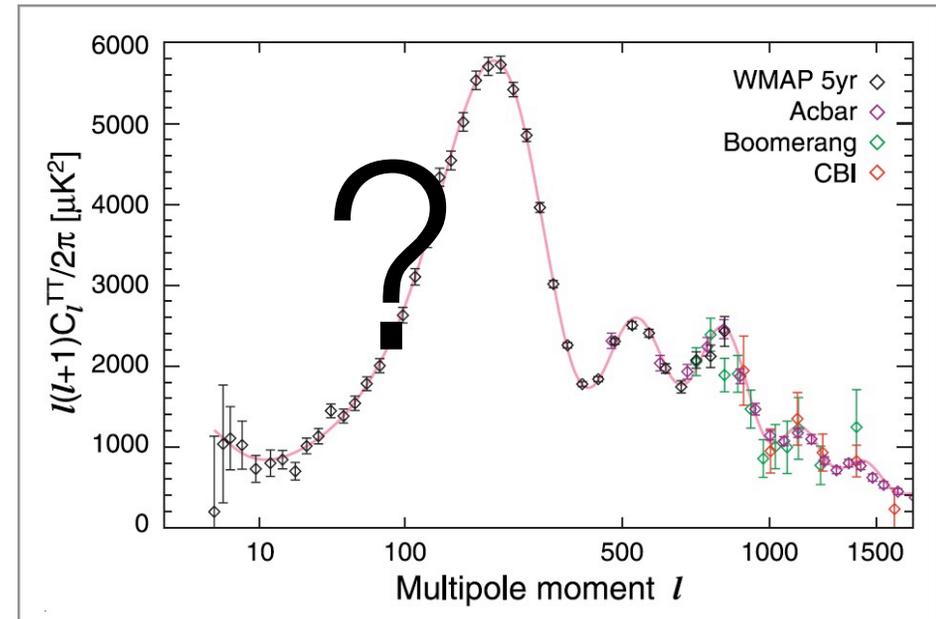
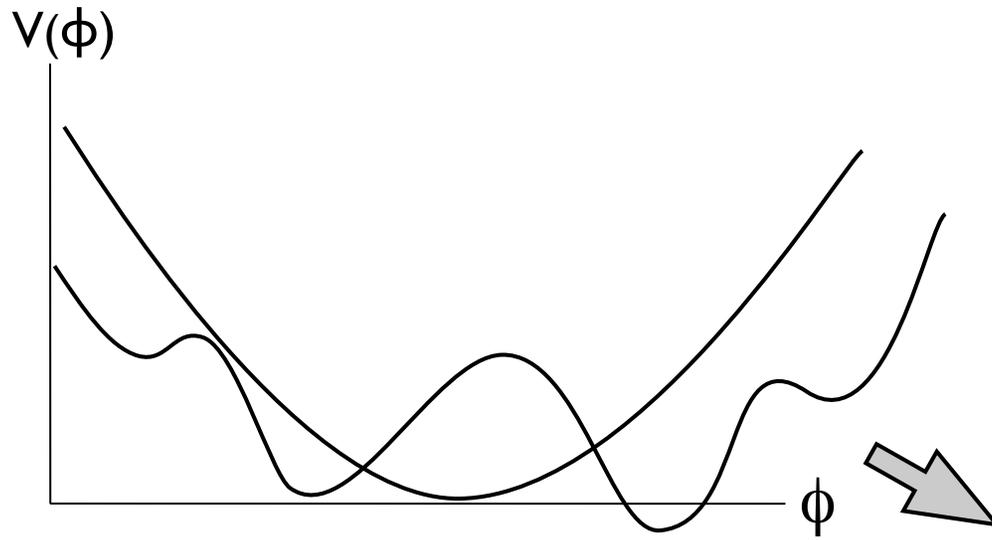


A status report on the observability of cosmic bubble collisions

Anthony Aguirre, UC Santa Cruz

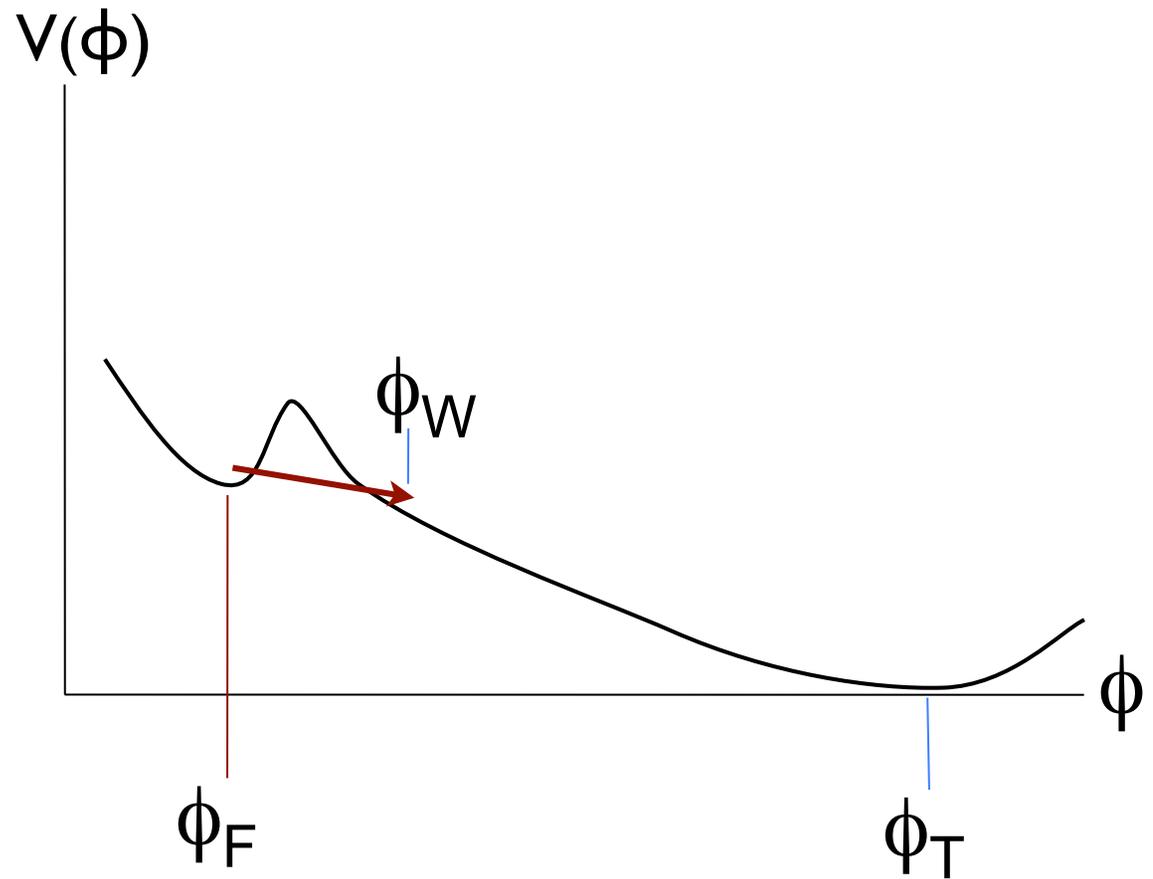
(work with M. Johnson, A. Shomer, M. Tysanner, J. Kozaczuk)

