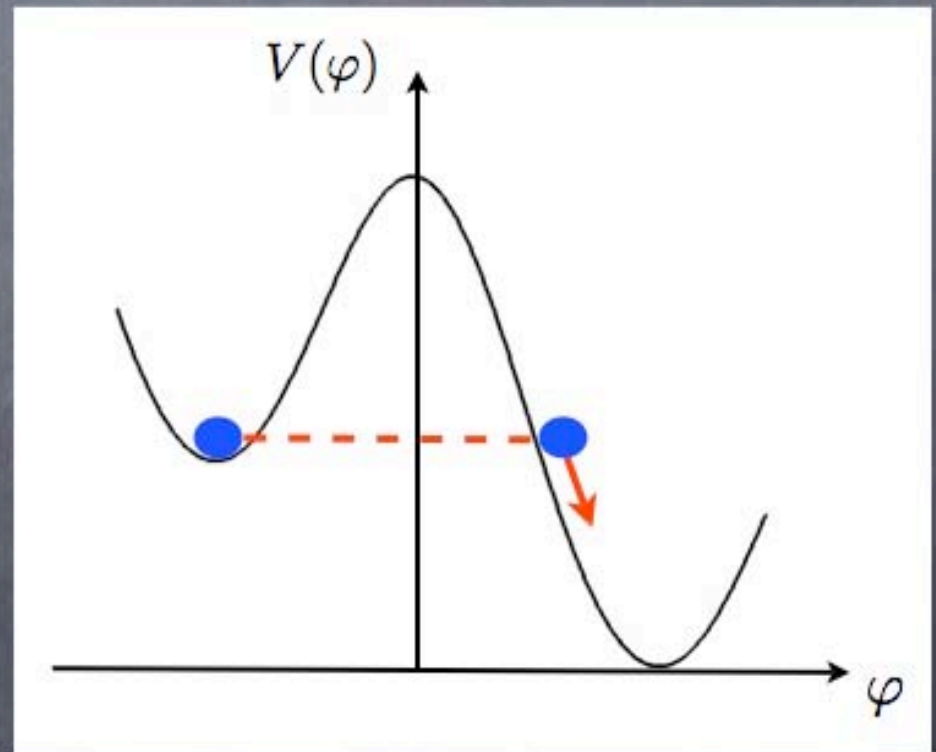


Old Inflation doesn't work

- 1st order transition - Single Tunneling Event
- Potential difference must yield enough inflation
- Bubbles of new phase must percolate

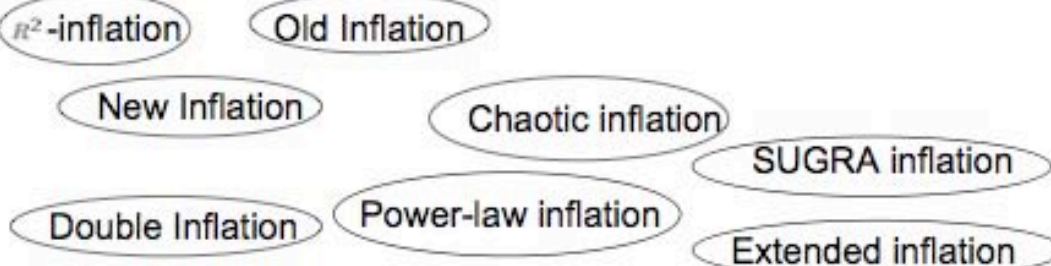
Unfortunately:

- Inflation doesn't end (Graceful Exit Problem)
- Single universe emerges
- Can't reheat (cold & empty)



Inflation remains an idea w/out a theory (no UV completion)

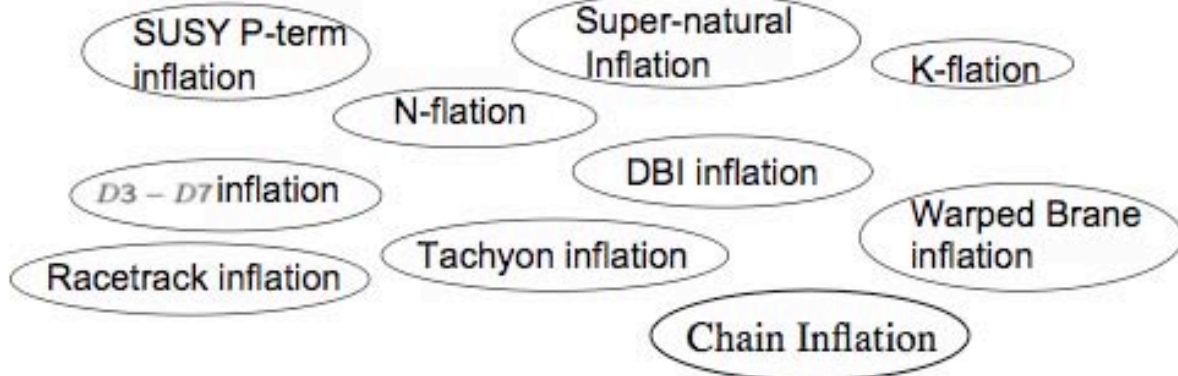
1980



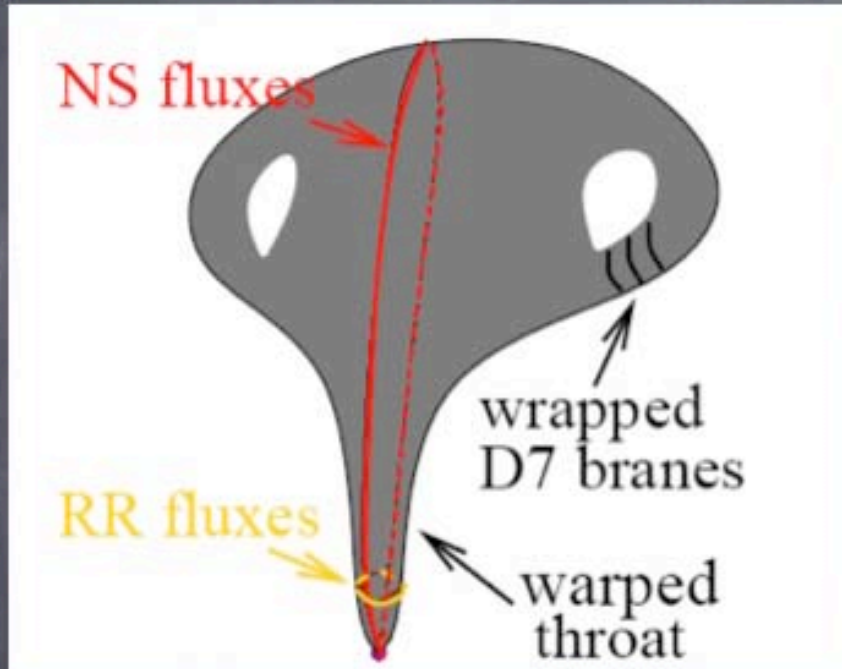
1990



2000

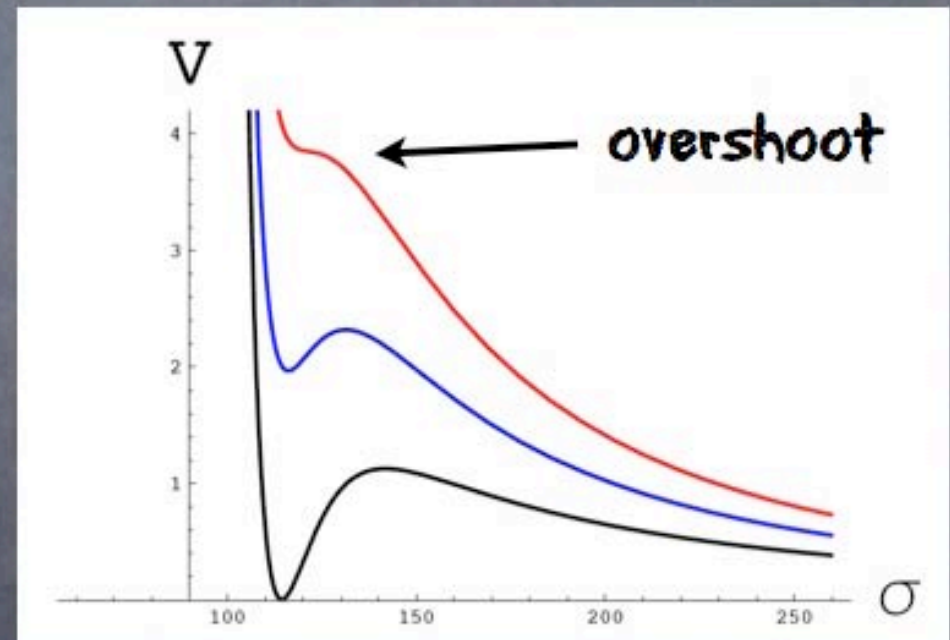


Towards inflation in string theory (e.g., KKLT, KK $\Lambda\Lambda\Lambda$ LT, BBCEGKLQ, etc..)



Many moduli - flat directions to stabilize

Universe is hot
--> Finite Temp.



Is Symmetry Attractive?

Are all minima equal?

Review of Strings on S^1

SUGRA Massless modes:

$$R \equiv \sqrt{G_{55}} \rightarrow \phi \quad A_{\mu}^{R/L} = G_{\mu 5} \pm B_{\mu 5} \quad \text{Chiral } U(1)$$

Higgsed scalar w/ winding charge (w/ knowledge of string theory)

$$m_w^2 = m_s^2 (\omega^2 R^2 - 4) \quad \omega = \pm 2$$

Time dependent effective mass

$$m_w^2 = g^2 \phi^2(t)$$

Enhanced gauge symmetry - ESP @ self-dual radius

$$R \rightarrow l_s \quad m_w \rightarrow 0 \quad U(1) \rightarrow SU(2)$$

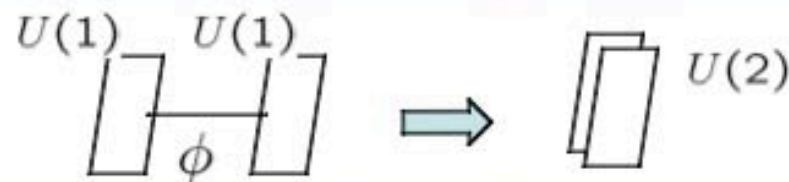
8 new scalars

4 new vectors

Enhanced Symmetry

Many examples of ESPs in string theory

- Heterotic strings on T^6 - Enhanced gauge symmetry
- Type II on $K3$ - ESPs at singularities
- Wrapped branes and strings on collapsing cycles (e.g. conifolds and flops)
- Coincident branes (open strings become light)



Moduli Trapping

- Kofman, Linde, Liu, Maloney, McAllister, Silverstein hep-th/0403001
- S.W. hep-th/0404177
- Cremonini & S.W. hep-th/0601082
- Greene, Judes, Levin, Weltman, & S.W. - to appear soon

$$\ddot{\phi} + 3H\dot{\phi} + g^2 \langle \chi^2 \rangle \phi = 0$$

$$\ddot{\chi} + 3H\dot{\chi} + g^2 \langle \phi^2 \rangle \chi = 0$$

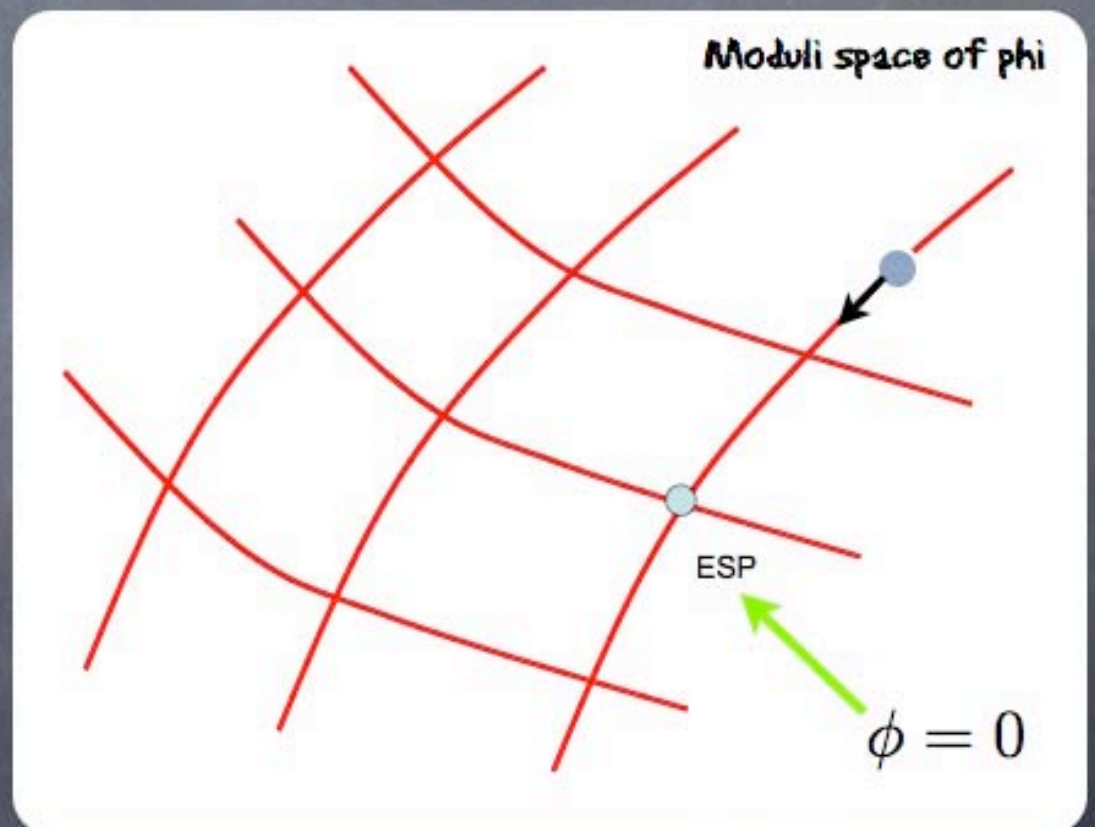
Initially: $\langle \chi^2 \rangle = 0$

Adiabaticity parameter

$$\frac{\dot{\omega}}{\omega^2} \approx \frac{\dot{m}}{m^2} \sim 1$$

Near ESP modes become excited

- Particle production -



$$\ddot{\phi} + 3H\dot{\phi} + g^2 \langle \chi^2 \rangle \phi = 0$$

Initially: $\langle \chi^2 \rangle = 0$

Adiabaticity parameter

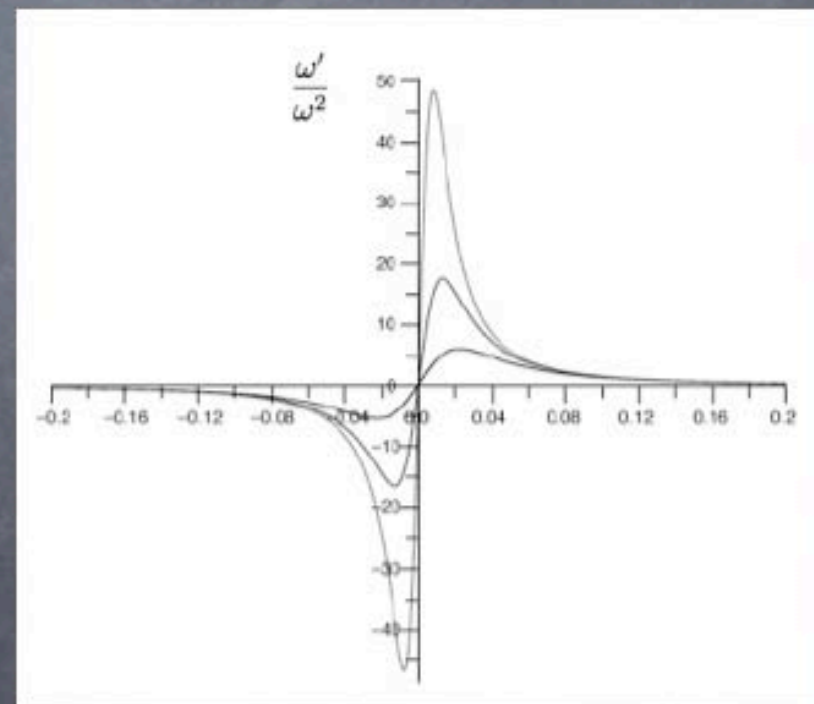
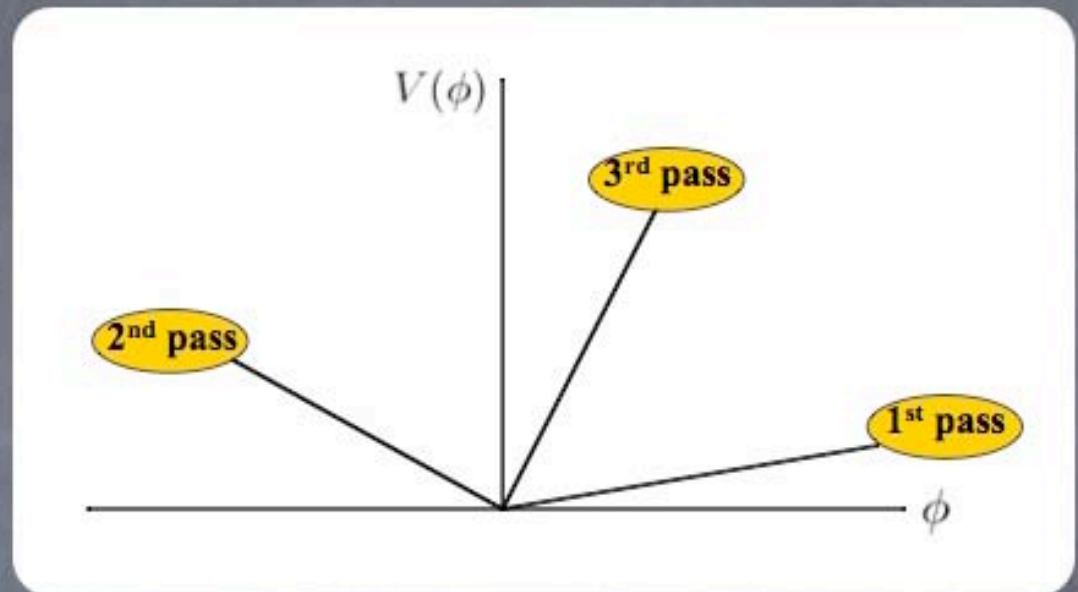
$$\frac{\dot{\omega}}{\omega^2} \approx \frac{\dot{m}}{m^2} \sim 1$$