Inflation



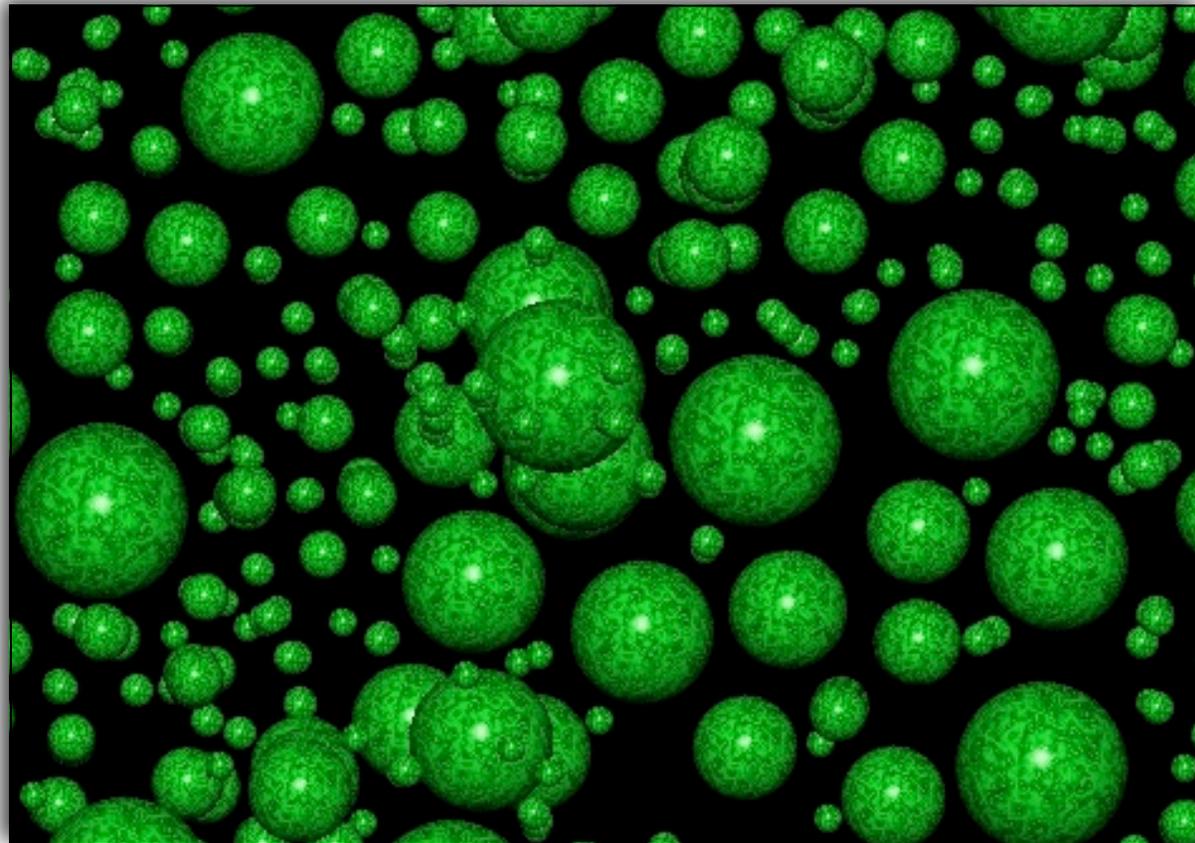
Everlasting open inflation

- (Multiple minima) + (slow transitions) = **eternal inflation**



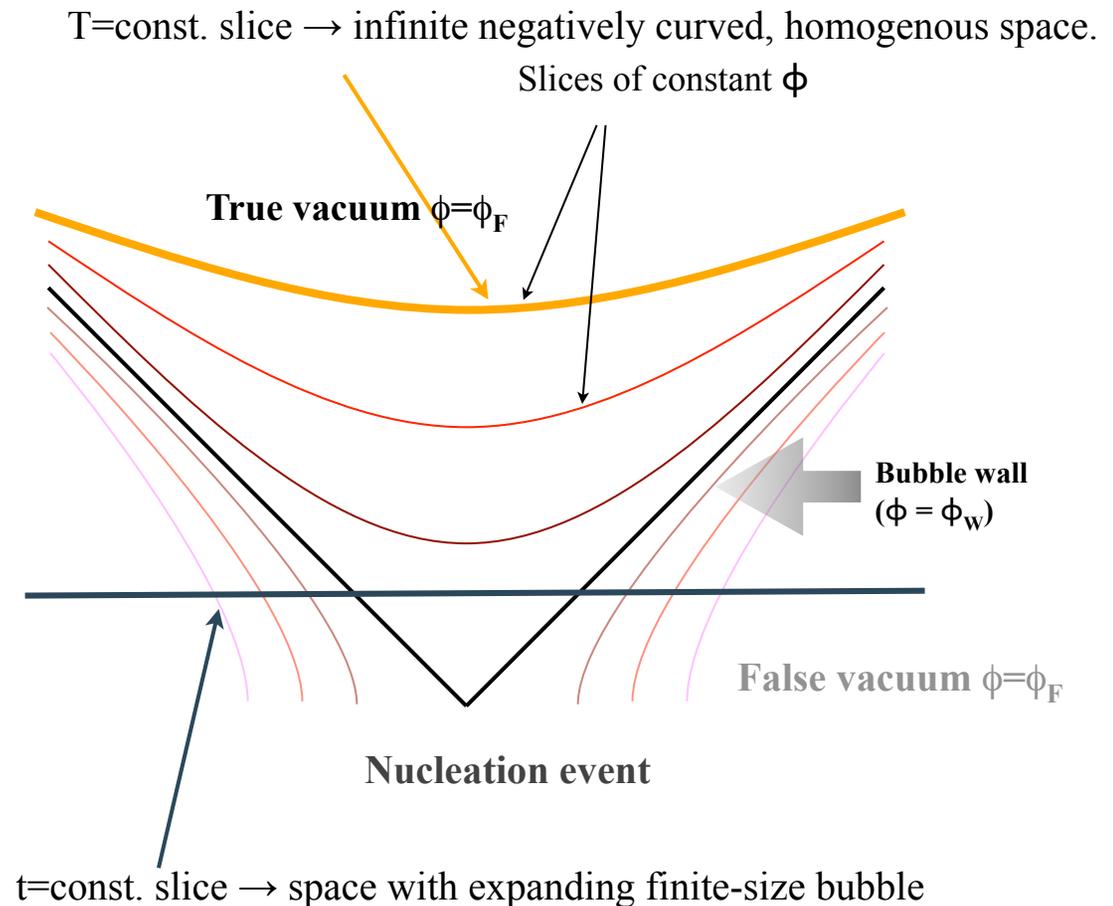
Everlasting open inflation

- (Multiple minima) +
(slow transitions)
= **eternal inflation**



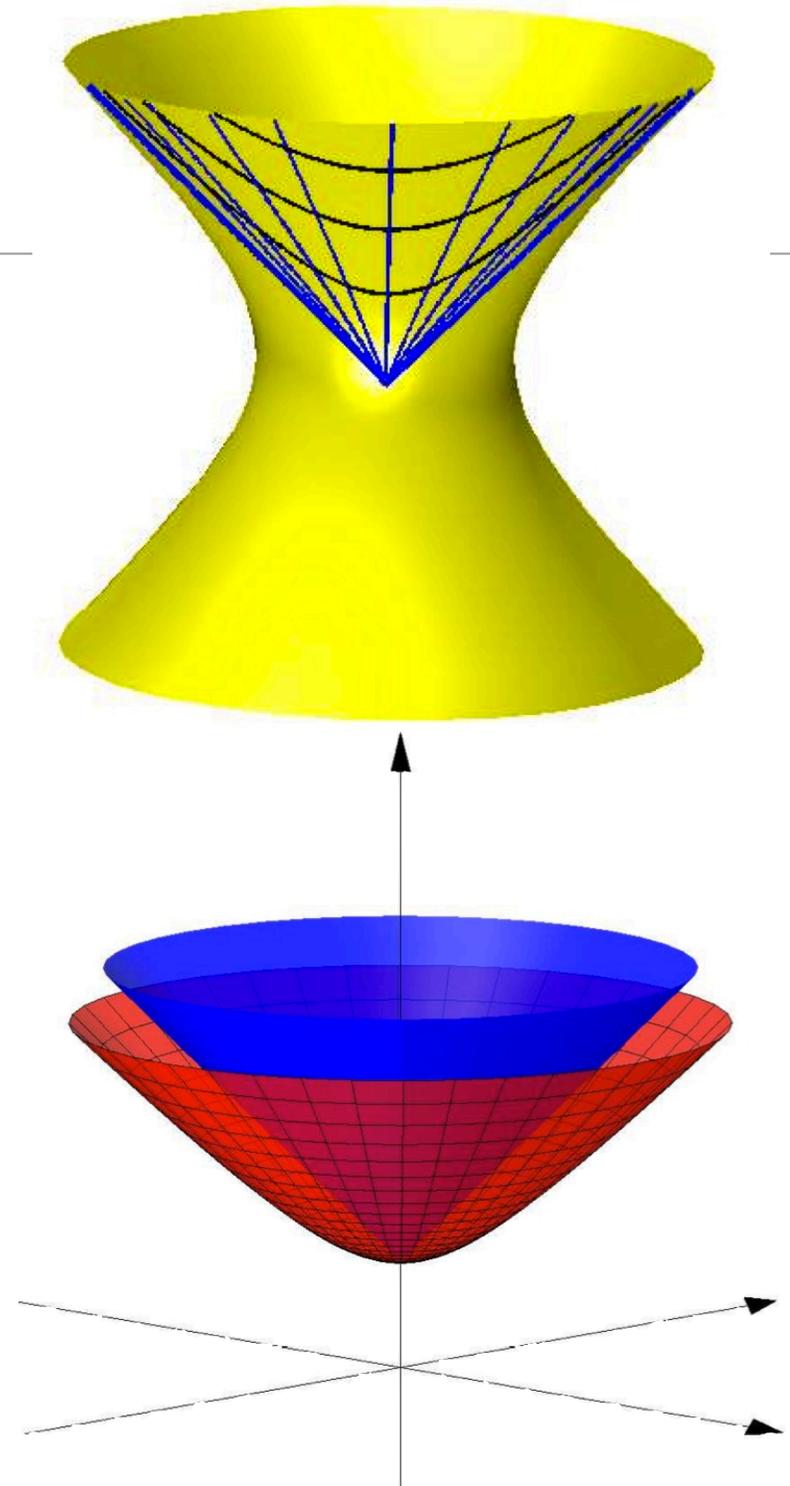
Everlasting open inflation

- (Multiple minima) + (slow transitions) = **eternal inflation**
- Each bubble has **open FRW cosmology** inside.



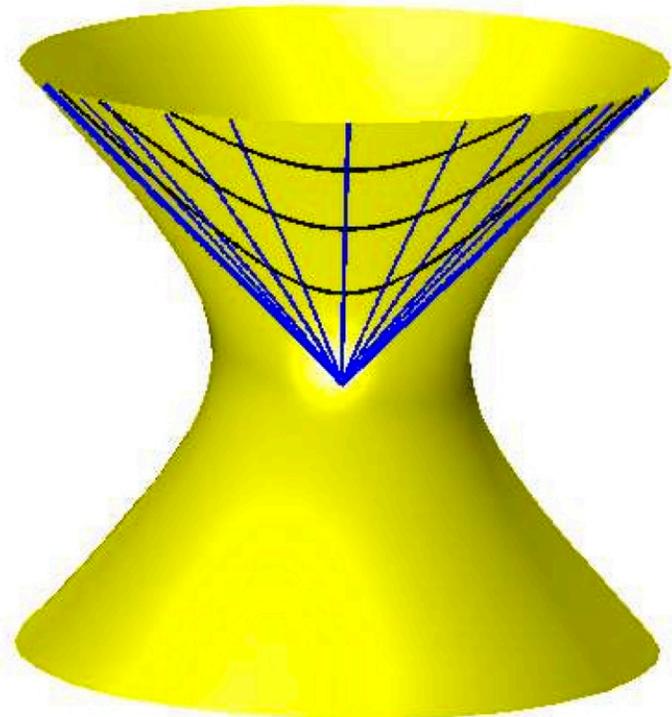
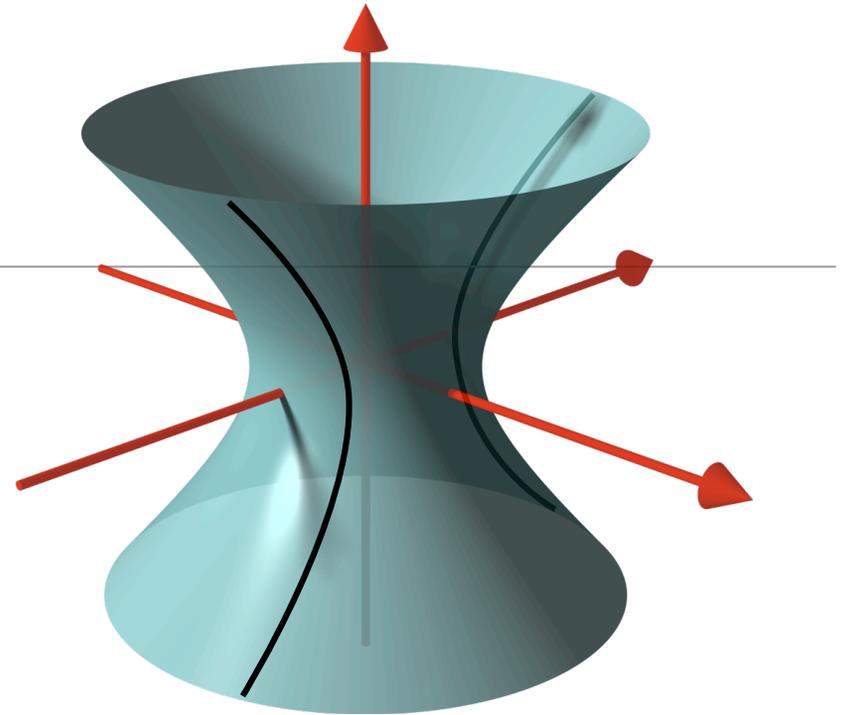
An embedded bubble

- D-dim de Sitter (dS)
 - Hyperboloid in D+1 Mink.
 - Maximally $SO(D,1)$ symmetric
- $X_i = \text{const.} > H^{-1} \rightarrow$ spacelike D-1 hyperboloid.
 - This is 'open slicing'.



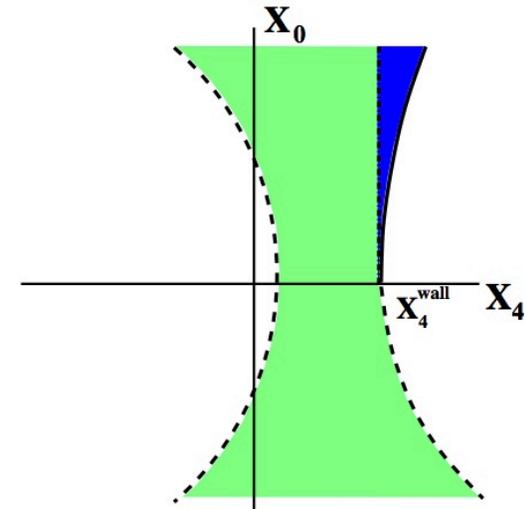
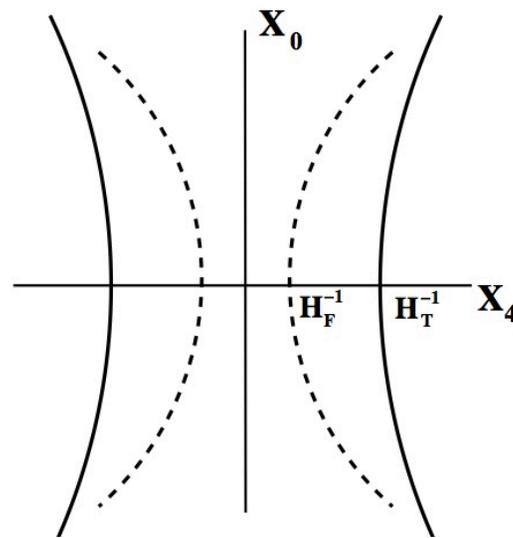
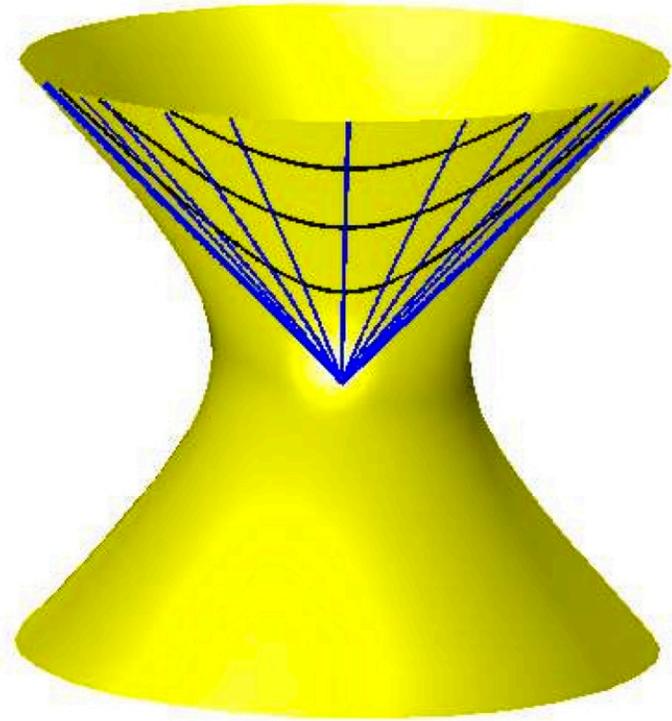
An embedded bubble

- $X_i = \text{const.} > H^{-1} \rightarrow$ timelike D-1 hyperboloid (D-2 sphere of constant outward acceleration)
- $X_i = \text{const.} = H^{-1} \rightarrow$ null cone.
- Boosts \parallel to X_i translate 'origin'.
- Boosts \perp to X_i do nothing overall, but translate points on D-1 hyperboloid.

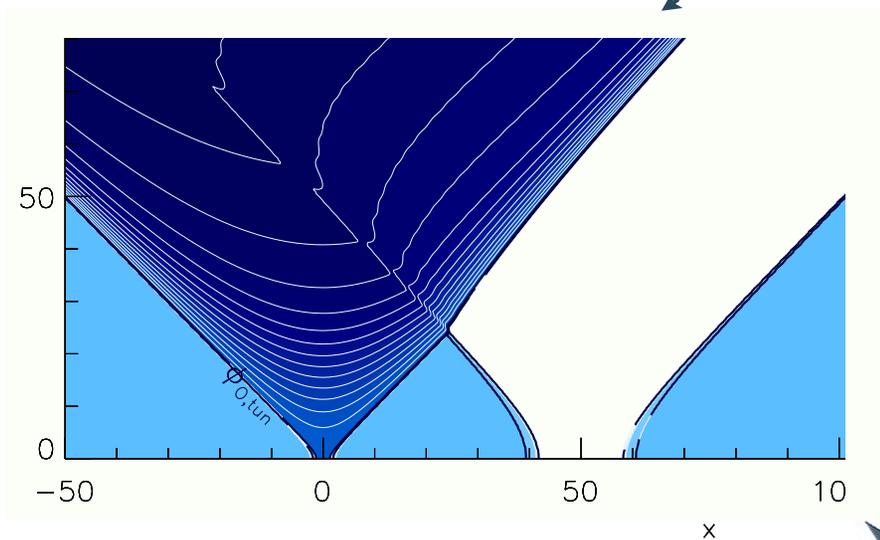
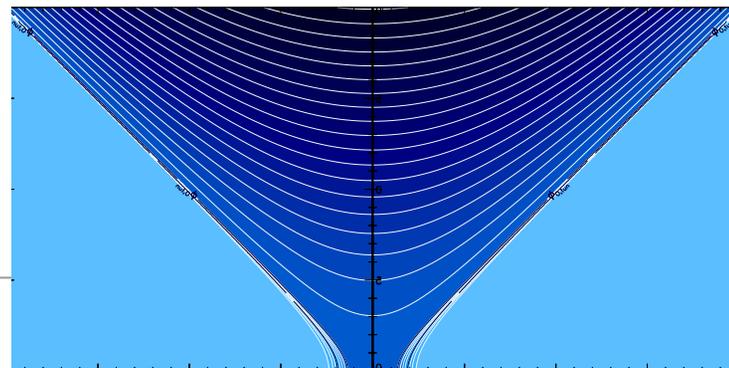


An embedded bubble

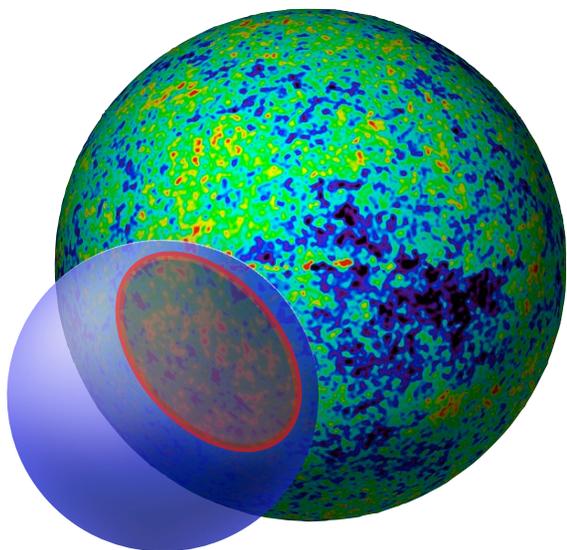
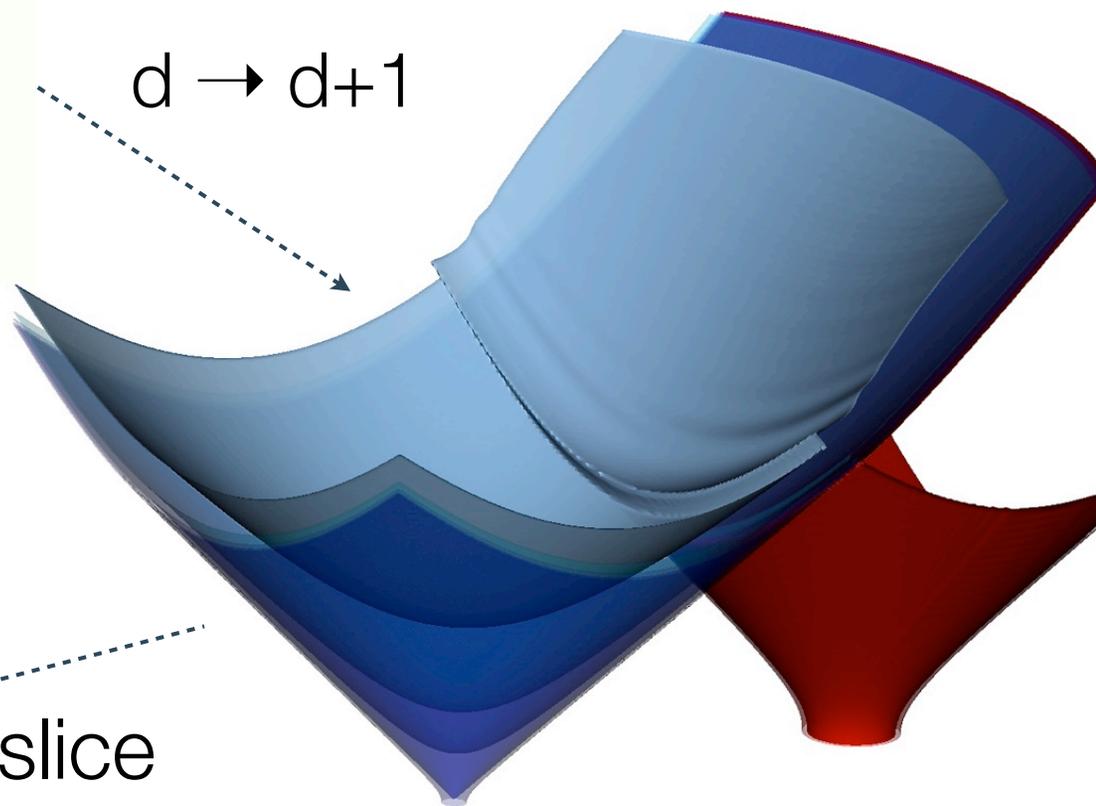
- Can embed arbitrary open FRW cosmology in similar manner; has $SO(D-1,1)$ symmetry, described by one parameter.
- Can match across timelike hyperboloid for 'vacuum bubble' like thin-wall CDL



Bubble collisions



$d \rightarrow d+1$



slice

Bubbles collide. Can we see the other ones?

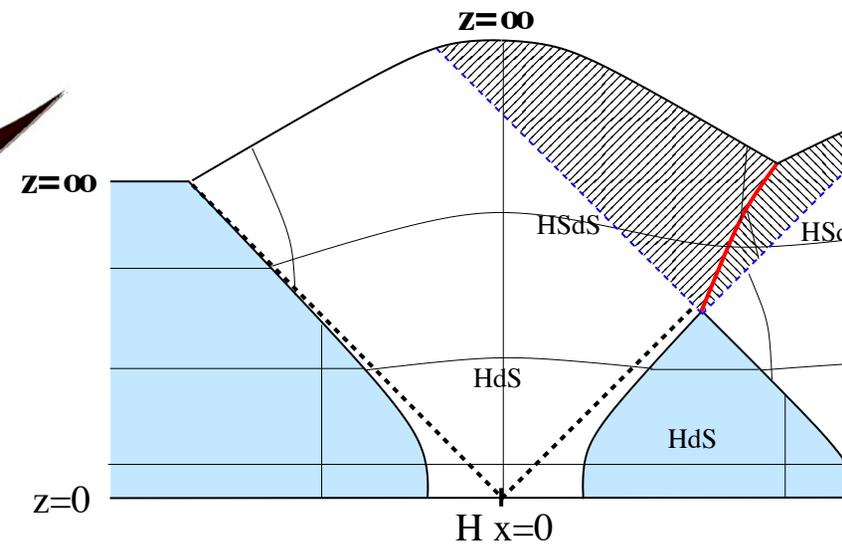
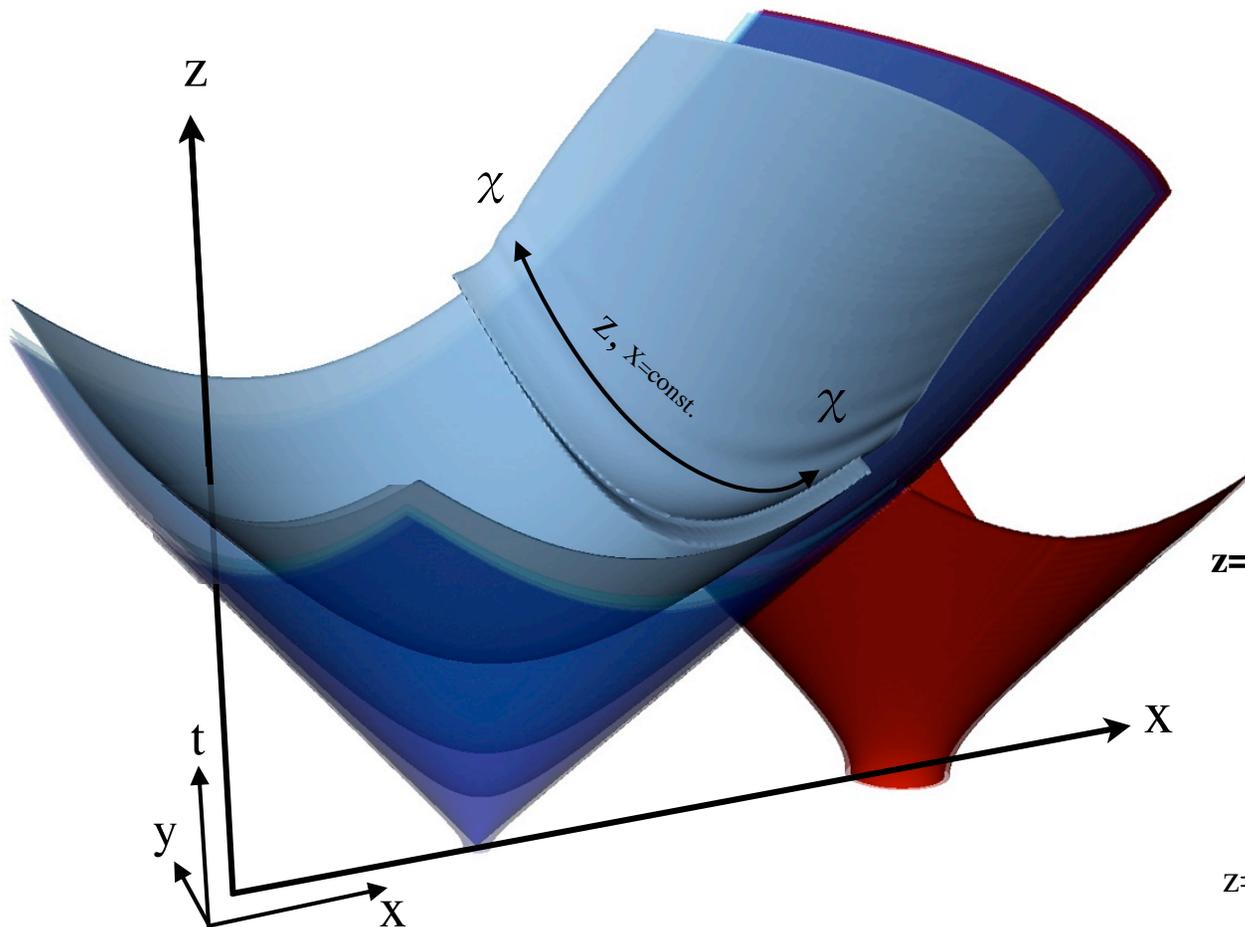
Three basic issues:

- What is the structure of a general collision spacetime?
- What is effect on post-collision observers?
 - **Non-existent**: No collisions exist in observer's past lightcone.
 - **Invisible**: unobservable effect.
 - **Perturbative**: small effect observable but not yet observed.
 - **Falsifiable**: incompatible with our observations, but not with observers.
 - **Fatal**: collisions prevent the formation of observers to their future.
- How could we observe **perturbative** or **falsifiable** effects?
- What are the relative probabilities for these five, especially:
 $(\text{falsifiable} + \text{perturbative}) / (\text{fatal} + \text{non-existent} + \text{invisible})$

What is the structure of a post-collision spacetime?