Near ESP modes become excited

-Particle production-

$$n_k \approx e^{-\frac{\pi k^2}{g v_0}}$$

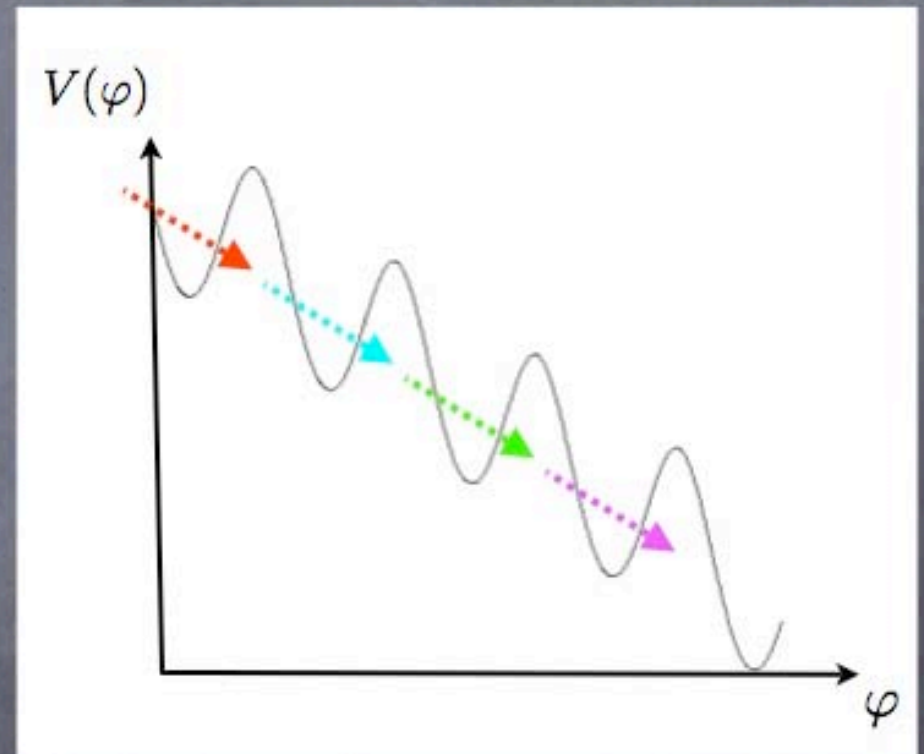
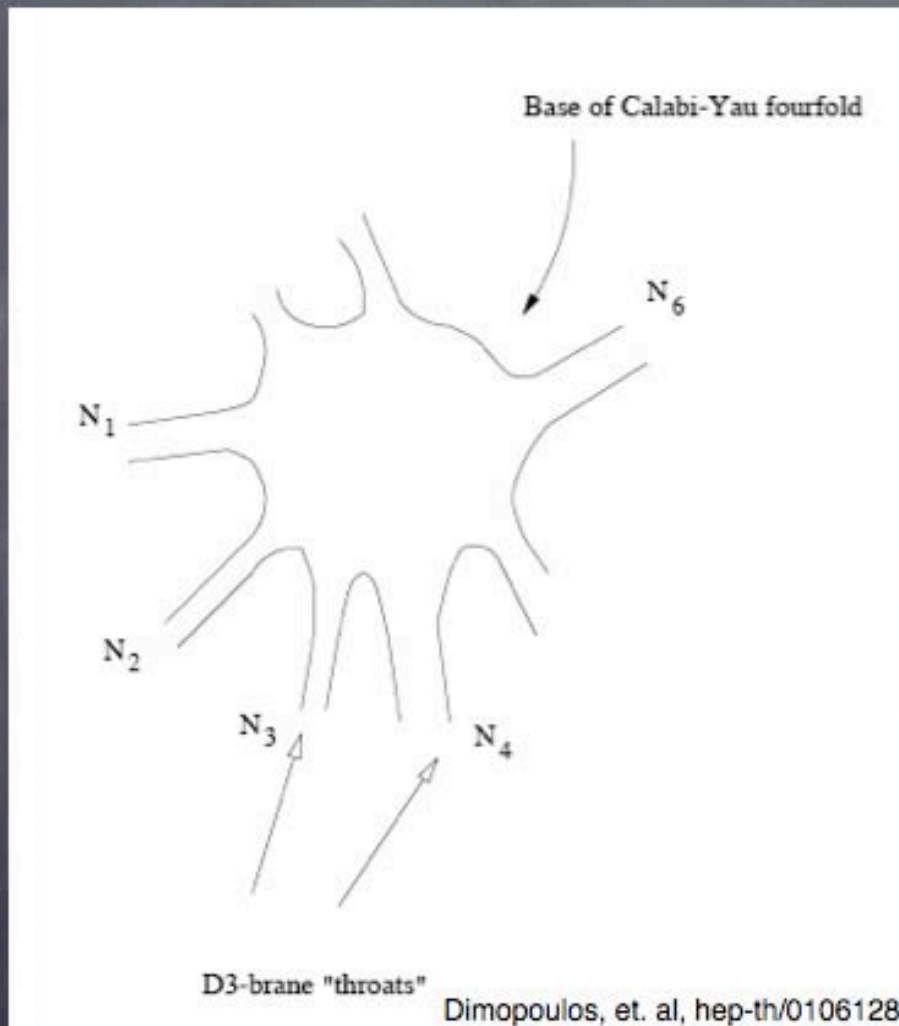
$$\ddot{\phi} + 3H\dot{\phi} = -g n_\chi \frac{\phi}{|\phi|}$$



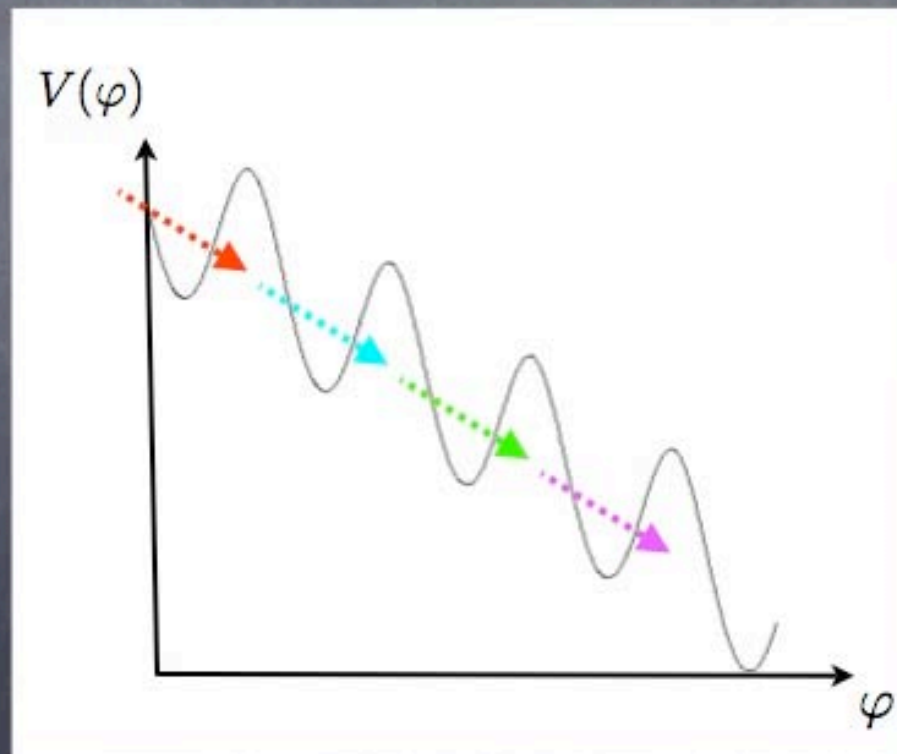
"Observations"

- Moduli dynamics require careful study of moduli space - new light d.o.f. (c.f. Vafa - Swampland)
- Points of enhanced symmetry seem to be dynamical attractors - some pts. in landscape preferred dynamically
- ESPs are fixed pts. of effective action... even after phase transition (protected by symmetry - c. f. Dine)
- Fixed points of dualities natural places to find moduli
- Can moduli dynamics + gravity generate hierarchies?
- The dilaton - difficult - but possible
(Cremonini & S.W. [hep-th/0601082](#))