Basic Structure

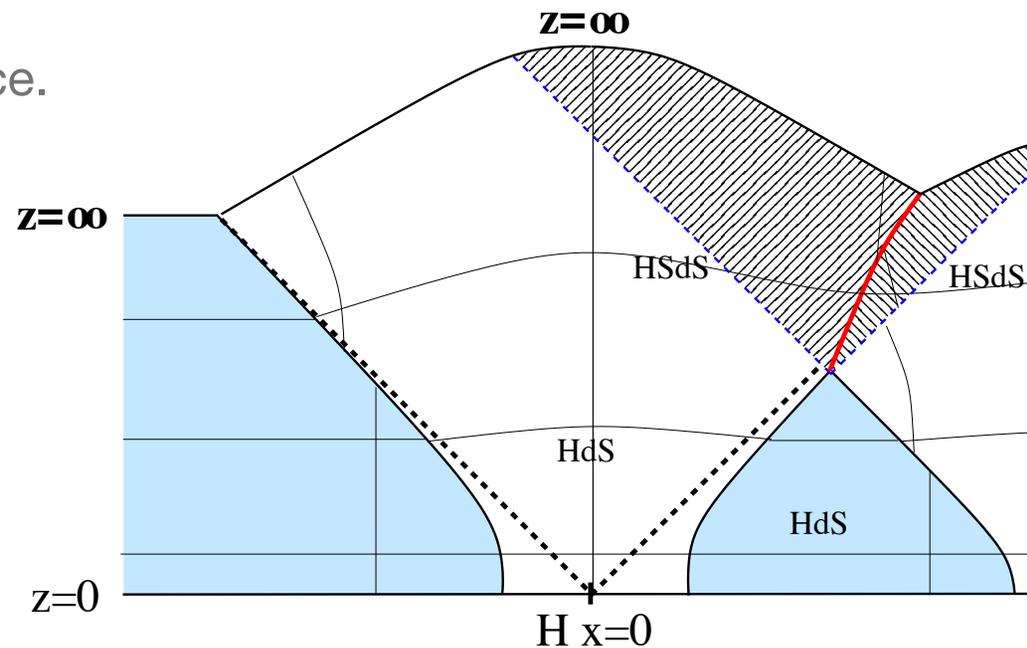
Each: $SO(3,1)$
Together: $SO(2,1)$



What is the structure of a post-collision spacetime?

Model I: Exact Solutions splicing vacuum bubbles

- Aguirre & Johnson 08 (or Chang, Kleban & Levi 08): generalize Freivogel, Horowitz & Shenker 07.
 - Small bubbles, Hyperbolic symmetry, thin walls connecting vacuum regions.
 - Thin domain wall between post-collision bubbles, tension κ
 - Radiation 'shell' from collision surface.
- Equations from:
 - Junction across shell
 - Junction across wall
 - Energy Conservation
- All determined by potential, initial separation, one unknown quantity (microphys.)

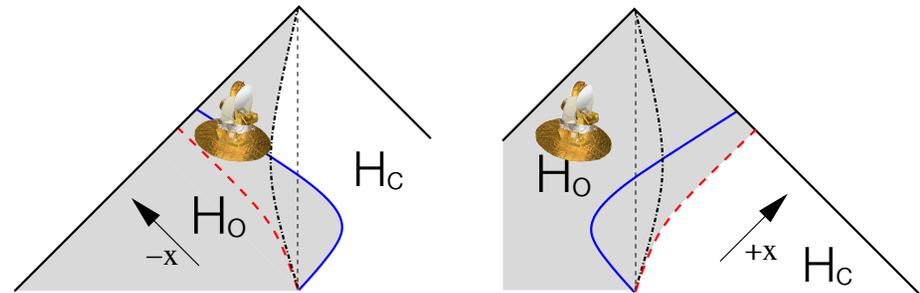


What is the structure of a post-collision spacetime?

Model I: Exact Solutions splicing vacuum bubbles

- Results:

- Asymptotic trajectory determined by vacuum energies, wall tension.
- Roughly, accelerates towards higher vacuum energy.
- Null shell necessary, but small overall effect possible.
- Do constant field surfaces near domain wall go timelike or spacelike?

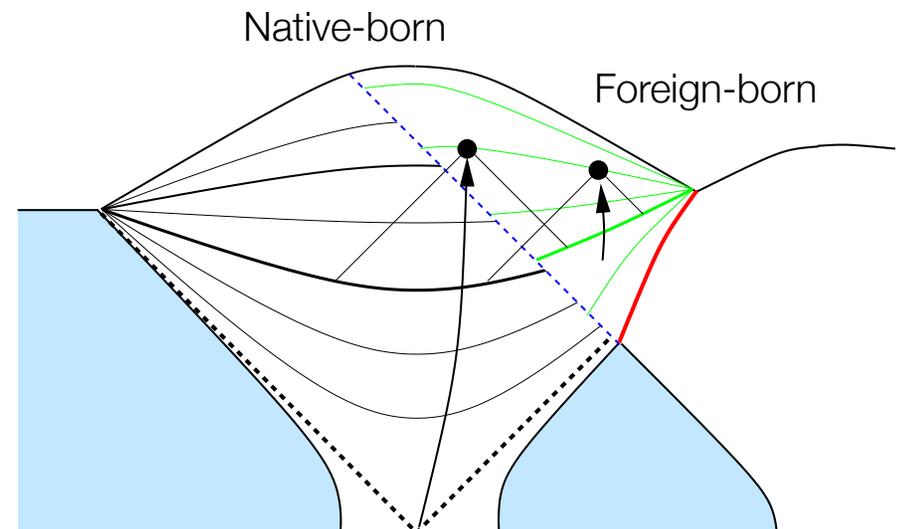


$$H_C^2 \leq H_o^2 - \kappa^2$$

(fatal)

$$H_C^2 \geq H_o^2 - \kappa^2$$

(falsifiable/perturbative/
invisible)

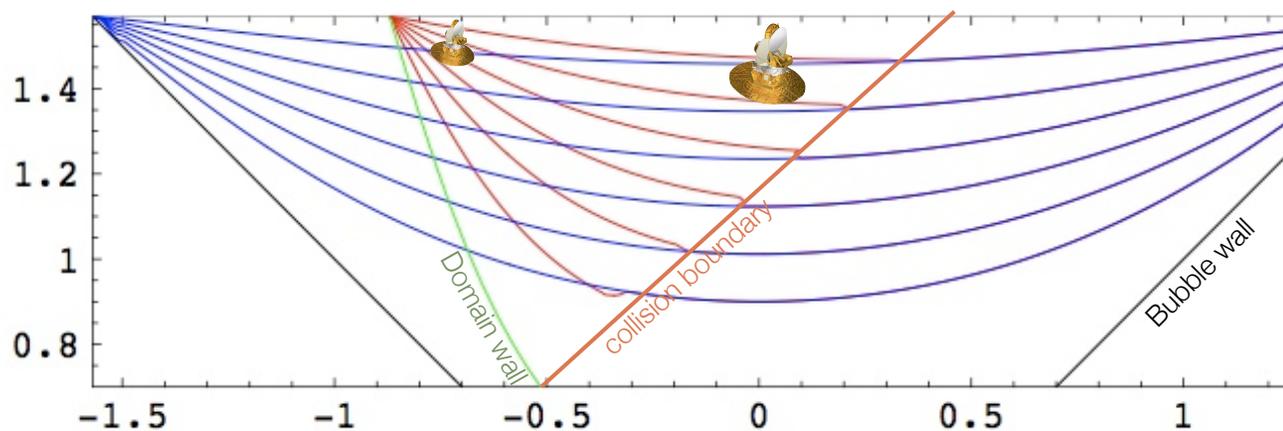


What is the structure of a post-collision spacetime?

Model II: Analytic model in fixed bubble background

- Chang, Kleban & Lev 09
 - Look at bubble interior, with fixed dS background.
 - Linear potential, boundary conditions on bubble wall and collision boundary
 - Joined by ‘null wave’ collision boundary with discontinuous field derivative.

- Asymptotically lines *look* timelike, but are spacelike (Aguirre et al. 09): very ‘foreign’ observers are possible, way up the domain wall.

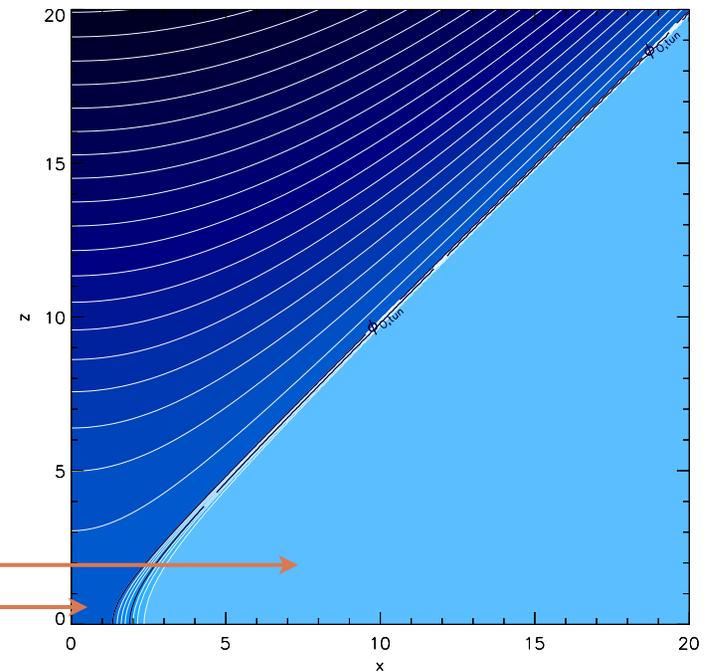
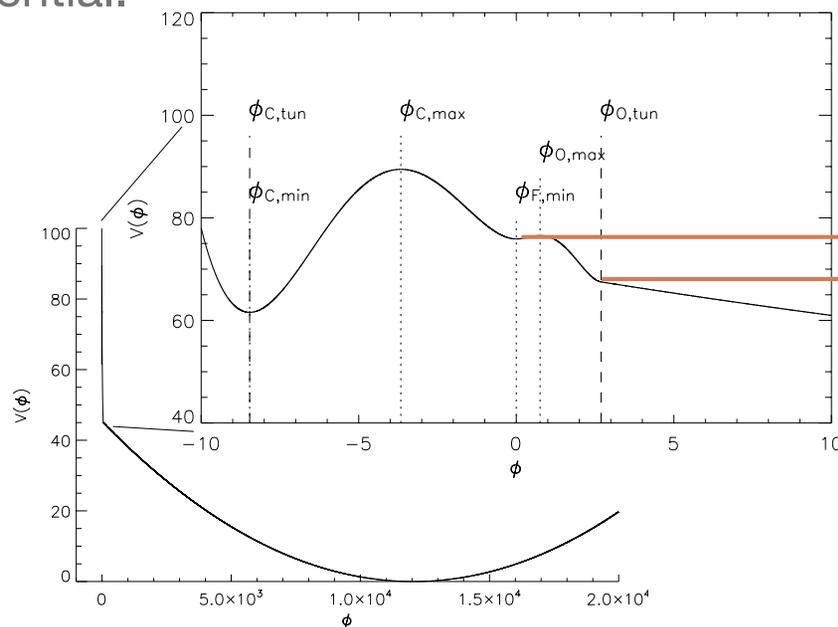


(adapted from) Chang et al. 09

What is the structure of a post-collision spacetime?

Model III: Numerical solutions in flat background

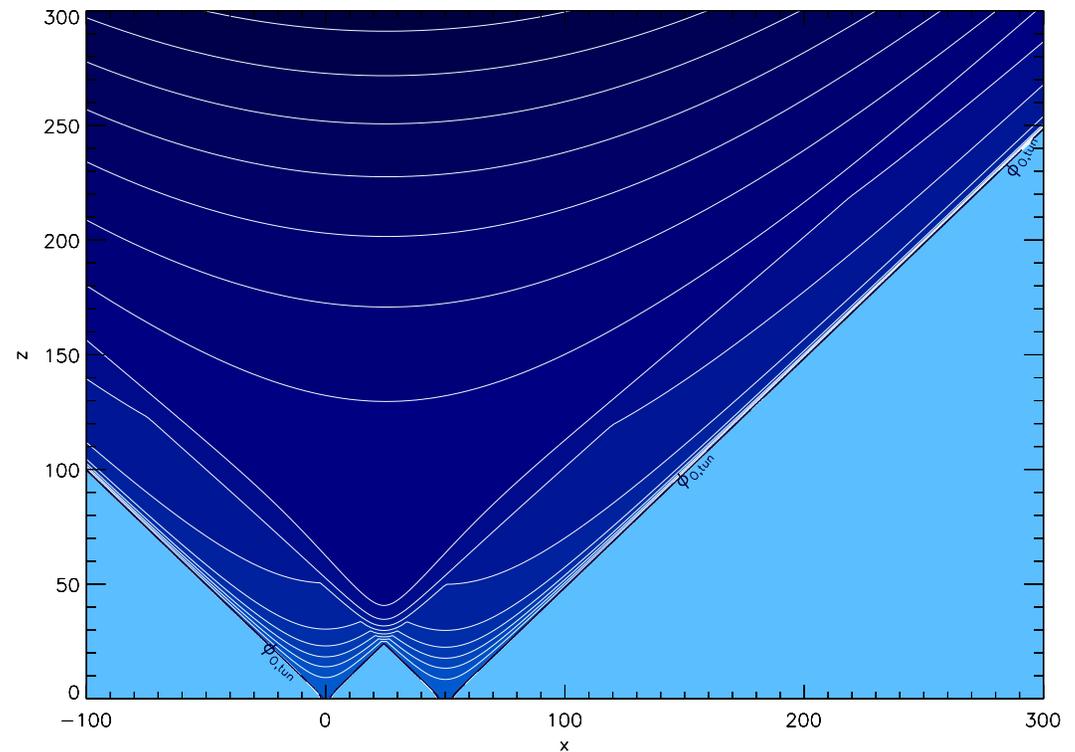
- Aguirre, Johnson & Tysanner 09
 - Single-field, flat background
 - Initial conditions from patched-together instantons for small bubbles.
 - ‘large-field’ inflation triple-well potential.