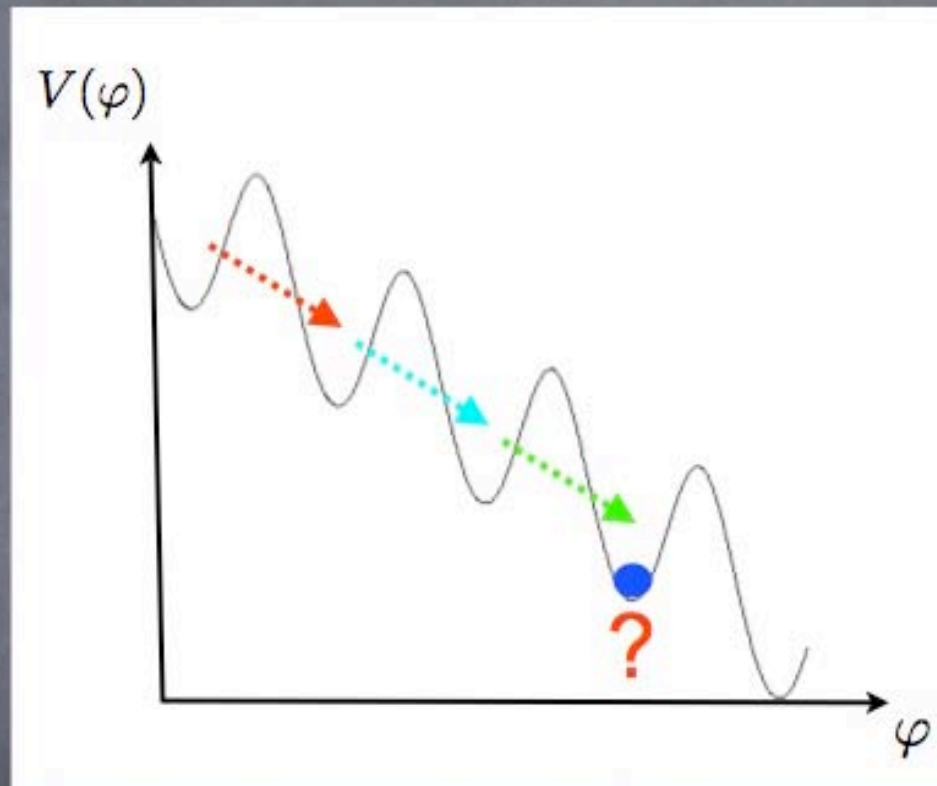
Traveling through the landscape



- Did the universe go through a series of rapid phase transitions?
- 1st or 2nd order?
- Can a successful model of inflation result?
- Signatures?



- Can this address the Cosmological constant problem? (Abbott)



Traveling through the landscape

Bousso-Polchinski (extension of Brown-Teitelboim mechanism)

$$F_{\mu\nu\rho\sigma}^{(i)} = n_i q_i \epsilon_{\mu\nu\rho\sigma} \quad n \in \mathbb{Z}$$

$$\Lambda = \Lambda_{\text{bare}} + \sum_{\text{fluxes}} \frac{1}{2} n_i^2 q_i^2 \quad \text{Make } \Lambda \text{ dynamical: } \Lambda \rightarrow F_{(4)}$$

Membrane nucleation (instantons)

$$n \rightarrow n - 1$$

Energy drop

$$\epsilon^4 = - \left(n - \frac{1}{2} \right) q^2$$

Ex: M-theory compactification

$$\tau_4 = 2\pi M_{11}^3 (V_3 M_{11}^3) \quad \text{M5} \rightarrow \text{4D}$$

$$M_{11} \sim 10^{-3} M_p$$

$$V_3 M_{11}^3 \sim 10^3 \quad n \sim 1000$$

$$\epsilon^4 \sim 10^{-7} M_p^4$$

Can we use degeneracy of vacua to address naturalness?

Kane, Perry, and Zytlow, hep-th/0311152

Near degeneracy

--> Super-position of vacua

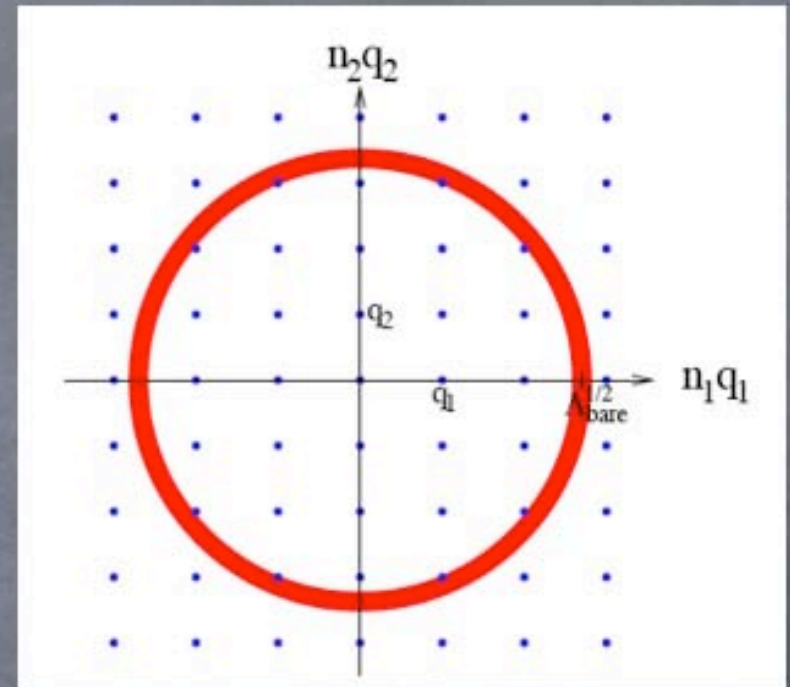
Ground State Energy

$$\rho(\theta) \approx H^2 M_p^2 - 2 \sum_{i=1}^d H^4 \cos(\theta_i) e^{-S_E}$$

$$H \sim 10^{15} \text{ GeV}$$

$$d \sim 10^{12} \quad N \sim 10^{100}$$

$$\longrightarrow \rho_0 \sim (10^{-3} \text{ eV})^4$$



Early Universe would have band structure --> interesting cosmology

S.W., Kane, Perry, and Adams, hep-th/06010054

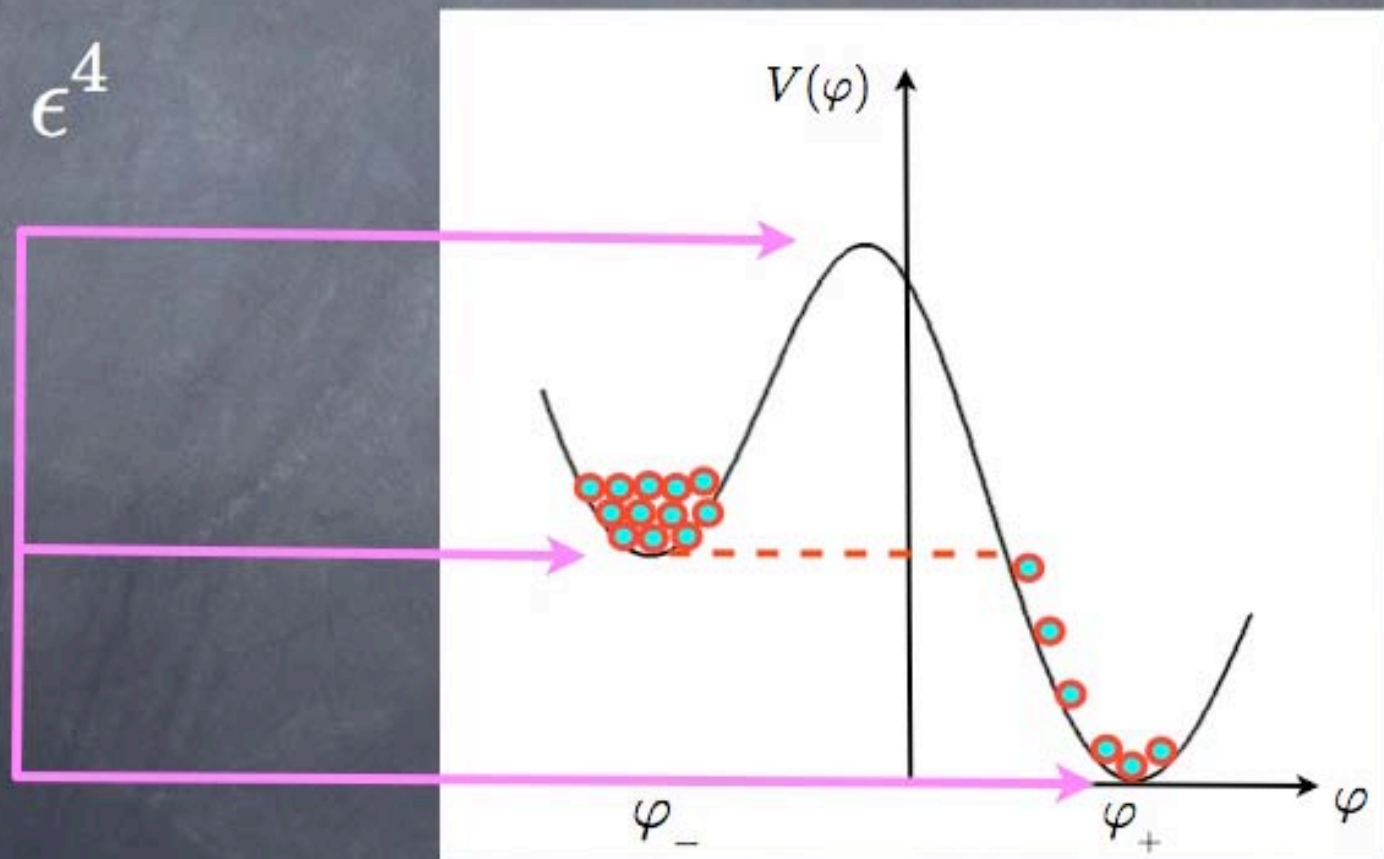
First Order Transitions

- Bubbles of new phase form in background of old phase
- Energy difference stored in walls / velocity typically relativistic
- Bubble collisions create regions of new phase as they collide
- Transition completes when all bubbles collide (percolation) and bath of radiation results