What is the structure of a post-collision spacetime?

Model III: Numerical solutions in flat background

- Aguirre, Johnson & Tysanner 09
 - Bubble self-collisions: merge into homogeneous* slices!
(const. field lines are hyperbolas)

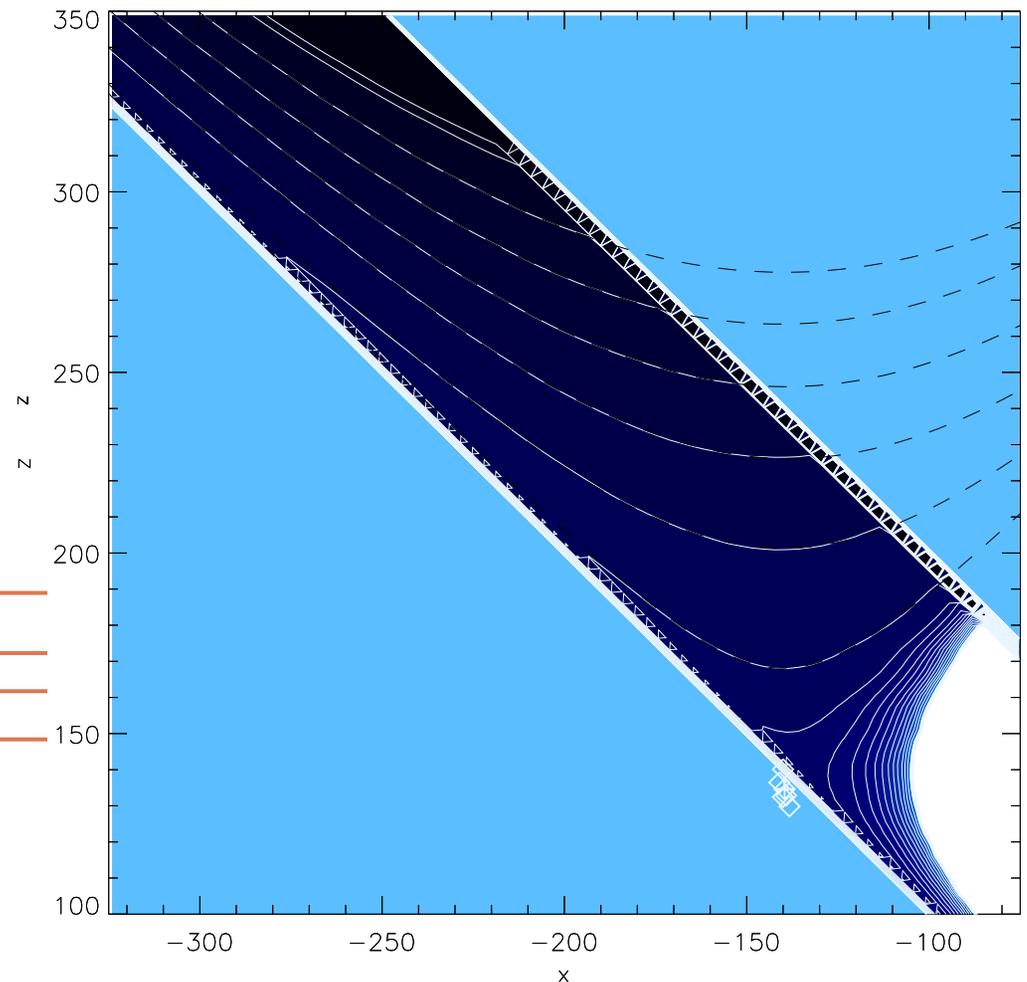
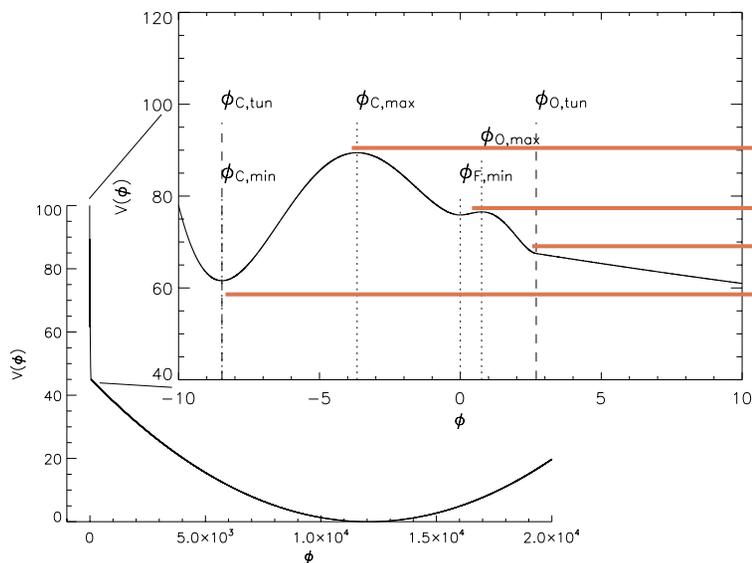


*really they are homogeneous in two directions with an axial symmetry. But at large z they regain homogeneity.

What is the structure of a post-collision spacetime?

Model III: Numerical solutions in flat background

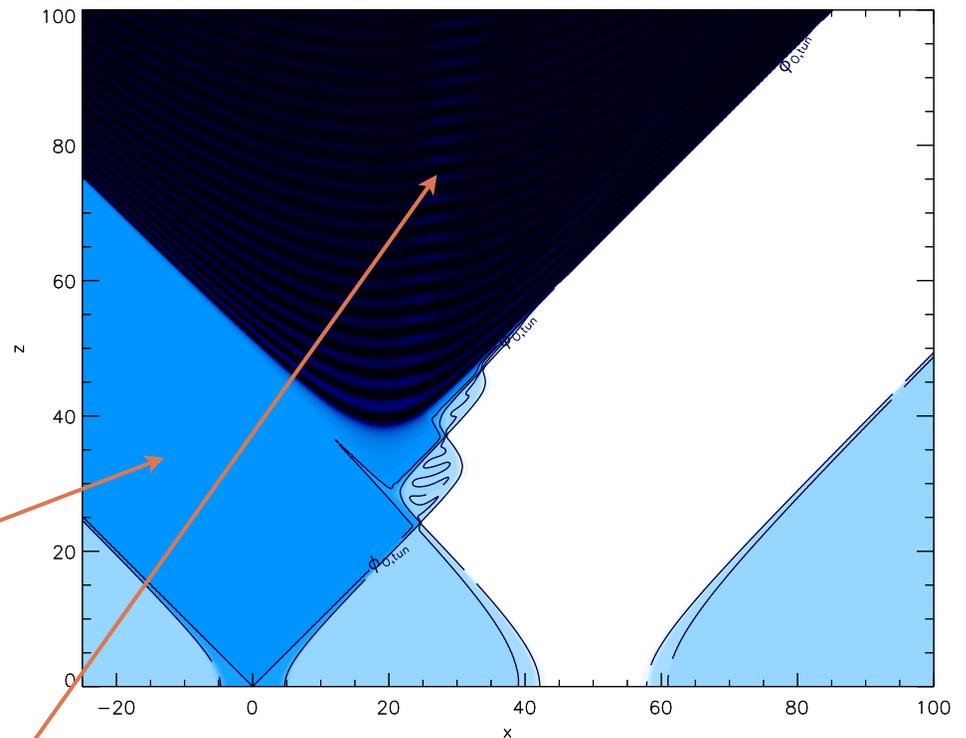
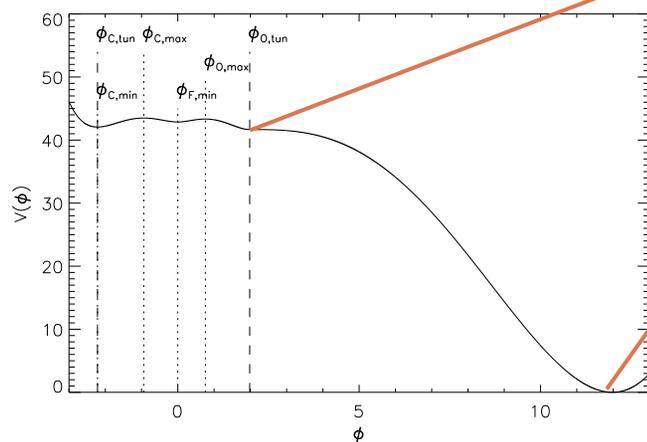
- Aguirre, Johnson & Tysanner 09
 - Bubble self-collisions: merge into homogeneous slices!
 - Two different bubbles: some perturbation, then return to homogeneity.



What is the structure of a post-collision spacetime?

Model III: Numerical solutions in flat background

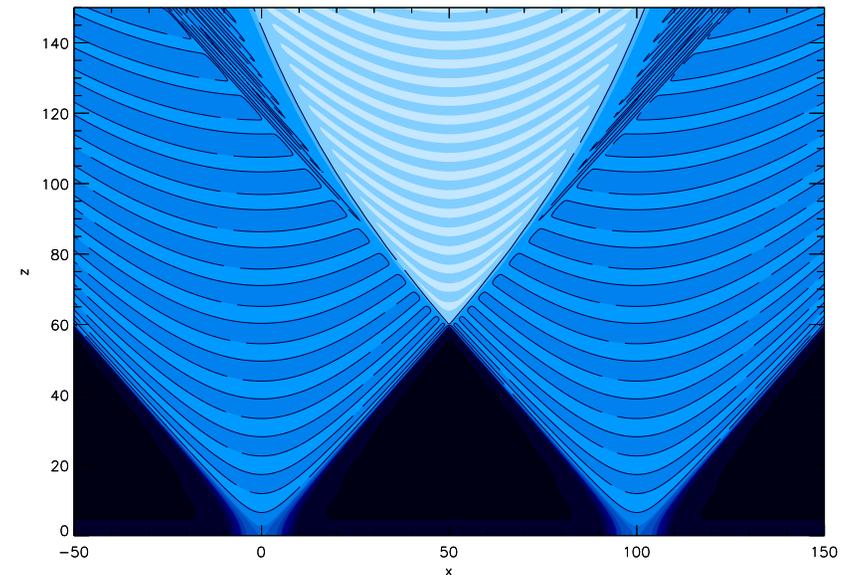
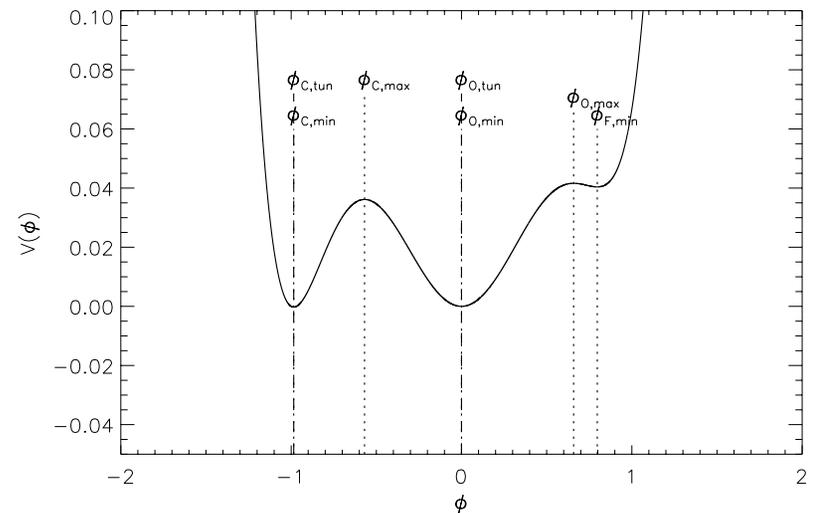
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 - Bubble self-collisions: merge into homogeneous slices!
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 - But: if inflation is 'fine tuned', disrupted in collision region: no foreign-born, perhaps fatal



What is the structure of a post-collision spacetime?