$$\xi^4 > \epsilon^4$$

$$\xi^4$$

$$\epsilon^4$$



The Bounce

$$\Gamma = Ae^{-B} \quad A \sim \epsilon^4$$

$$\epsilon^4 = V(\varphi_+) - V(\varphi_-)$$

$$B = S_E(\varphi_b) - S_E(\varphi_-)$$

Dimensionless Decay rate

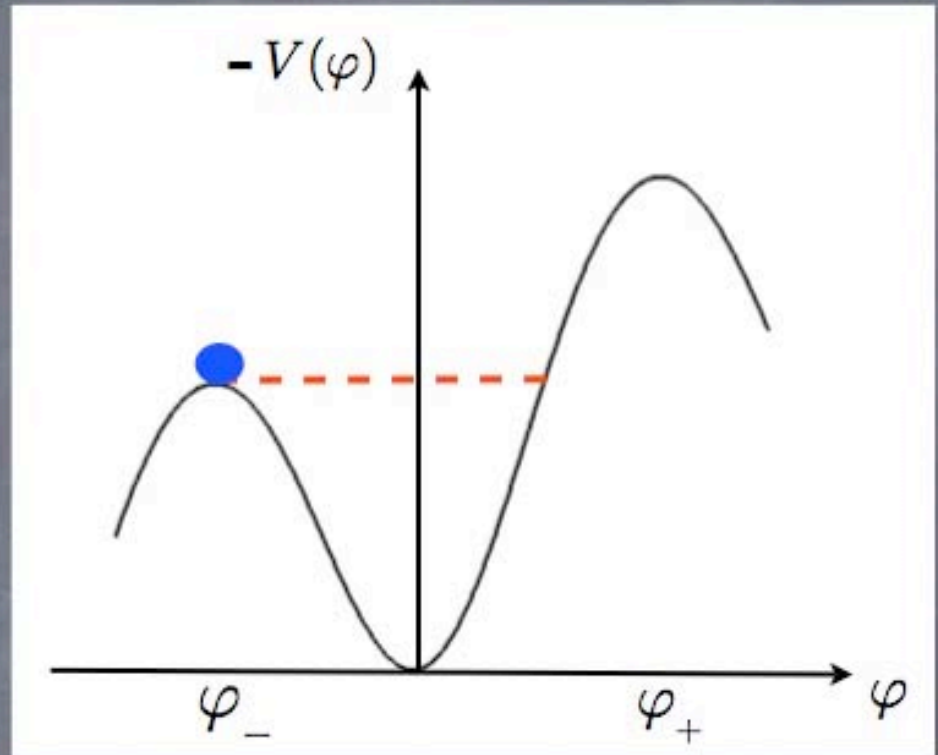
$$\beta = \frac{\Gamma}{H^4}$$

Percolation and e-folds

$$p(t) \sim e^{-\frac{4\pi}{3}\beta H t} \quad \tau \sim (\beta H)^{-1}$$

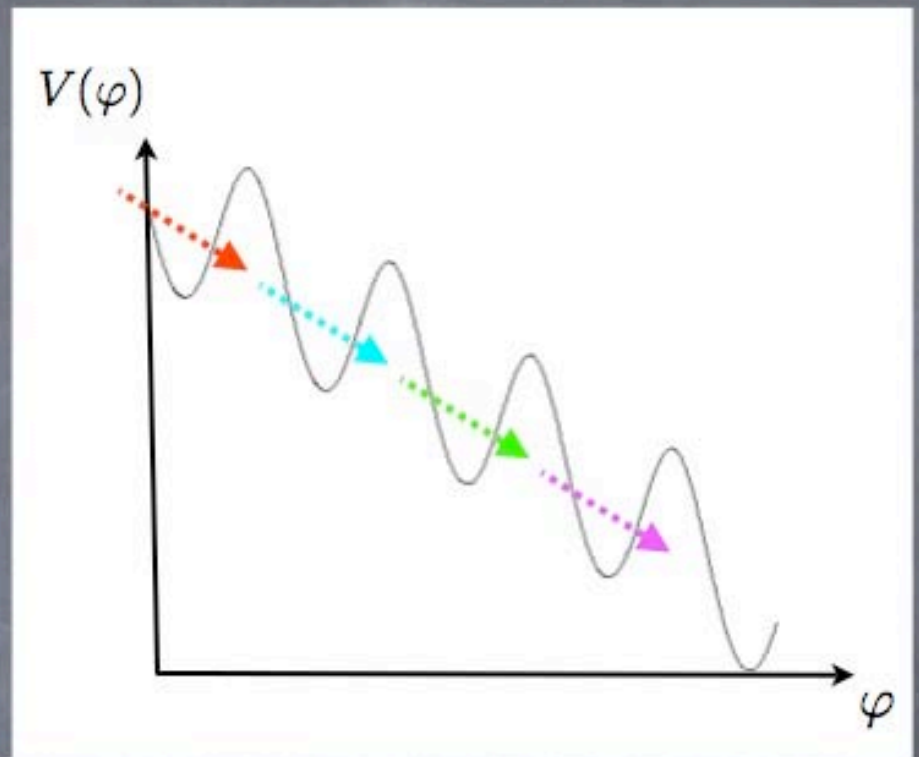
$$\beta \geq \frac{9}{4\pi} \quad \text{graceful exit} \quad \longrightarrow$$

$$\beta \ll 1 \quad \text{enough e-folds}$$



$$N = \int H dt \approx H\tau \leq \frac{1}{3}$$

$$N = \int H dt \approx H\tau \leq \frac{1}{3}$$



Observations:

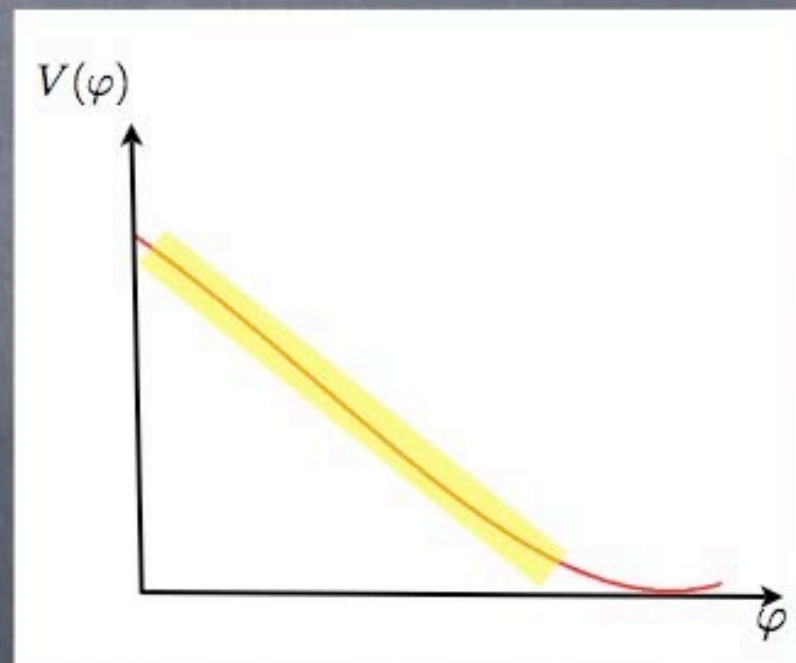
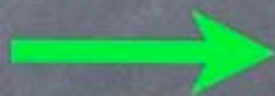
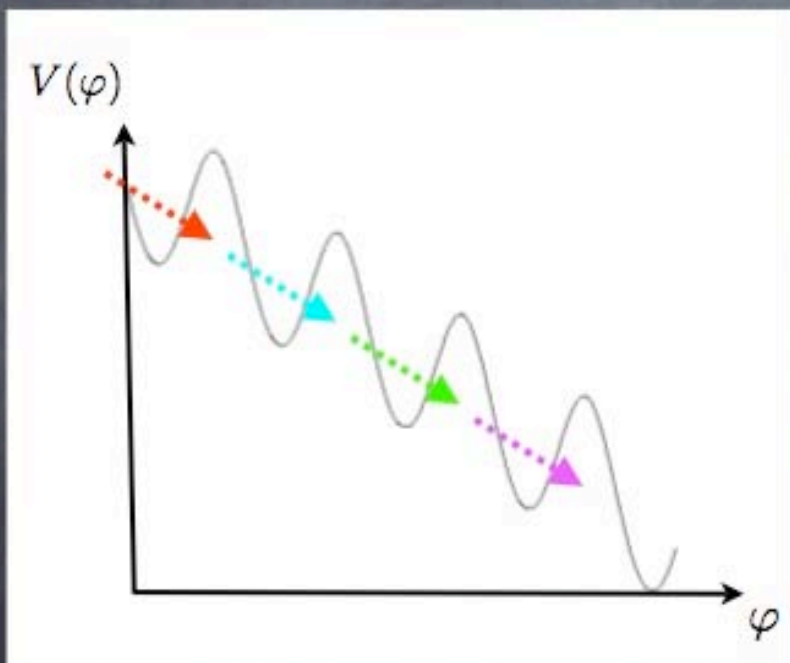
- Transitions will be weakly first order
- Characteristic bubble size \ll Hubble scale
(gravitational effects unimportant)

$$r_b \ll H^{-1} \quad r_b \sim \frac{\xi^2 \Delta\varphi}{\epsilon^4}$$

Hawking, Moss, and
Stewart Phys Rev D26 1982

Macroscopic description

- Coarse grain \rightarrow Bubbles act as radiation bath $r_b \ll H^{-1}$
- Slow roll inflation w/ radiation present



Cosmology with Multiple Fluids

$$\nabla_{\mu} T_{(\alpha)}^{\mu\nu} = Q_{(\alpha)}$$

$$\nabla_{\mu} T_{\text{total}}^{\mu\nu} = 0 \quad \sum_{\alpha} Q_{(\alpha)} = 0$$

$$\dot{\rho}_{\varphi} = -3H\dot{\varphi}^2 + Q_{\varphi}$$

$$\dot{\rho}_r = -4H\rho_r + Q_r$$

$$Q_{\varphi} = -Q_r$$

$$3H^2 = \frac{8\pi}{M_p^2} \rho$$

$$\dot{H} = -\frac{4\pi}{M_p^2} \left(\dot{\varphi}^2 + \frac{4}{3}\rho_r \right)$$

Inflation with Multiple Fluids

$$\epsilon = \frac{d}{dt} (H^{-1}) = 3\Omega_k + 2\Omega_r$$

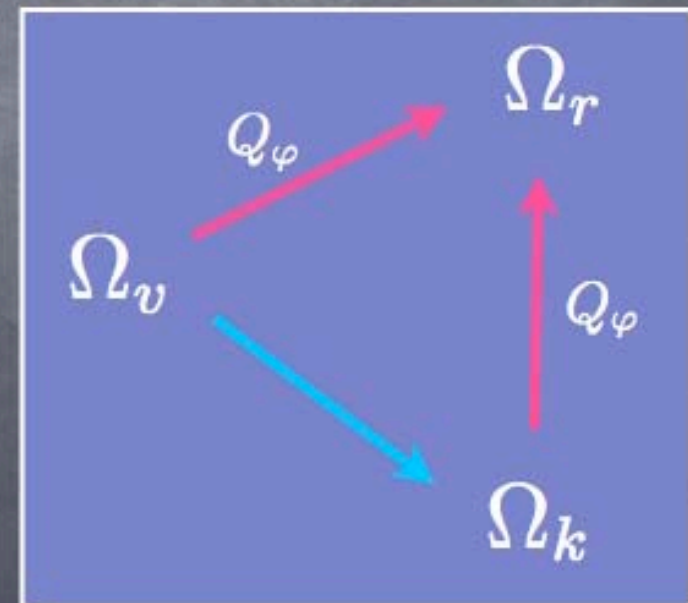
Standard slow roll
inflation

Effect of Bubbles

$$\Omega_k = \frac{\frac{1}{2}\dot{\varphi}^2}{\rho} \quad \Omega_r = \frac{\rho_r}{\rho} \quad \Omega_v = \frac{V(\varphi)}{\rho}$$

$$\Omega_k + \Omega_v + \Omega_r = 1$$

$$\ddot{a} > 0 \quad \longrightarrow \quad \epsilon < 1$$



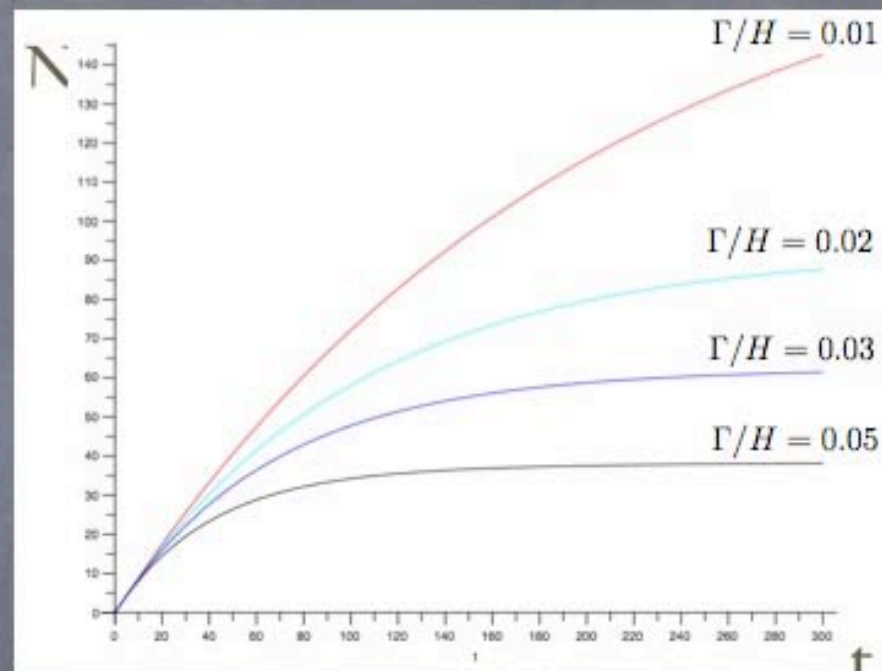
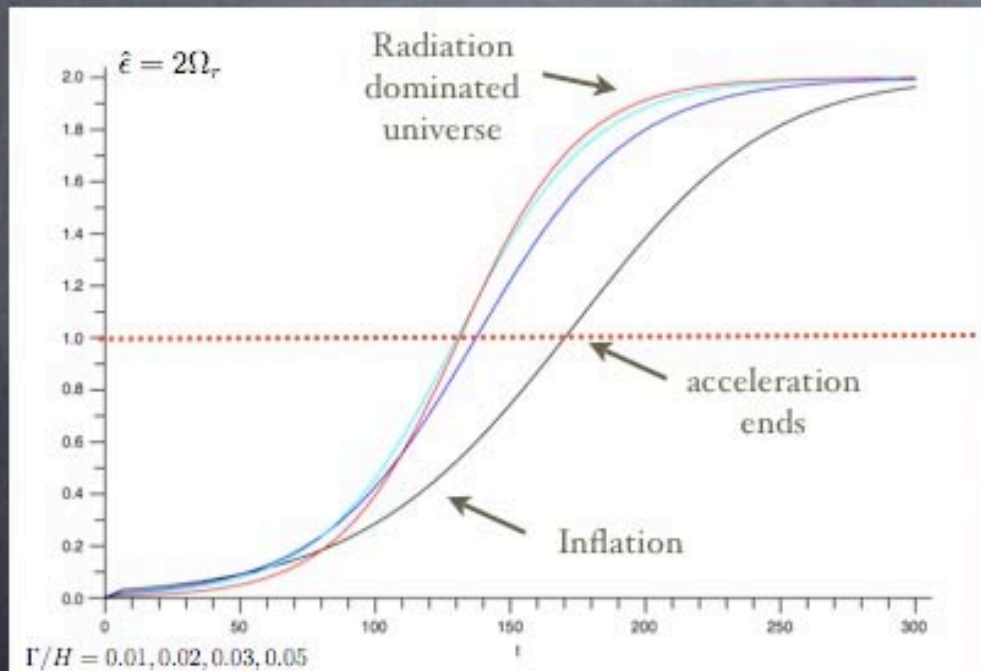
Example One: Inflation w/out inflatons

S.W., Perry, Kane, Adams hep-th/0610054

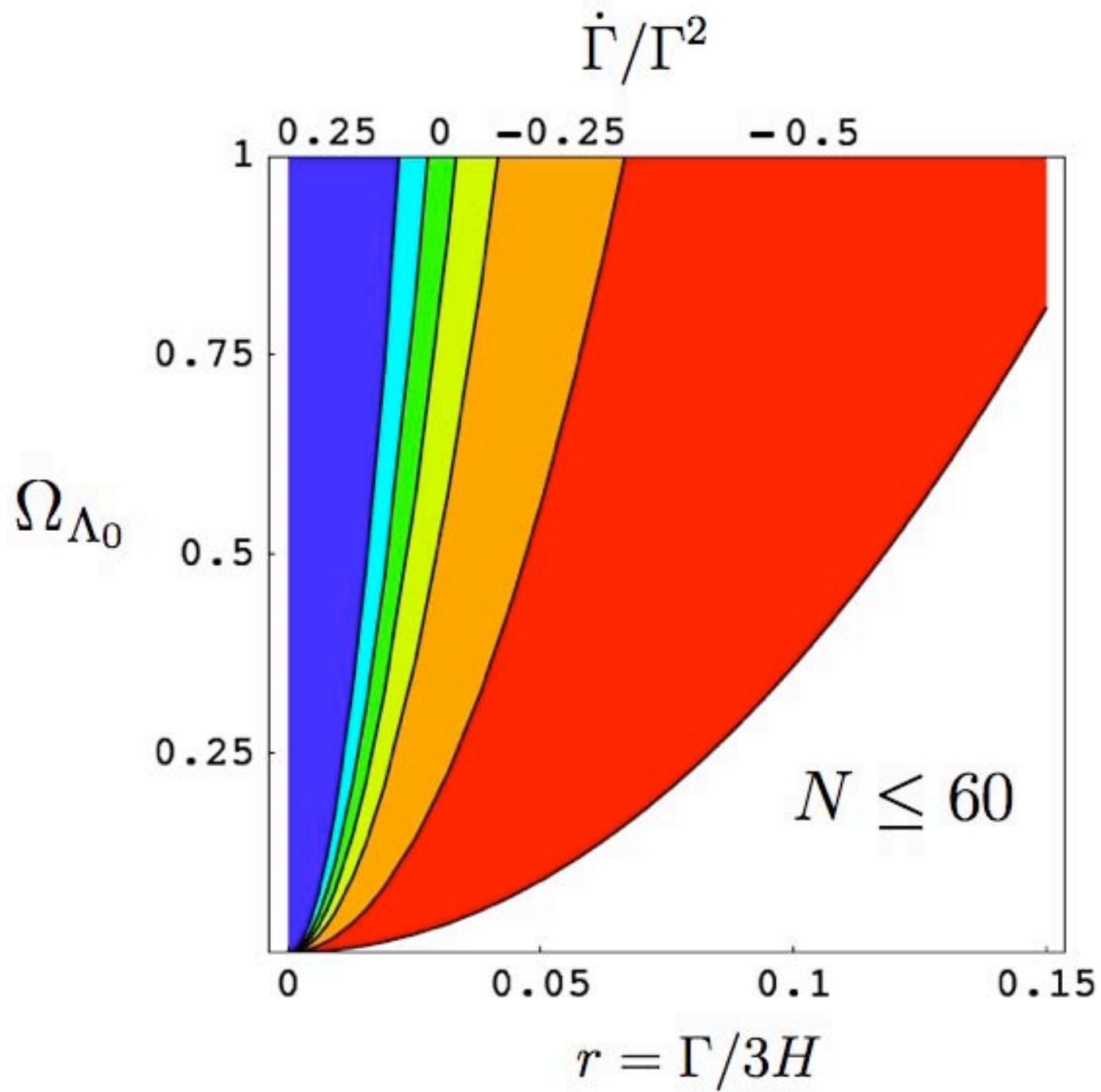
$$Q_\phi = -\Gamma\rho_\phi \quad \dot{\psi} = 0$$