Model III: Numerical solutions in flat background

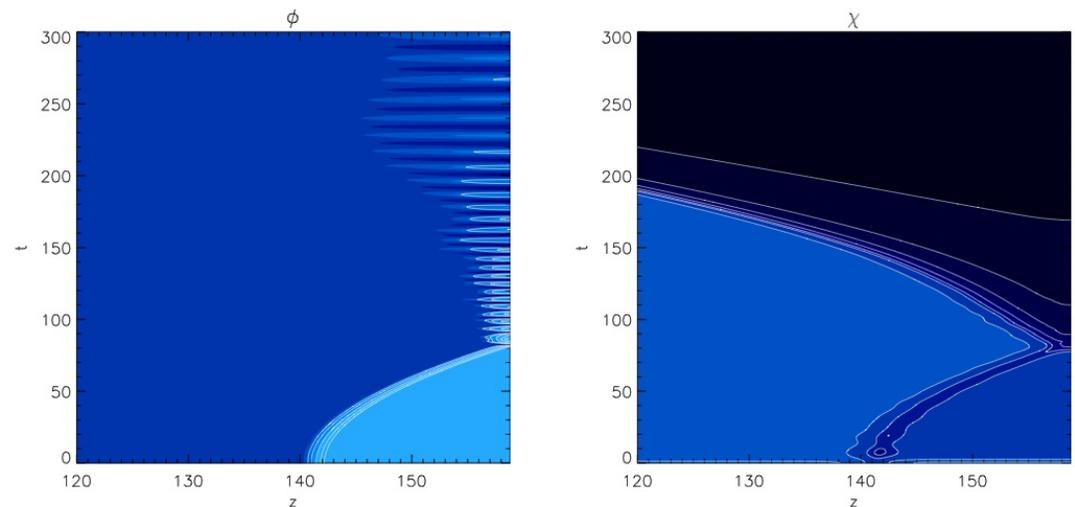
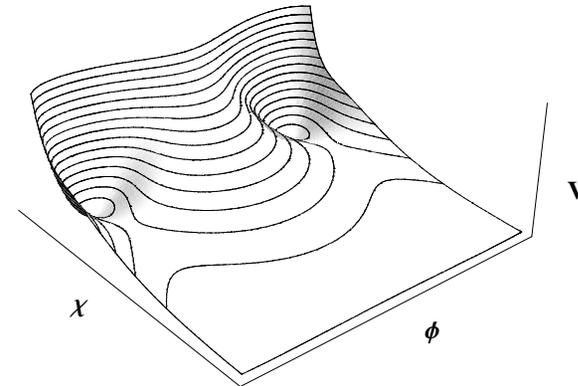
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 - Bubble self-collisions: merge into homogeneous slices!
 - Two different bubbles: some perturbation, then return to homogeneity.
 - But: if inflation is 'fine tuned', disrupted in collision region: no foreign-born, perhaps fatal
 - Many more possibilities:
 - Form yet lower vacuum bubbles (Easter et al. 09)



What is the structure of a post-collision spacetime?

Model III: Numerical solutions in flat background

- Aguirre, Johnson & Tysanner 09
 - Bubble self-collisions: merge into homogeneous slices!
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 - Many more possibilities:
 - Form yet lower vacuum bubbles (Easter et al.)
 - Multifield: lots more.



Collision-induced decompactification
(Aguirre, Johnson & Larfours 10)

What is the structure of a post-collision spacetime?

Model III: Numerical solutions in flat background

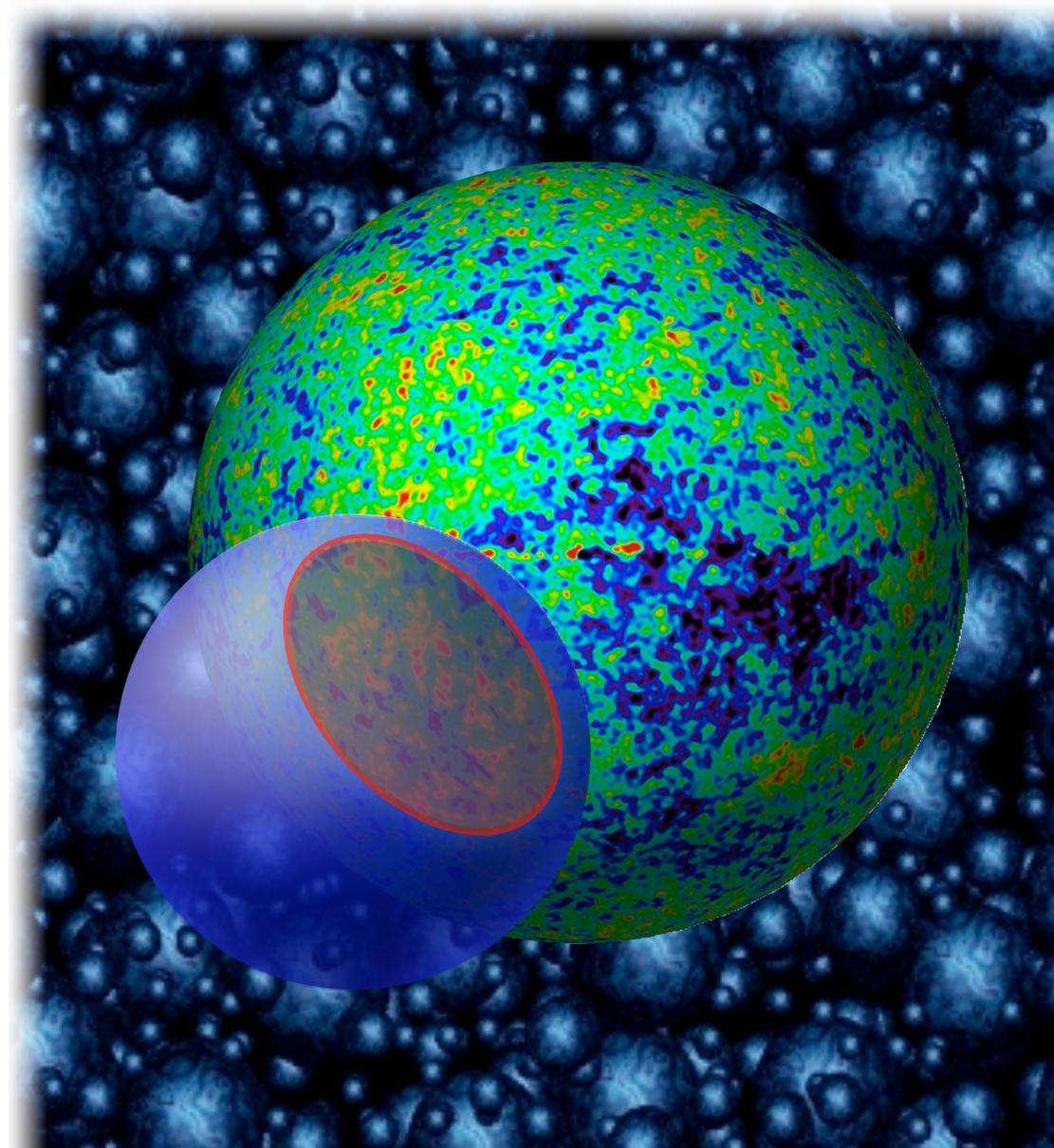
- Aguirre, Johnson & Tysanner 09
 - Bubble self-collisions: merge into homogeneous slices!
 - Two different bubbles: some perturbation, then return to homogeneity.
 - But: if inflation is 'fine tuned', disrupted in collision region: no foreign-born.
 - Many more possibilities:
 - Form yet lower vacuum bubbles (Easter et al.)
 - Multifield: lots more.



colliding decompactifying bubbles
(See Salem 10)

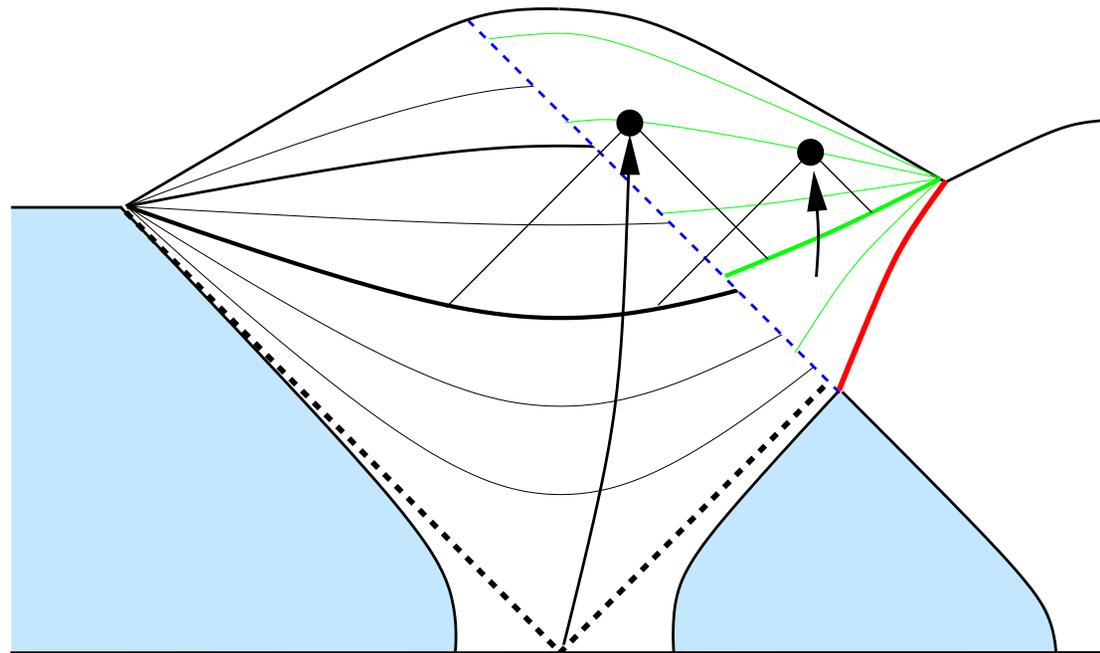
Observables (see Chang et al. 08; 09; Aguirre & Johnson 09)

- General considerations:
 - Must be no obliteration (but strong selection effect...)
 - Axisymmetric effects about collision direction.



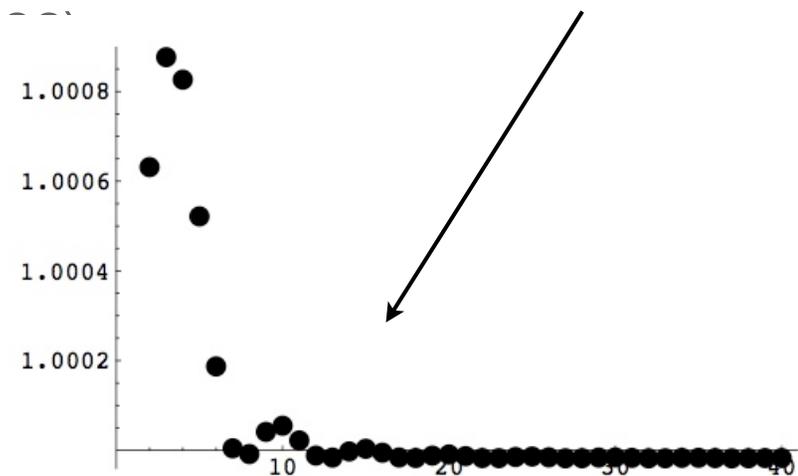
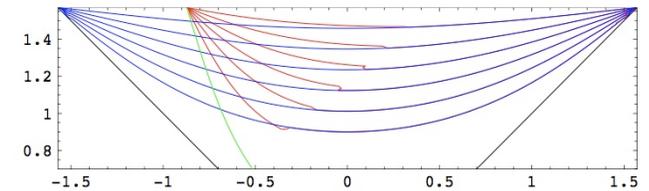
Observables (see Aguirre & Johnson 09; Chang et al. 08; 09)

- Collision ‘debris’:
 - Radiation wall, but probably too diluted to see.
 - Gravity waves vanish to first order (if progenitor bubbles have full $SO(3,1)$ symmetry).



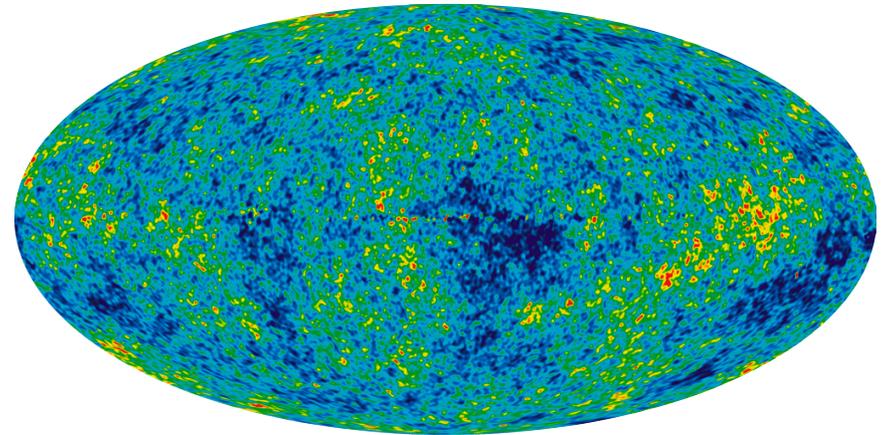
Observables

- Distortion of early equal-field surfaces
 - Density Perturbations (CMB, 21cm)
 - Polarization (see Levi talk)
 - Each collision: disk of affect.
 - Model as redshift back to perturbed reheating surface (Chang et al.)
 - In simple model, find C_l s
 - Should do 'real' perturbative calculation.
 - Large-scale flows possible

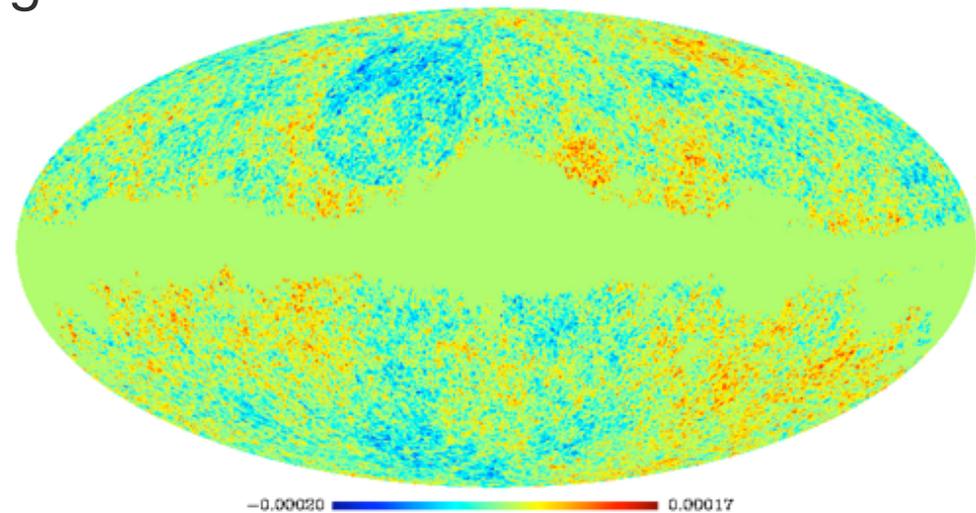


Bubble in Planck 1-year data?

- **A**ll-sky map data leak
- **P**rocessed with iterated self-similar wavelet edge-detection
- **R**edundant Bayesian prior analysis
- **I**ntegrated monte-carlo fold-in testing
- **L**ikelihood Fisher ratio of $\sim 10^8$
- **1st** non-vanilla inflation evidence?



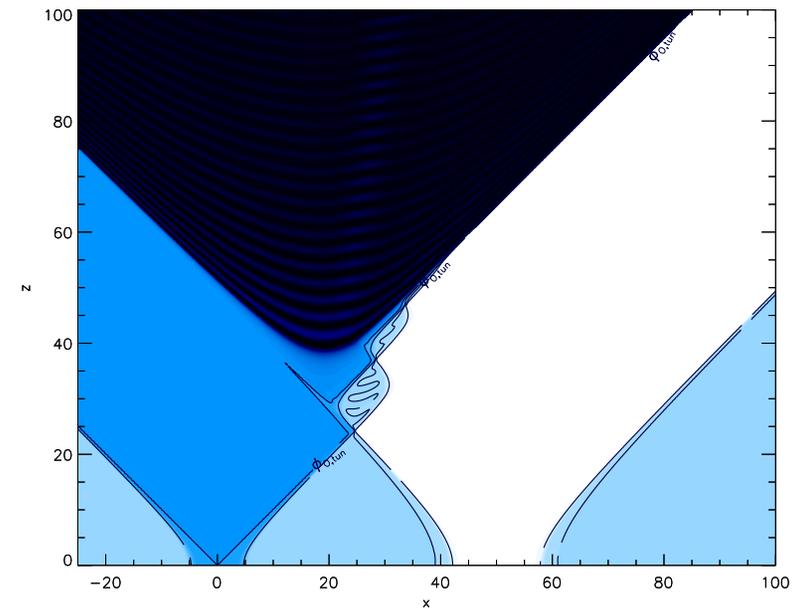
WMAP year 7 cleaned



Planck year 1, fractal wavelet edge-enhanced

Observables

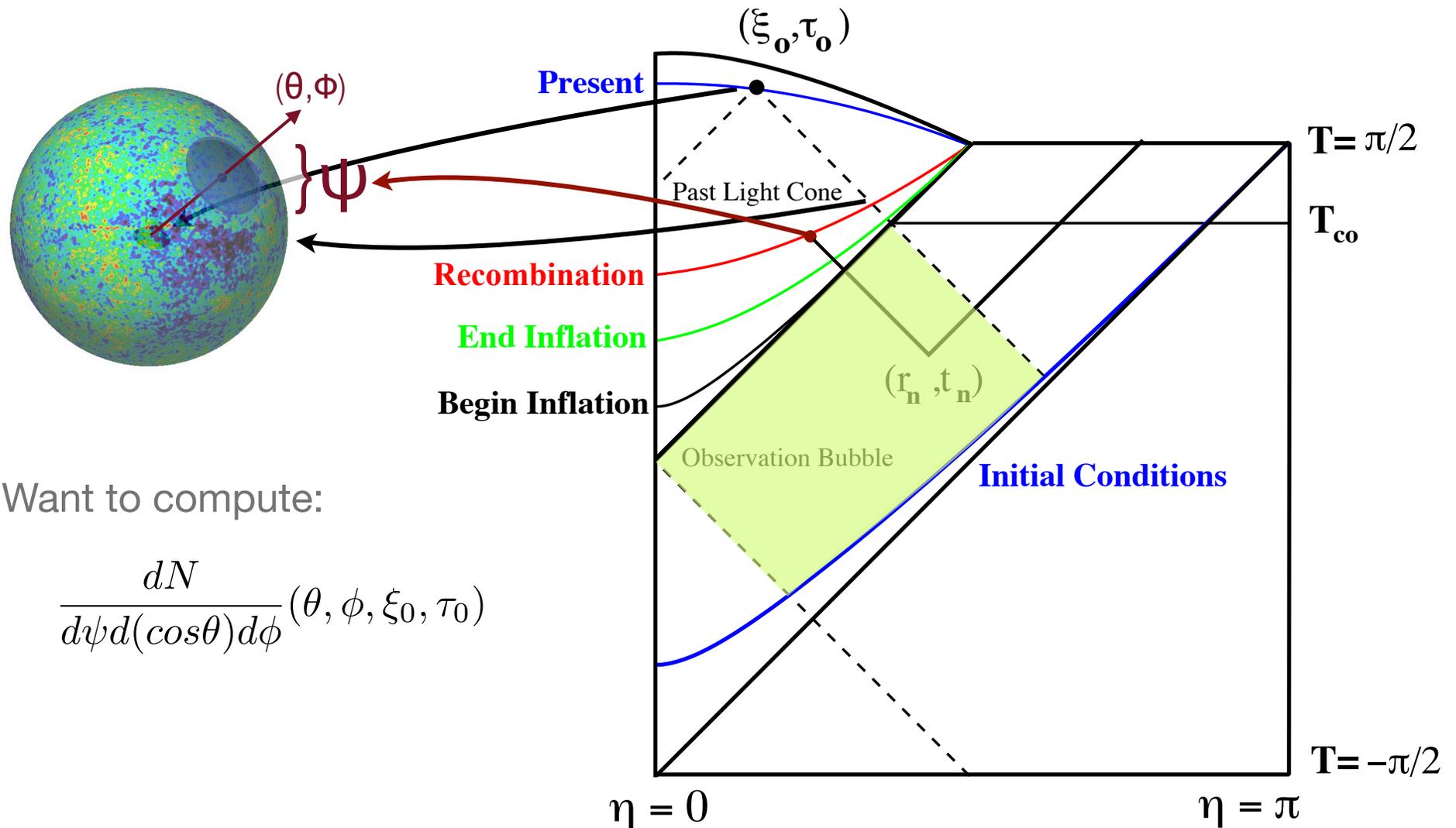
- Different inflationary history in collision region.
 - Disruption of inflation ('hole' in sky, falsifiable.)
 - Less e-folds in collision region.
 - Different field directions for multifield.
- Inflationary perturbations will be affected by this difference.



What are the probabilities for observing (various types of) collisions.

- Core Model (Garriga, Guth & Vilenkin 06):
 - Observation bubble forms at ‘late times’, so that we can model as $t=0$ bubble with $t \rightarrow -\infty$ initial ‘no bubble’ surface.
 - Incoming bubbles do not affect observation bubble.
 - Thin walls and small nucleation size \rightarrow incoming bubbles are lightcones.
 - How many bubbles enter observer’s past lightcone?
- 3 Extensions.

The setup

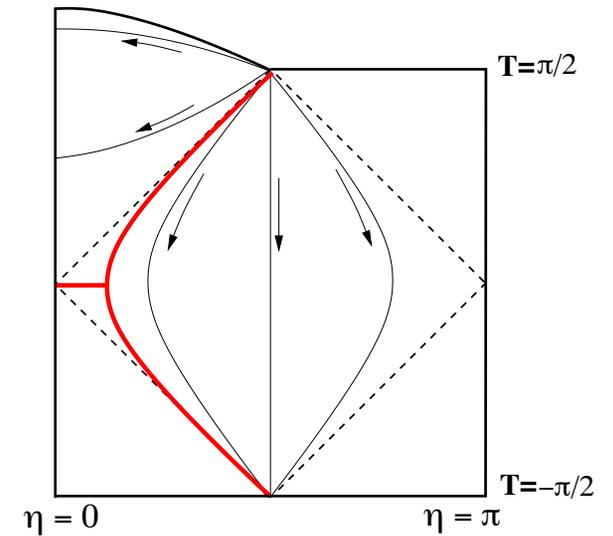


- Want to compute:

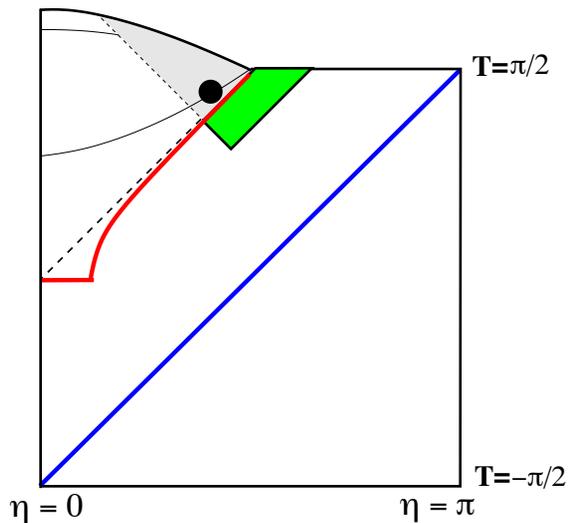
$$\frac{dN}{d\psi d(\cos\theta) d\phi}(\theta, \phi, \xi_0, \tau_0)$$

Frames and classifications

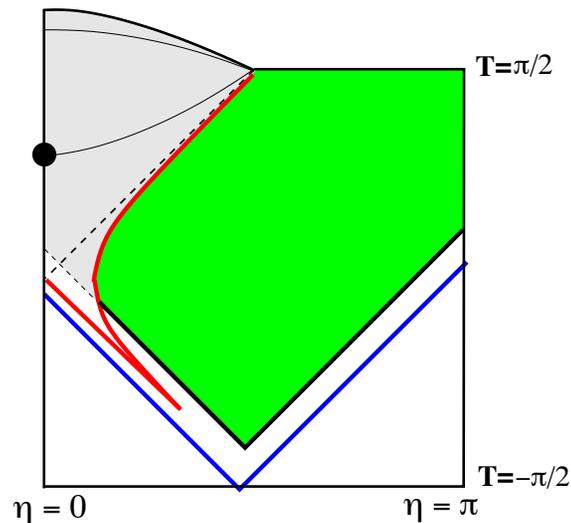
- Neglecting effect of collisions, we can ‘boost’ spacetime in well-defined way.