$$\dot{\rho}_\Lambda = -\Gamma\rho_\Lambda$$

$$\dot{\rho}_r = -4H\rho_r + \Gamma\rho_\Lambda$$



$$r = \frac{\Gamma}{3H} \lesssim \frac{1}{150}$$



Example Two: Warm Inflation

Berera, astro-ph/9509049,

Criticism: Linde & Yokoyama hep-ph/9809409

$$Q_\varphi = -\Gamma\dot{\varphi}^2$$

$$\dot{\rho}_r = -4H\rho_r + \Gamma\dot{\varphi}^2$$

$$\dot{\rho}_\varphi = -3H\dot{\varphi}^2 - \Gamma\dot{\varphi}^2$$

Condition for inflation

$$\epsilon = \epsilon_\varphi(1+r) \ll 1$$

Three regimes

$$r = \frac{\Gamma}{3H} \gg 1$$

Warm Inflation

$$r = \frac{\Gamma}{3H} \approx 1$$

New regime (motivated by bubbles)

$$r = \frac{\Gamma}{3H} \ll 1$$

Standard inflation

Comments about Warm Inflation:

- Reheating is not necessary
- Potential can be less fine-tuned if many vacua are present (e.g. string landscape)
- Thermal correction to inflaton potential can be important (place for concern / fine tuning?)
- When vacuum energy \sim radiation density
- > interesting physics!
- Initial state is modified (transplanckian effects? [hep-th/0611277](#))

Density Perturbations

Scalar Metric Perturbations

(no anisotropic stress / longitudinal gauge / 1 d.o.f.)

$$ds^2 = -(1 + 2\Psi) dt^2 + a^2 (1 - 2\Psi) d\vec{x}^2$$

Curvature Fluctuation

$$\zeta = -\Psi - \frac{H}{\dot{\rho}} \delta\rho$$

$$\zeta_\alpha = -\Psi - \frac{H}{\dot{\rho}_\alpha} \delta\rho_\alpha$$

Entropy or Isocurvature Fluctuation

$$S_{\alpha\beta} = 3(\zeta_\alpha - \zeta_\beta)$$

Ex: Baryon / Photons (Isocurvature)

$$\delta\rho = 0 \rightarrow \delta\rho_b = -\delta\rho_\gamma \quad S_{b\gamma} = \frac{\delta(n_b/n_\gamma)}{n_b/n_\gamma}$$

Standard Scenario

Curvature Fluctuation

$$\zeta = -\Psi - \frac{H}{\dot{\rho}} \delta\rho$$

$$\dot{\zeta} = - \left(\frac{H}{\rho + p} \right) \delta P_{\text{NAD}}$$

$$\delta P_{\text{int}}^{(\alpha)} = \delta p^{(\alpha)} - c_{\alpha}^2 \delta\rho^{(\alpha)}$$

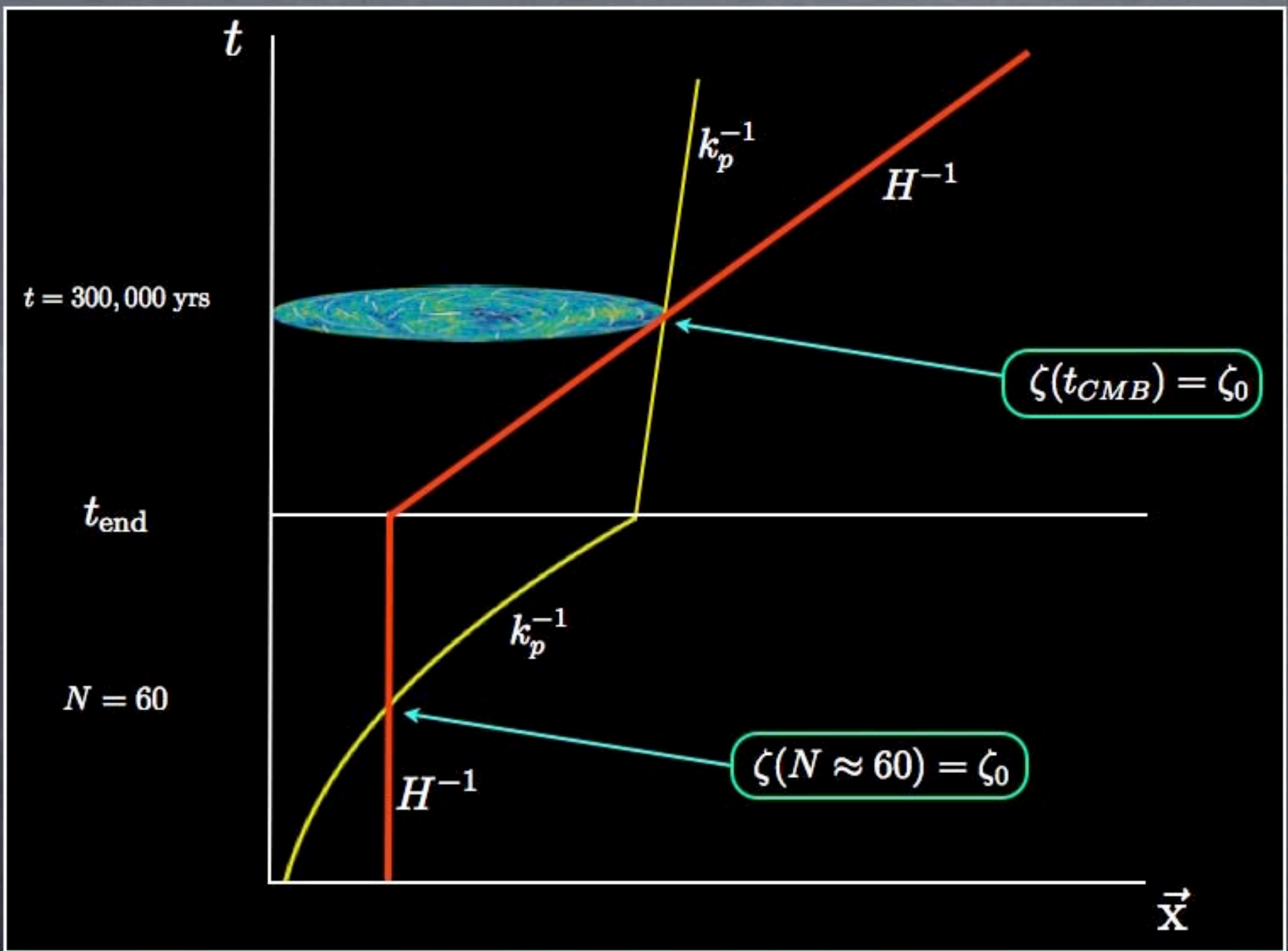
$$\delta P_{\text{rel}} \sim \sum_{\alpha\beta} S_{\alpha\beta}$$

Scalar field inflation

$$\delta P_{\text{int}}^{(\alpha)} \sim -k^2 \Psi$$

$$\dot{\zeta} \rightarrow 0 \quad k^{-1} \gg H^{-1}$$

Curvature perturbation conserved
on Super-Hubble scales



Density Fluctuations w/ multiple fluids (e.g. scalars)

$$\dot{\zeta} = - \left(\frac{H}{\rho + p} \right) \delta P_{\text{NAD}}$$

Multiple fields w/ significant interactions can lead to new generation mechanisms:

- Perturbations during (p)reheating
- Curvaton
- Modulated Perturbations

Upshot: Significant contribution to density fluctuations can result ***AFTER*** inflation ends or by fields other than inflaton!