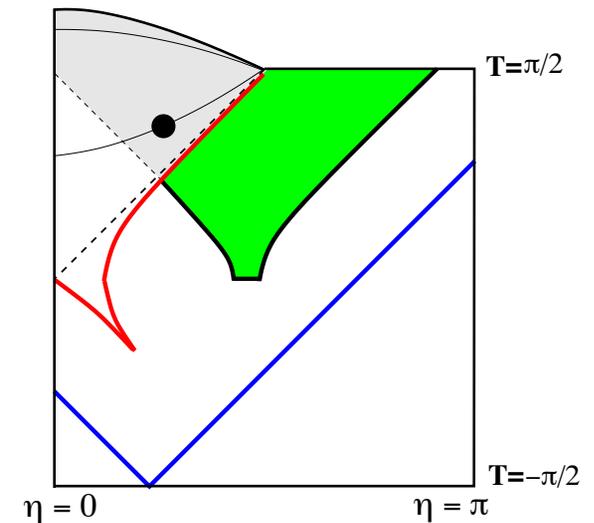
Steady-state frame



Observation frame

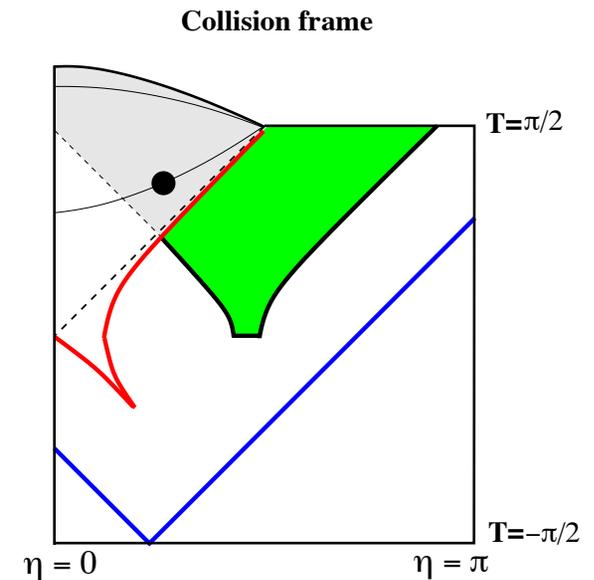
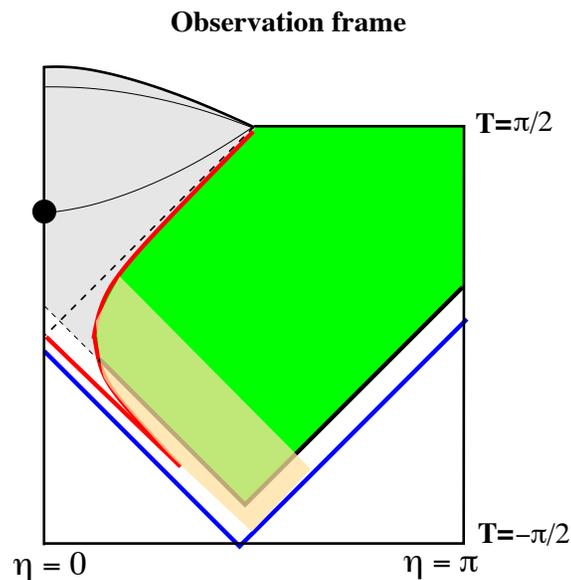
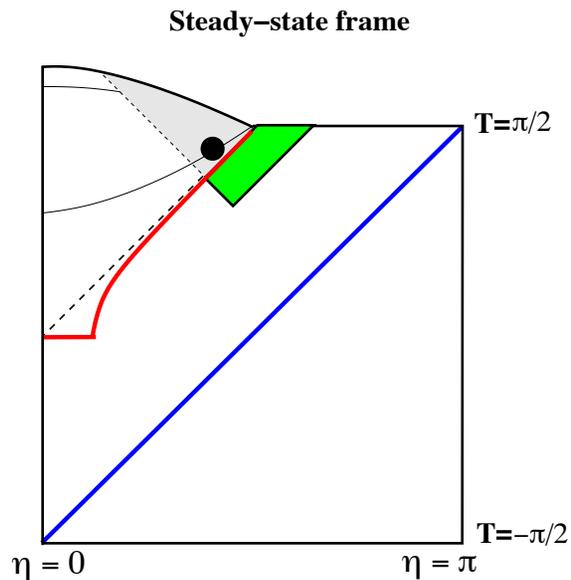


Collision frame



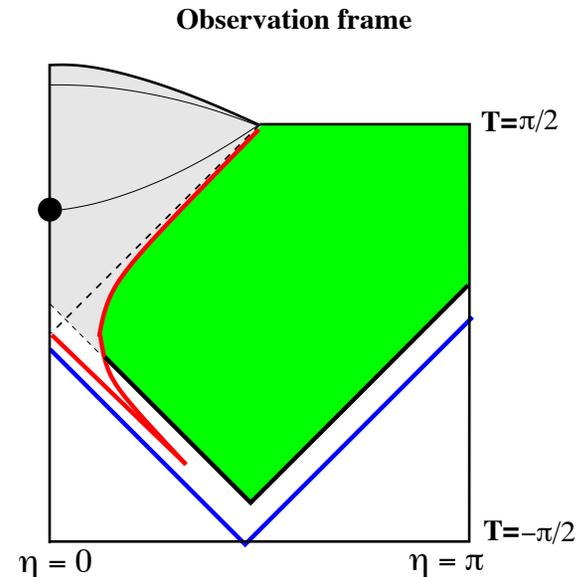
Frames and classifications

- Neglecting effect of collisions, we can ‘boost’ spacetime in well-defined way.
- Can put observer at origin, and can look for regions of large 4-volume inside past lightcone.



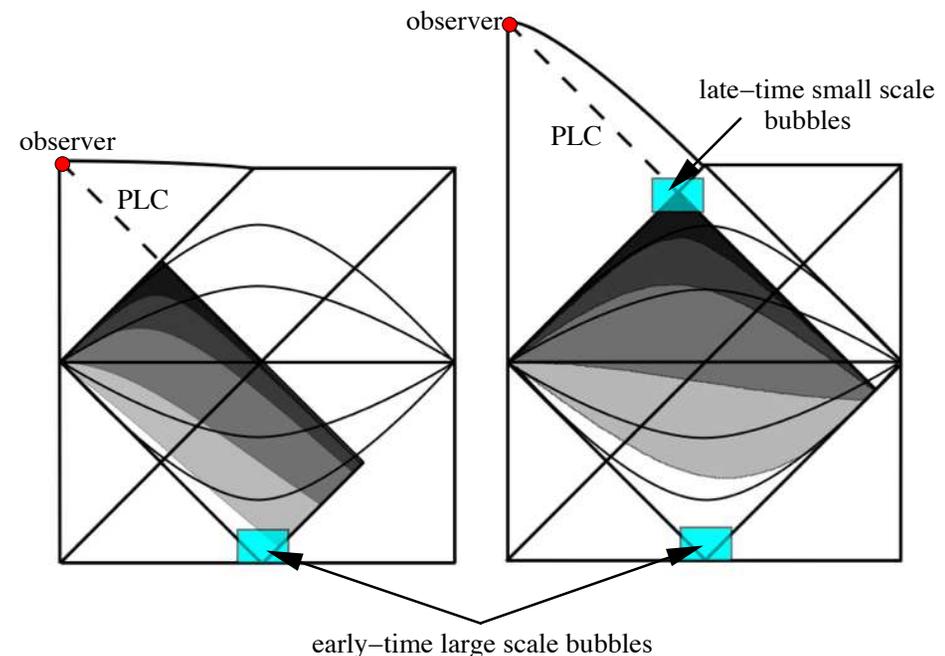
What are the probabilities: Results

- Core Model (Garriga, Guth & Vilenkin 06):
 - Go to observation frame.
 - Effect of boost is to distort initial condition surface.
 - Minimal expected number at zero boost, $N \sim \lambda(4\pi/3)H_F^{-4}$. Large-boost (up the bubble wall) gives divergent rate.
 - Preferred position pointing to preferred frame in background “persists”, “remembers” initial surface.



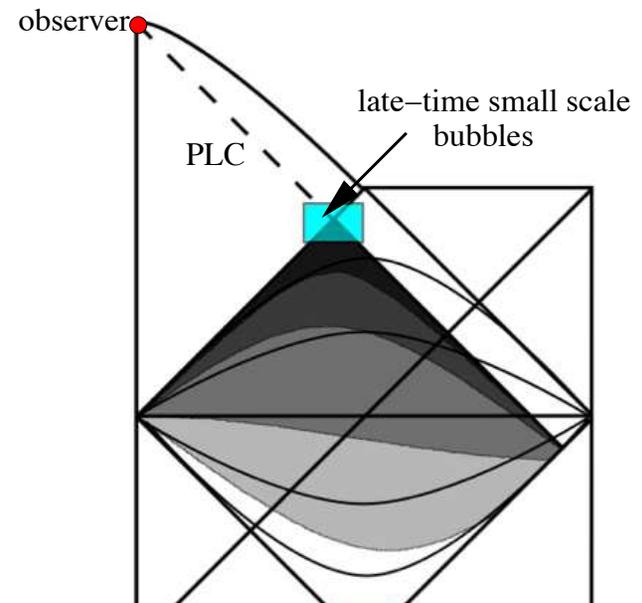
What are the probabilities: Results

- Extension I: Arbitrary FLRW cosmology inside observation bubble; what are angular sizes on $\tau \rightarrow 0$ surface? (Aguirre, Johnson & Shomer 07, 08; see also Gott 1984)
- Bimodal distribution, two classes of bubbles:
 - ‘Early’ bubbles enter p.l.c. at $\tau \ll H_I$, have large angular size, and have divergent number at large boost.
 - ‘Late’ bubbles enter p.l.c. at $\tau > H_I$, have range of angular sizes, boost-independent number.



What are the probabilities: Results

- Extension I: Arbitrary FLRW cosmology inside observation bubble; what are angular sizes on $\tau \rightarrow 0$ surface? (Aguirre, Johnson & Shomer 07, 08; see also Gott 1984)
- Number of 'late' depends on 'Hat size' from cosmology inside: how many false-vacuum Hubble 4-volumes H_F^{-4} can be seen.
 - With inflation inside at H_I , to 'solve horizon problem' or to get near-flatness, must see $O(1)$ inflationary Hubble volumes.
 - If $H_I < H_F$, boost of $(H_F/H_I)^2$. (Could be large!)
 - No further late-time enhancement unless there is curvature-dominated epoch.

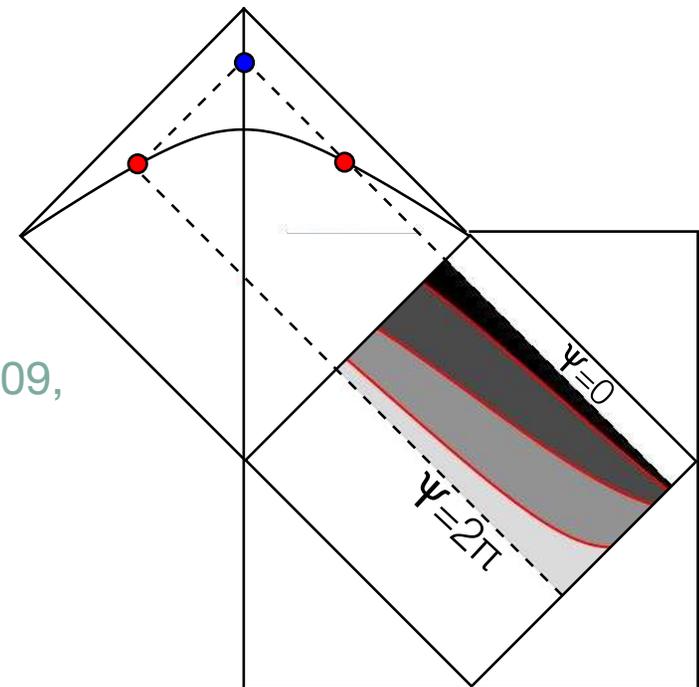


What are the probabilities: Results

- Extension II (Freivogel et al. 09: Ignore early and all-sky bubbles; assume collision effect propagates as null disturbances inside observation bubble; What are angular sizes Ψ on $\tau \neq 0$ *surface*?)
- For small current curvature, find disks of influence on last-scattering surface 'sky' obey

$$dN = \frac{4\lambda}{3} \left(\frac{H_F}{H_I} \right)^2 d(\cos \Psi) d\Omega_2^2$$

- This distribution is fairly flat. (see Aguirre & Johnson 09, for slight generalization, plots and details.)



What are the probabilities: Connecting to bubble structure.

- Extension III: What is the effect of back-reaction on the observation bubble?
(See AA et al. 09; AA & Johnson 09; Freivogel et al. 09:)
 - Extend 'homogeneous volume' measure across collision regions.
 - Restricted to native-born observers, not much difference.
 - But if they are allowed, 'all' observers should be foreign born (by the arguments of GGV)
 - But same argument re-capitulated applies: 'all' should be foreign-foreign born...
 - Global, (e.g. scale factor cutoff, etc.) may well matter.
 - Collisions may come in to global measure:
 - Comparing volumes in some ways -> 'victorious' bubbles have vastly more volume.
 - Bubbles allowing foreign-born observers may likewise have vastly more observers.

Conclusions

- **Basics results:**

- Even if the universe is not observably open, it may very well have formed in an open inflation bubble-nucleation event.
- In this case, our bubble will collide with infinitely many others.
- There's been huge progress in understanding the resulting picture. Some fun results:
 - Even for exponentially suppressed nucleation rates, these collisions probably lie to the past of most observers.
 - For large enough (but still small) nucleation rates, could see 'disks of influence' of finite angular size on CMB etc.
 - Depending on potential, collisions 'eat' either fraction 1 or 0 of the observation bubble.

Conclusions

- **Basics results:**

- Even if the universe is not observably open, it may very well have formed in an open inflation bubble-nucleation event.
- In this case, our bubble will collide with infinitely many others.
- There's been huge progress in understanding the resulting picture. The bottom line:
 - **If we live in open eternal inflation and if our parent vacuum can nucleate other bubbles (that do not invade ours) at a rate $\lambda H_F^{-4} > (H_F/H_I)^2$, and if there are not too many extra efolds of inflation in our bubble, then we should expect to 'see' collisions.**

Conclusions

- **Open questions:**

- Could bubble collisions be crucial for measures over vacua? Or vice-versa?
- What is the expected maximum nucleation rate from our parent vacuum?
- Any good reason to hope for the 'just right' number of e-folds?
- How, precisely, do the effects of the collision propagate inside the observation bubble? What is effect on CMB?
- What about more thick wall/large bubble, decompactifying, classical-transitioning, multifield, etc. models?
- *Are there bubble collisions in the observed sky (see Johnson, Pieris talks)?*