Modulated Perturbations

- Dvali Gruzinov, Zaldarriaga astro-ph/0303591 & astro-ph/0305548
- Kofman astro-ph/0303614 & astro-ph/0403315
- Kofman & S.W. - in progress

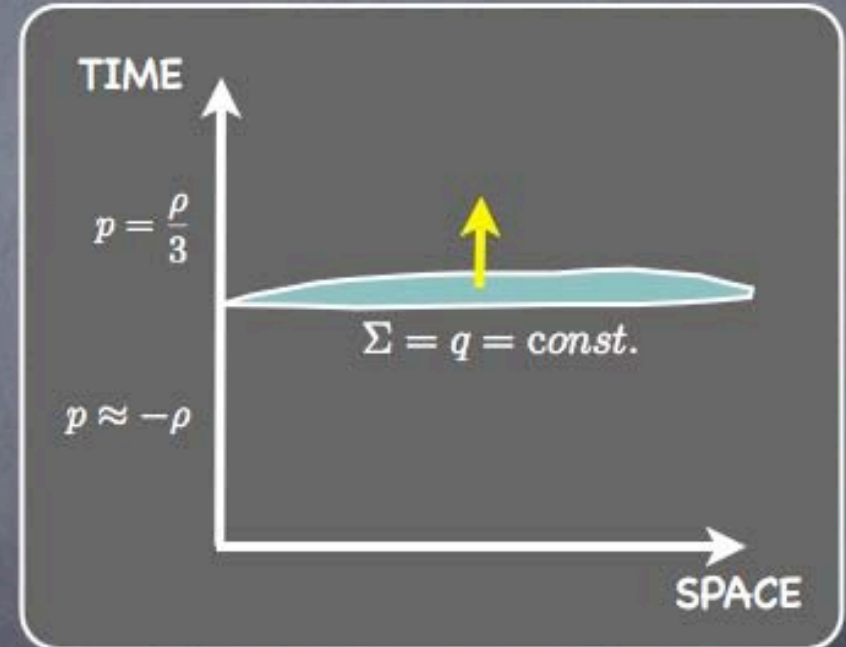
Light scalars during inflation

$$\delta\chi \sim \frac{H}{2\pi}$$

Couplings controlled by moduli
will fluctuate

$$V(\phi) = \frac{1}{2}m^2(\chi)\phi^2 + \lambda^4(\chi)\phi^4$$

$$\frac{\delta\chi}{\chi} \rightarrow \left(\frac{\delta m}{m} \text{ or } \frac{\delta\lambda}{\lambda} \right) \rightarrow \frac{\delta\rho}{\rho} \rightarrow \frac{\delta T}{T}$$



Density Perturbations for Bubbles

Key Observations

$$r = \frac{\Gamma}{3H} \leq 1$$

$$\epsilon = 3\Omega_k + 2\Omega_r \ll 1$$

$$\rho_r \ll \rho_\varphi \rightarrow \delta\rho_r \ll \delta\rho_\varphi$$

Significant entropy perturbation can develop,
but radiation ultimately dominates washing out entropy perturbations
(c.f. Curvaton, Modulated Perturbations)

Density Perturbations for Bubbles

$$\dot{\zeta} = -\frac{H}{\rho + p} \delta P_{\text{nad}} + \frac{k^2}{3Ha^2} (\Psi - \zeta) + \frac{k^4}{9\dot{H}Ha^4} \Psi,$$

$$\dot{\Psi} = -\left(H - \frac{\dot{H}}{H}\right) \Psi - \frac{k^2}{3Ha^2} \Psi + \frac{\dot{H}}{H} \zeta,$$

$$\dot{\nu}_\phi = -\left(\frac{Q_\phi(1 + c_\phi^2)}{\dot{\phi}^2} - \frac{Q_\phi}{\dot{\phi}^2} - 3Hc_\phi^2 - \frac{2V'}{\dot{\phi}}\right) \nu_\phi - \Psi + \frac{\dot{\rho}_\phi}{H\dot{\phi}^2} (\zeta_\phi + \Psi),$$

$$\dot{\zeta}_\phi = \frac{3H^2}{\dot{\rho}_\phi} \delta P_{\text{int}}^\phi - \frac{H}{\dot{\rho}_\phi} (\delta Q_{\text{int}}^\phi + \delta Q_{\text{rel}}^\phi) + \frac{k^2}{3Ha^2} \left(\frac{Q_\phi}{\dot{\rho}_\phi} \Psi + \left[1 - \frac{Q_\phi}{\dot{\rho}_\phi}\right] H\nu_\phi\right),$$

$$\delta P_{\text{nad}} = \frac{2V'\dot{\phi}}{H} (\zeta_\phi + \Psi + H\nu_\phi) + \frac{\dot{\rho}_\phi}{H} (c_r^2 - c_\phi^2) (\zeta - \zeta_\phi),$$

$$\delta P_{\text{int}}^\phi = \frac{2V'\dot{\phi}}{H} (\zeta_\phi + \Psi + H\nu_\phi),$$

$$\delta Q_{\text{int}}^\phi = \delta Q_\phi + \frac{\dot{Q}_\phi}{H} (\zeta_\phi + \Psi),$$

$$\delta Q_{\text{rel}}^\phi = \frac{Q_\phi \dot{\rho}}{2H\rho} (\zeta - \zeta_\phi),$$

Density Perturbations for Bubbles

Power Spectrum

$$P_\zeta = \frac{1}{4\pi^2 c_s \epsilon} \left(\frac{H}{M_p} \right)^2 (-kc_s \eta)^{-2\epsilon} \quad \epsilon = 3\Omega_k + 2\Omega_r$$

Scalar Tilt:

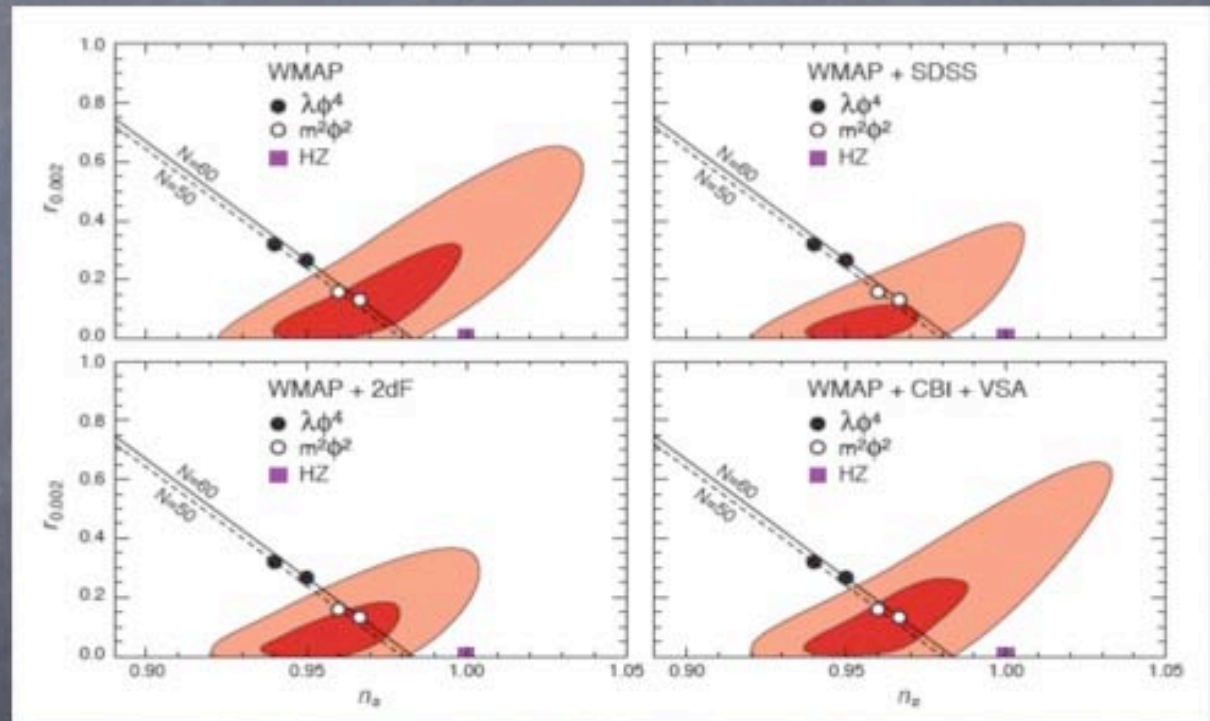
$$n_s = 1 + \frac{d \ln P_\zeta}{d \ln k} = 1 - 2\epsilon$$

Gravity Waves

$$P_h = \frac{8}{\pi^2} \left(\frac{H}{M_p} \right)^2 (-k\eta)^{-2\epsilon}$$

Tensor to Scalar ratio:

$$r = \frac{P_h}{P_\zeta} = 16\epsilon c_s$$



Single field slow-roll models

Conclusions

- Moduli Trapping offers a way to stabilize moduli near locations of higher symmetry
- Rapid transitions through landscape (1st or 2nd order) suggests new approach to fine tuning issues (replaced by energy splitting)
- Cosmological Perturbations are consistent with observations
- May be additional signatures.. gravity waves? tensor/scalar?
- Much left to explore...